

Design of steel and Timber structure:

CE 651

1. Steel structure and their Analysis and Design.
 - 1.1 Introduction to steel structure
 - 1.2 Structural steel and classification
 - 1.3 Method of analysis & Design
 - 1.4 Design process and Basis

A steel structure is an assemblage of a group of member or elements expected to sustain their share of applied forces.

Design of steel structure involves:

- a) functional design
- b) structural design

a) functional design: The planning of structure for specific purpose such as ventilation, lighting, aesthetic view etc.

b) structural design: It consists of proportioning various elements of the building in the most economical manner, so that load acting on it are transferred safely to ground without using excess material.

The members are usually subjected to axial force, bending, or torsion or the combination of all loads. Axial force is either T (tve) or C (ve).

Member force

Tie Tensile

column or strut compression

Beam bending

Advantage and disadvantage of steel structure.

A) Advantage

- i) High strength per unit weight, result in smaller section should be used.
- ii) Posses high ductility so it doesn't fail suddenly.
- iii) Structural steel are tough, having both strength & durability so during fabrication & erection steel member will not fracture easily.
- iv) Light in weight so easy to handle and transport.
- v) Steel is ultimate recycleable material and has higher salvage value.

B: Disadvantage:

i) It is susceptible to corrosion therefore they required frequent painting & maintenance.

- ii) For fabrication and erection skill manpower is required.
- iii) Initial installation is so costly.
- iv) Maintenance cost is also high.

Use of steel as a building material:

- a) Bridge over a tank
- b) Highrise building
- c) Industrial buildings
- d) Transmission towers

2. Structural steel: It is an alloy of iron & carbon. It is a standard steel carbon content is 0.2 to 0.35%, carbon contributes to strength but reduce ductility. Structural steel has been classified by (BIS) based on ultimate or yield strength.

Physical property:

a) Modulus of Elasticity	$E = 2 \times 10^5 \text{ N/mm}^2$
b) Shear modulus	$G = 0.769 \times 10^5 \text{ N/mm}^2$
c) Poisson's ratio	$\mu = \begin{cases} 0.3 \text{ Elastic} \\ 0.5 \text{ Plastic} \end{cases}$

d) Coefficient of thermal expansion: $(\alpha) = 12 \times 10^{-6}/^{\circ}\text{C}$

e) unit mass of steel (ρ) = 7850 kg/m^3

steel as a structural material:

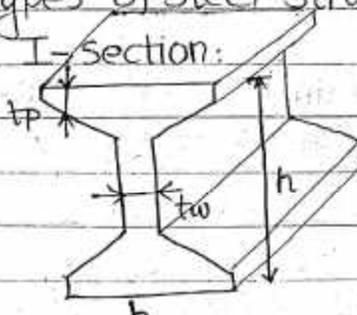
Structural steel is a material used for steel construction, which is formed with a specific shape following standards of chemical composition and strength. They can also be defined as hot rolled products, with a x-section of special form like angle, channel and beam/joints steel has always been more preferred to concrete because steel offers better tension and compression thus result in light construction. Usually steel uses three dimensional trusses hence making it larger than its concrete counter part.

Technique to produce wide range of structure and shape.

- High precision stress analysis
- Computerized
- Innovative joints.

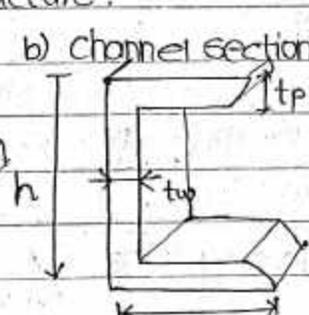
Types of steel structure:

a) I-section:



uses: Beam and column

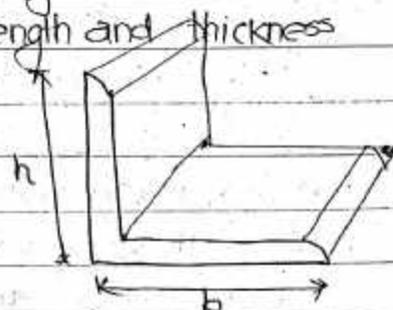
b) Channel section:



uses: Beam/column (heavy)

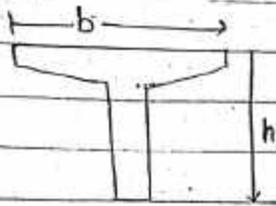
c) Angle section:

length and thickness



uses: compression and Tension member

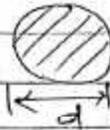
d) T-section:



uses:- compression and tension member of door & window.

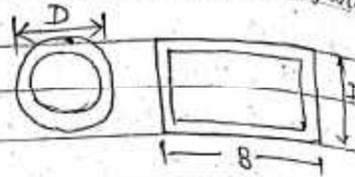
e) Rolled steel Bars:

round bar designated by diameter



f) Rolled steel, Tubular section:

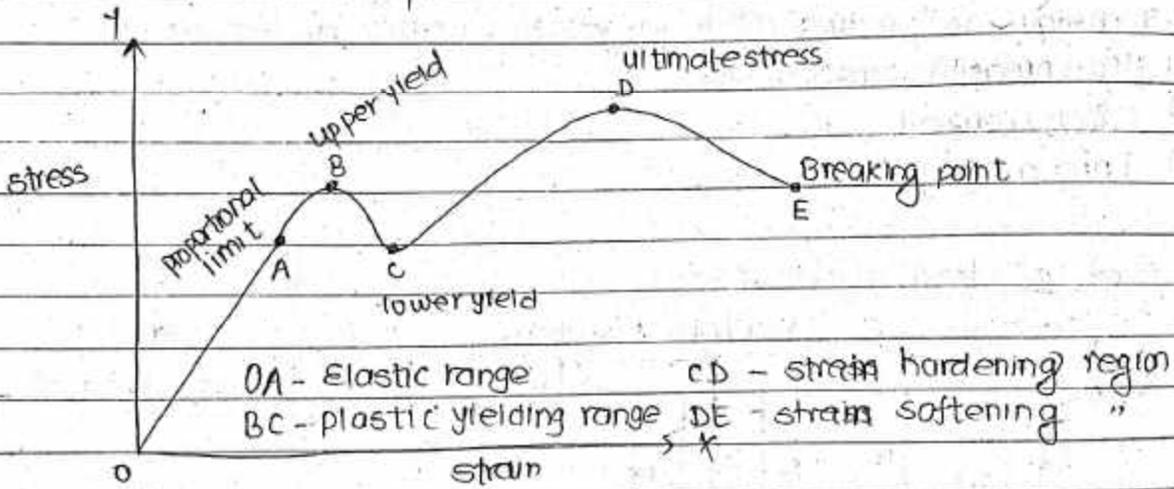
designated by outside diameter and self wt.



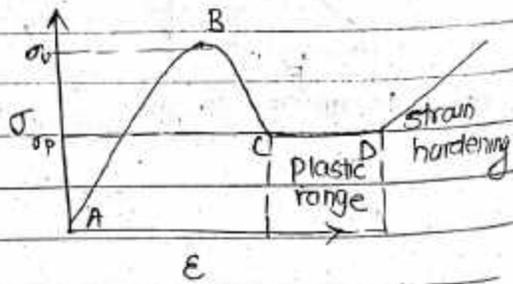
uses: compression member of roof & truss:

Loads: The force that act on a structure are called loads. for safe design of structure it is essential to have a knowledge of various material or man made or combined load acting on it.

Stress strain relationship:



since, plastic range is sufficiently large and it seems reasonable to extent it without limit that is to ignore the effect of strain hardening.



strain hardening : or work hardening.

It is the strengthening of a metal by plastic deformation, which occurs because of dislocation movements and dislocation generation within the crystal structure of materials. Many non-brittle metals having high melting point can be strengthened by this effect.

Design philosophy:

⇒ Design of steel structure consists of design of steel members and their connections, so that they can safely and economically resist and transfer applied load to ground. The design process begins with selection of trial section & checking its safety.

The design are based on :-

- a) attainment of full yielding
- b) Tensile strength
- c) critical buckling
- d) Max. deflection permitted
- e) stress concentration
- f) fatigue
- g. Brittle fracture.

Philosophy:

- a) Working stress method
 - b) Limit state method
 - c) Ultimate stress method
- 1) Ultimate tensile strength: It is max. stress that the material can withstand while being stretched or pulled before failure
- 2) Yield strength: stress at which stress-strain curve for axial loading deviates the strain of 0.2% from linear elastic to non-linear curve.

Working stress Method:

a) It is an elastic method of design. According to this method, members are designed on the basis of working stress and those will never exceed the permissible stress.

A permissible stress is defined as the ratio of yield stress according to factor of safety:

$$\text{Permissible stress} = \frac{\text{yield stress}}{\text{FOS}}$$

Basic assumptions:

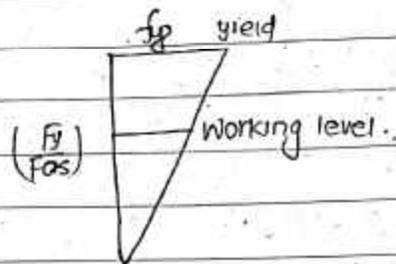
- a) Material is homogenous and isotropic
- b) Material is assumed to be linearly elastic.
- c) It is a deterministic approach:

suppose $f_{ck} = 20 \text{ N/mm}^2$ at least 20 N/mm^2 $\frac{f_{yk}}{f_{ck}} \geq 1.0$

d) Working or service load is not modified.

e) Permissible stress = $\frac{\text{Yield stress}}{\text{FOS}}$ (obtained by modification)

f) FOS : in steel: 1.6 to 1.92 $\text{FOS}_{\text{avg. value}} = 1.78$
 in concrete: FOS = 3



Permissible or allowable stress

- a) Tension/compression $= 0.6 f_y$
- b) Bending $= 0.66 f_y$
- c) Shear $= 0.45 f_y$

Limitation: i) failure load is factor of safety x working load, which is not true
 ii) actually it is more because a material can resist load after yield occurs at failure

iii) In structure just formation of plastic hinge is not the collapse criteria, still can resist more load till collapse mechanism is formed

iv) It gives uneconomical section

v) deals only elastic behaviour.

Advantage:

This method is simple and reasonably reliable.

working stress is low, serviceability requirement are satisfied

Limit state method:

It is similar to plastic design which consider most critical limit state of strength and serviceability.

⇒ The acceptable limit for the safety and serviceability requirements before the failure occurs is called limit state:

The section design should satisfy serviceability requirements such as limitation of deflection & vibration and shouldn't collapse under the accidental loads.

There are two limit states:

a) Limit state of strength:

for checking the strength and stability of structure, the load are multiplied by relevant load factor (γ_f) Table: 4: IS: 800 - 2007.

The modified load are called factor loads account for uncertainties involved in estimating the magnitude of dead and live loads.

The design strength of members or its connections are determined by dividing ultimate strength w.r. to partial safety factor (γ_m) for materials: IS 800-2007 table 5.

b) Limit state of serviceability:

It is the limit state beyond which the service criteria such as deflection, vibration, repairable damage due to fatigue, corrosion, fire resistance.

load factor (γ_f) is used for all load to check serviceability requirements:

Codes for loads:

IS 875 - Part 1 Dead load

IS 875 - Part 2 or 4 live load

IS 875 - Part 3. wind load

IS 1893 earthquake load.

Mechanical property of steel:

- a) Elasticity b) Plasticity c) Ductility d) Brittleness e) Hardness
f) fatigue g) creep h) Malleability i) slow deformation

Malleability: Property of material due to which it can be rolled into thin sheet of metal without toughness. It can be stretch, bend, twisted under a high stress before failure.

Assumptions of Limit state design.

a) Material is homogenous and isotropic

b) Material behaviour is elastoplastic

c) It is a probabilistic approach

d) Working load or service load is modified by partial safety factor for load: $PSF = 1.5$

e) Design load/action $Q(d) = \gamma_f \times Q$

γ_f - partial safety factor

Q - service/working load.

f) Design strength is obtained by modifying (yield to ultimate) stress by PSF
ie, Designed strength (S_d) = $\frac{S}{\gamma_m}$

γ_m - partial safety factor for material

S - yield to ultimate stress

for yield $\therefore \gamma_{m0} = 1.1$

$\gamma_{m0} = 1.1$ (buckling)

Difference between:

WSM

- a) It is a traditional method
- b) It is not economical
- c) It is deterministic approach
- d) Material is linearly elastic
- e) Working or service load is not modified and reduced
- f) Designed stress is modified by FOS
- g) Simple and reliable method calculation

LSM

- a) It is a modern method
- b) It is more economical
- c) It is probabilistic approach
- d) Material is elastoplastic
- e) Modified by partial safety factor
- f) Designed stress is modified by partial safety factor
- g) Design is more complex as compared to WSM.

Safety and serviceability requirement of structure

The design of steel structure should satisfy the safety and serviceability requirement regarding strength, serviceability, brittle fracture, fatigue, fire and durability even during worst combination of load structure should meet following requirements:-

- a) Remain fit and adequate reliable and able to sustain all loads
- b) Have adequate durability under normal maintenance
- c) Do not suffer overall damage or collapse disproportionality under accidental loads like explosions, impact, human error.

The catastrophic damage can be limited by:-

- a) avoiding the exposure to hazard
- b) choosing structural forms, layout & details during designing
- c) choosing suitable materials, designing and detailing procedure

Design process and Basis for Design:

It is a process to decide shape, size and connection details of both concrete and reinforcement so that structure being designed will perform satisfactory during its intended life, with an required degree of safety.

⇒ Basis of Design of structure

- a) sustain all loads expected on it
- b) Sustain deformation during and after construction
- c) Should have adequate durability
- d) should " " resistance to misuse and fire
- e. structure should be stable and have alternate load path to prevent overall collapse under accidental loadings.

Grade of steel:

Steel grade classify various steels by their composition & physical properties

As per IS 2062: 2006. 9 grades of steels are designated as

F165, E 250 A, E 250 B, E 250 D, E 300, E 350, E 410, E 450 (D), E 450 (E)

Numerical value - yield strength in Mpa.

These grades of steel have their own chemical composition & mechanical properties.

Classification of Structural steel as per IS.

g) Hot rolled sections: various products made using this methods are plate, strip, shape & section, flat, bars as per IS:

1. Beam: (ISJB, ISLB, ISMB, ISWB)

2. Column (ISSC, ISHB)

3. Parallel flange Beam / column - ISMPB, ISWPB

4. Channel: ISJC, ISLC, ISMC, ISMC?

5. Angle. ISA

6. T section: ISNT, ISDT, ISLT, ISMT, ISHT

7. Tubular

8. Rectangular / Hollow

cold formed light-gauge:

cold formed light gauge are used where thicker hot rolled section become uneconomical in small building subjected to lighter load. They are produced from steel strips, generally not thicker than 8mm, for mass production. They are produced by cold rolling. They are available in the form of equal angle, unequal angle, channel, hat section, denoted by depth x width x thickness.

Classification of steel according to moment rotation capacity.

plastic x-section.	compact x-section	semicompact	Slender x-section
develop full plastic moment	develop full plastic moment	stress in extreme fiber limited to yield	yield in the extreme fibre can't be attained
allow sufficient rotation	buckling prevent	local buckling	premature
redistribution of moment	required rotation	prevent development of full plastic moment	local buckling occurs in the elastic range.
take place until failure mechanism occurred			

advantages of steel structures: ✓

Design in tension, compression, bending and shear.

while designing a structural member subjected to Tension, compression, Bending & shear, allowable stress are as follows:-

$$\text{tensile stress } (\sigma_{tu}) = 0.6 f_y$$

$$\text{compressive, } (\sigma_{ca}) = \lambda f_y$$

λ = Slenderness ratio

$$\text{bearing stress} = 185 \text{ Mpa}$$

$$\text{max. bending tension/compression} = 0.66 f_y$$

$$\text{max. Shear stress } (\tau_{vm}) = 0.42 \text{ to } 0.45 \times f_y$$

Different limit state for Steel design:

A) Limit state of strength:

- a) loss of equilibrium of whole or part of structure
- b) loss of stability
- c) failure by excess of deformation
- d) fracture by fatigue
- e) Brittle fracture

B) limit state of serviceability:

- i) Deflection & deflection affect the appearance of structure
- ii) vibration cause ^{loss of} functional effectiveness
- iii) repairable damage or crack due to fatigue
- iv) Corrosion
- v) fire

CH: 4 Structural Steel Connections

Connection:

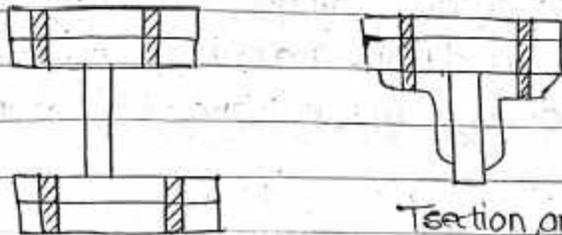
- a) Permanent connection (i) Welded ✓
(ii) Riveted (Introduction)

- b) Temporary connection (i) Bolted ✓
(ii) Nailed ✗

Various elements of steel structure like Tension, compression and flexural members are connected - fasteners or connectors.

Needs of connection

- a) To transmit load from one member to another
b) assemblage of individual member to form composite section.
connecting
eg. Plates, angles, channels, I section

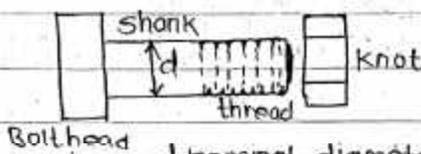


T-section, angle and plates

- c) connections of two length of a member to make up a required length.

a) Bolted connection :-

A bolt may be defined as a metal pin with a thread at one end, a shank threaded at other end to receive a nut.



Bolts are used for joining together pieces of metals by inserting them through holes in the metal and tightening the nut at threaded ends.

Based on load Transfer:

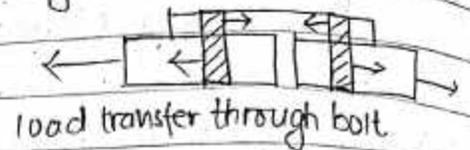
Types of Bolt features

- a) Bearing type bolt: - load transfer by shearing action
- Suitable for light structure
- not suitable for vibration, fatigue
- suitable for static loading

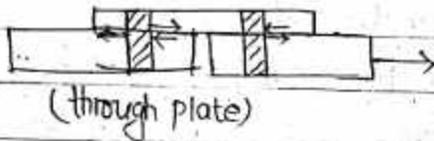
(Designation) Nominal diameter: 12, 16, 20, 22, 24, ...

designated as M12, M16, M20, M22, ...

eg: Slip critical connection



- b) High strength friction grip bolt (HSFG): Transfer load by friction
- Suitable for heavy structure
- Suitable for vibration and fatigue
- Suitable for dynamic & static loading



It is made from high strength steel rod and surface is finished. Bolt are tightened by using calibrated wrenches and knots are provided by clamping devices. The shearing load is restricted by frictional force betⁿ shank and member and washers.

Nominal diameter: 16, 20, 24, 30, 36.

Property class of bolt (Pr. CI.)

The ratio of net tensile area at thread to nominal plain shank area of bolt is 0.78.

$$A_n = 0.78 A_s$$

A_n - area at root of threads / stress / proof area.

Common bolt is black bolt of class 4.6 and 8.8 are available

It is represented as $x.y$

$x = \frac{1}{10}^{\text{th}}$ of ultimate tensile strength of bolt in kgf/mm^2

$y = \text{fraction of } \frac{1}{10}^{\text{th}}$ of ultimate tensile strength as yield strength of bolt.

3.6, 4.6, 4.8, 5.6 - Bearing type

9.8, 10.8, 12.9 (HSFG)

$x.y$

for eg:- tensile for Pr. cl: 4.6

$$\begin{aligned} \text{ultimate strength of bolt } f_{ub} &= 40 \text{ kgf/mm}^2 \\ &= 40 \times 9.81 \text{ N/mm}^2 \\ &= 392.4 \text{ N/mm}^2 \\ &\approx 400 \text{ N/mm}^2 \end{aligned}$$

$$\begin{aligned} \text{so, Yield tensile strength of bolt } (f_{yb}) &= \frac{y}{(x+y)} \cdot f_{ub} \\ &= \frac{6}{(6+4)} \times 400 \\ &= \frac{6}{10} \times 400 \\ &= 240 \text{ N/mm}^2 \end{aligned}$$

Specification for spacing:

P should not be less than $2.5d$ ($P \geq 2.5d$)

d - nominal diameter of bolt

P is $\geq 16t$ or 200mm

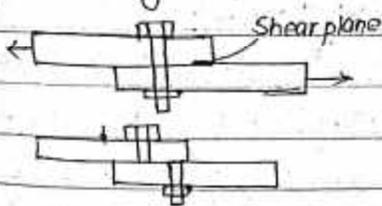
$P \geq 16t$ } tension
200mm

$P \geq 12t$ } compression
200mm

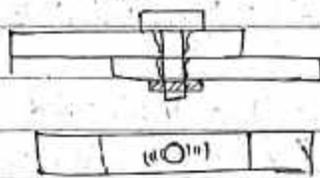
t - thickness of thinner plate.

Plate in a joint made with Bolted joint failure under 3 causes:

(a) shearing failure

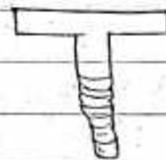


(b) Bearing failure



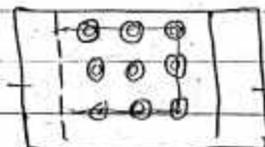
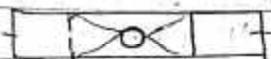
(b) crushing or tearing

(c) Tension failure



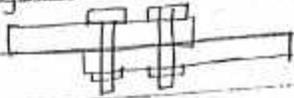
Block shear failure

(a) yielding of plate

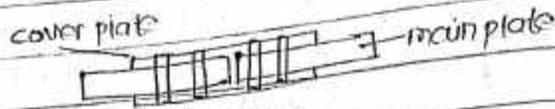


Type of bolted joints

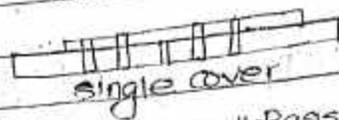
a) Lap joints



(b) Butt joints (end-to-end connection)

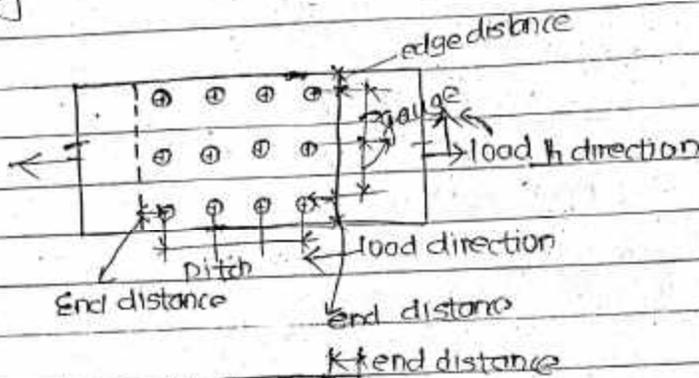


Double cover



Single cover

Design parameters and design specification: on the basis of



Type of force

Shear - lap and butt joints

Tension - hanger connection

combined (T+T) = When inclined member is to be connected to through column through bracket
eg: Connection of bracing.

Specification: 10:2.2 clause page 73/74

1. Diameter of hole (d_o/d_n) = Nominal diameter (d) + clearance

(table: 19 page 73) IS-800

2. Pitch of bolt shouldn't be less than $2.5d$ (d - nominal diameter)

$$Pitch \neq 2.5d \text{ or } Pitch \geq 2.5d$$

3. Pitch shouldn't be greater than $3t$ or 300mm whichever is greater in general

$$P \neq 16t \text{ or } 200 \text{ mm (T+ve)}$$

$$P \neq 12t \text{ or } 200 \text{ mm (C-ve)}$$

Fe - 410

$f_u = 410 \text{ MPa}$

$f_y = 250 \text{ MPa}$

t = thickness of thinner plate.

4. End distance shouldn't be less than $1.5d_o$, in case of machine flame cut

$1.7d_o$ in case of hand flame cut

5. Max. end distance shouldn't be greater than $12 \times t E_o$

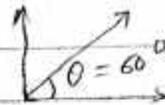
$$E_o = \sqrt{\frac{250}{f_y}}$$

Design strength of bolt in ::

a) shear strength of bolt:

Nominal shear strength of bolt: Page: 75 clause 10.3.3

$$(V_{nsb}) = \frac{f_{ub} \times (\eta_n A_{nb} + \eta_s A_{sb})}{\sqrt{3}}$$



f_{ub} = ultimate tensile strength of bolt

η_n = no. of shear planes intercepting with threaded portion of bolt

A_{sb} = area of shank or non threaded portion ($\pi d^2/4$)

η_s = no. of shear planes intercepting with non. threaded portion of bolt

A_{nb} = area of threaded portion (generally $0.78 A_{sb}$)

b) Design shear strength of bolt:

$$(V_{dsb}) = \frac{V_{nsb}}{\gamma_{mb}}, \quad \gamma_{mb} \text{ - partial safety factor for bolt:}$$

Table: 5, Page: 30

B) Bearing capacity of bolt: Page 75, 10.3.4

a) nominal bearing capacity of bolt:

$$(V_{npb}) = 2.5 k_b d t (f_u \text{ or } f_{ub})$$

k_b is lesser of

$$\frac{e}{3d_o}, \frac{p}{3d_o}, 1, \frac{f_{ub}}{f_u}$$

bolt
plate

p - pitch distance

e - end distance

d - nominal diameter

t - thickness of thinner plate

d_o = diameter of hole

f_{ub} - ultimate tensile strength of bolt

b) Design bearing strength of bolt: $(V_{d,b}) = \frac{V_{npd}}{\gamma_{mb}}$

c) Tensile strength of bolt: (10.3.5) / page 76

i) Nominal tensile strength of bolt: $= 0.9 f_{ub} A_{nb} \leq \frac{f_{yb} A_{sb}}{\gamma_{mo}}$

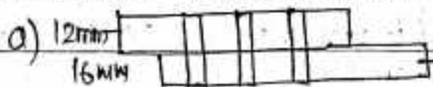
γ_{mo} = partial safety factor for yielding

Table: 5 page: 30

ii) Design tensile strength of bolt: $T_{db} = \frac{T_{nb}}{\gamma_{mb}}$

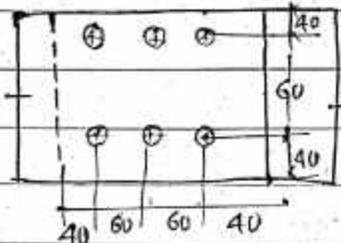
Numerical

Calculate bolt value, in following cases:



All dimension in mm

Use M20 bolt Pr. Cl. 4.6



Nominal diameter (d) = 20 mm

hole diameter (d_h) = 20 + 2 = 22 mm

page: 73, table-B

ultimate tensile strength of bolt $f_{ub} = 400 \text{ MPa}$

critical: threaded portion yield " " " " " $f_{yb} = 240 \text{ MPa}$

pitch distance $p = 60 \text{ mm}$

Design:

end distance $e = 40 \text{ mm}$

a) Shear strength of bolt: $V_{dsb} = \frac{f_{ub} (n_n A_{nb} + n_s A_{sb})}{\sqrt{3} \gamma_{mb}}$

$$= \frac{400}{\sqrt{3} \times 1.25} \left(1 \times 0.78 \times \frac{\pi \times d^2}{4} \right) = 45.27 \text{ kN}$$

assuming: shear plane intercept with threaded portion of bolt

$$n_n = 1$$

$$n_s = 0$$

Page 30, table: 5 $\gamma_{mb} = 1.25$

b) Design Bearing capacity:

k_b is at least:

$$\frac{e}{3d_0}, \frac{P}{3d_0}, 1, \frac{f_{ub}}{f_b}$$
$$\Rightarrow \frac{40}{3 \times 22}, \frac{60}{3 \times 22} \cdot 0.25, 1, \frac{400}{410}$$

$$\boxed{0.606}, 0.659, 1, 0.976$$

$$\therefore k_b = 0.606$$

$$V_{dpb} = \frac{V_{npb}}{\gamma_{mb}} \quad \text{(least among them)}$$
$$= \frac{2.59 k_b d t (f_u \text{ or } f_{ub})}{\gamma_{mb}}$$

$$= \frac{2.59 \times 0.606 \times 12 \times 400}{1.25}$$

$$= 116.352 \text{ kN}$$

c) Tensile bearing strength of bolt:

Design tensile strength $T_{db} = \frac{T_{nb}}{\gamma_{mb}}$

$$T_{nb} = 0.9 f_{ub} A_{nb} \leq f_y b A_{sb} \gamma_{mb}$$

$$= 0.9 \times 400 \times 0.78 \times \frac{\pi d^2}{4} \leq \frac{240 \times \pi d^2}{4} \times \frac{1.25}{1.1}$$

$$= 88.216 \leq 85.679 \text{ kN}$$

least among them

$$T_{db} = \frac{85.679}{1.25}$$

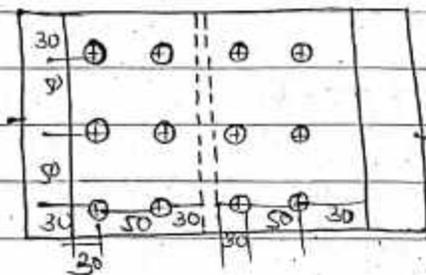
$$= 68.5 \text{ kN}$$

Bolt value = min. of shear, bearing and Tensile capacity of bolt
 = 45.27 kN

Bending आरम्भ Tensile strength एनि check जात 1.

Connection Design:

(B)



$d = 16 \text{ mm}$

$d_o = 16 + 2 = 18 \text{ mm}$

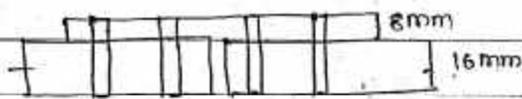
clearance 2mm

$e = 30 \text{ mm}$

$p = 50 \text{ mm}$

$f_{ub} = 400 \text{ N/mm}^2$

$f_{yb} = 240 \text{ N/mm}^2$



① Design shear capacity of bolt

$$(V_{dsb}) = \frac{f_{ub}}{\sqrt{3} \times \gamma_{mb}} (n_n A_{nb} + n_s A_{sb})$$

Use M16 bolt of Pr. Cl 4.6

Now,

assume, shear plane lies on thread

$n_n = 1, n_s = 0$

$$V_{dsb} = \frac{400}{\sqrt{3} \times 1.25} (1 \times 0.78 \times \frac{\pi}{4} \times 16^2)$$

$$= 28.97 \text{ kN}$$

② Bearing capacity

k_b is least of

$$\frac{e}{3d_o}, \frac{p - 0.25}{3d_o}, 1, \frac{f_{ub}}{f_u}$$

$$\text{or, } \frac{30}{3 \times 18}, \frac{50 - 0.25}{3 \times 18}, 1, \frac{400}{410}$$

$$\therefore 0.556, 0.676, 1, 0.976$$

$$\text{so, } k_b = 0.556$$

$$(V_{dpb}) = \frac{2.5 k_b d t (f_u \text{ or } f_{ub})}{\gamma_{mb}} = \frac{2.5 \times 0.556 \times 16 \times 8 \times 400}{1.25} = 56.889 \text{ kN}$$

Tensile:

$$(T_{db}) = \frac{T_{nb}}{\gamma_{mb}}$$

Since,

$$T_{nb} = 0.9 f_{ub} A_{nb} \leq f_{yb} A_{sb} \frac{\gamma_{mb}}{\gamma_{mo}}$$

$$= 0.9 \times 480 \times \frac{0.78 \times \pi \times 16^2}{4} \leq 240 \times \frac{\pi \times 16^2}{4} \times \frac{1.25}{1.10}$$

$$= 56458 \leq 54835$$

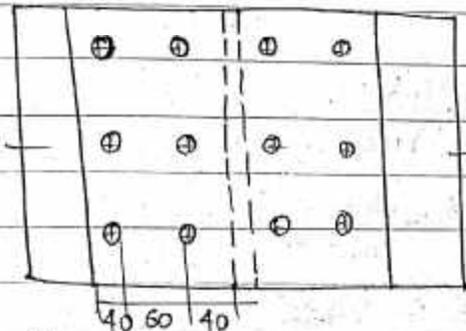
$$\text{So, } T_{db} = \frac{54835}{1.25}$$

$$= 43868 \text{ KN}$$

$$\text{Bolt value} = \text{least among } V_{dsb}, V_{dps}, T_{db}$$

$$= 28.97 \text{ KN}$$

©



1 shear plane in threaded region
1 shear " " un " "
 $N_n = 1, N_s = 1,$

use M20 bolt of pr. cl \Rightarrow 4.6

Now:

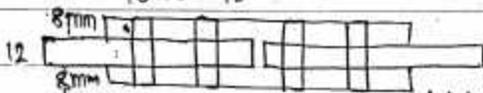
$$d = 20 \text{ mm}$$

$$\text{clearance} = 2 \text{ mm}$$

$$d_o = 22 \text{ mm}$$

$$f_{ub} = 480 \text{ Mpa}$$

$$f_{yb} = 240 \text{ Mpa}$$



function गर्दा कत acid गर्दा

$$t_1 = \text{⊕} + 8 = 16 \text{ mm}$$

$$t_2 = 12 \text{ mm (least)}$$

2. In case of double cover butt joint, eccentricity force doesn't exist so bending is eliminated but not in lap joints

$$\begin{aligned}
 \text{a) Designed shear strength} &= V_{dsb} = \frac{f_{ub} (A_{n1} A_{nb} + n_s A_{sb})}{\sqrt{3} \times \gamma_{mb}} \\
 &= \frac{400 (1 \times 0.78 \times 71 \times 20^2 + 1 \times 71 \times 20^2)}{\sqrt{3} \times 1.25} \\
 &= 103.314 \text{ KN}
 \end{aligned}$$

$$\text{b) Designed Bearing capacity (} V_{dpb} \text{)} = \frac{2.5 k_b d t (f_u \text{ or } f_{ub})}{\gamma_{mb}}$$

$$\frac{e}{3d_0}, \frac{p}{3d_0} = 0.25, 1, \frac{f_{ub}}{f_u}$$

$$\text{or, } \frac{40}{3 \times 22}, \frac{60}{3 \times 22} = 0.25, 1, \frac{400}{410}$$

$$\text{or, } 0.606, 0.659, 1, 0.975$$

$$\text{So, } (V_{dpb}) = \frac{2.5 \times 0.606 \times 16 \times 12 \times 400}{1.25}$$

$$= 116.352 \text{ KN}$$

$$\text{c) Design tensile strength (} T_{db} \text{)} = \frac{T_{nb}}{\gamma_{mb}}$$

$$T_{nb} = 0.9 f_{ub} A_{nb} \leq \frac{f_{yb} A_{sb} \gamma_{mb}}{\gamma_{mo}}$$

$$= 0.9 \times 400 \times 0.78 \times 71 \times 20^2 \leq \frac{240 \times 71 \times 20^2}{4} \times \frac{1.25}{1.1}$$

$$= 88.216 \leq 85.679$$

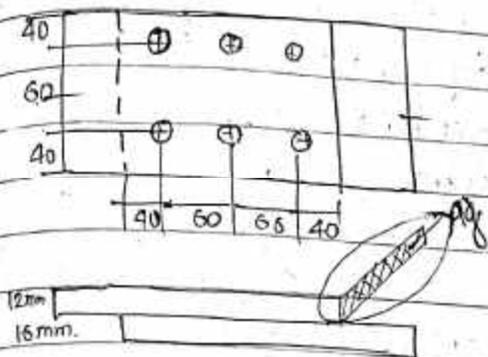
$$\text{So, } T_{db} = \frac{85.679}{1.25} = 68.544 \text{ KN}$$

Hence, Bolt value = 68.544 KN

Note: for snug tight bolt use butt joints because,

1. for Double cover butt joints \rightarrow Total shear force to be transmitted by member is split into 2 parts, and force acts on each half.
 But for lap, there is only one shear plane, on which force acts and shear-carrying of a bolt in double cover butt joint is double that of a bolt in lap joints.

Calculate bolt value, strength of connection and efficiency of connection for following cases:
 for question (a).



Given, M20 bolt Prcl. 4.6

$$d = 20 \text{ mm}$$

$$d_o = 22 \text{ mm}$$

$$e = 40 \text{ mm}$$

$$p = 60 \text{ mm}$$

from above solⁿ: Bolt value = 45.27 kN.

(i) Shear capacity of bolt $(V_{dsb}) = 45.27 \text{ kN}$

(ii) Bearing capacity $\dots (V_{dpb}) = 116.352 \text{ kN}$

(iii) Yielding capacity of plate: Page 32. 6.2

$$T_{dg} = \frac{f_y A_g}{\gamma_{m0}} \quad f_y = 250$$

A_g - gross area of plate having least thickness.

If not stated Fe 410, $t = 12 \text{ mm} < 20$

$$\therefore f_u = 410 \text{ MPa}$$

$$\therefore f_y = 250 \text{ MPa}$$

$$\therefore T_{dg} = \frac{250 \times (140 \times 12)}{1.10}$$

$$= 381.82 \text{ kN}$$

(iv) Rupture strength due to rupture of critical section

$$T_{dn} = \frac{0.9 A_n f_u}{\gamma_{m2}}$$

γ_{m2} = partial safety factor for failure at ultimate stress

f_u = ultimate stress

A_n = net effective area of member

Note: Force mechanism: - Connection
 Bearing type: bolt bears against hole to transfer load - slip type
 friction " " "

$$A_n = \left[b - nd_h + \frac{\sum P_{s_i}^2}{4g_i} \right] \times t$$

net area, tear area



n - no. of bolt in tear zone
 d_h = diameter of bolt hole
 t = thickness of plate
 b = width

$$\therefore A_n = (140 - 2 \times 22) \times 12$$

$$\therefore T_{dn} = \frac{0.9 \times (140 - 44) \times 12 \times 410}{1.25}$$

$$= 340.070 \text{ kN}$$

④ Total Shearing capacity of connection = no. of bolt \times Shear strength of single bolt

$$= 6 \times 45.27$$

$$= 271.62 \text{ kN}$$

⑤ total Bearing capacity of connection = 6×116.352

$$= 698.112 \text{ kN}$$

Hence, strength of connection = least of ③, ④, ⑤, & ⑥

$$= 271.62 \text{ kN}$$

For, efficiency of connection:

$$\text{strength of plate before drilling} = \frac{0.9 A_m f_u}{\gamma_{ms}}$$

$$= \frac{0.9 \times 140 \times 12 \times 410}{1.25}$$

$$= 495.936 \text{ kN}$$

$$\% \text{ efficiency} = \frac{\text{strength of connection after drill}}{\text{strength of plate before drill}} = \frac{271.62}{495.936} \times 100\%$$

$$= 54.769\%$$

connection Design:

(a) single cover butt joints:

Bolt shear strength of bolt (V_{dsb}) = 28.97 kN

Bearing " " " (V_{dpb}) = 56.889 kN

$$d = 16 \text{ mm}$$

$$d_o = 18 \text{ mm}$$

$$e = 30 \text{ mm}$$

$$p = 50 \text{ mm}$$

$$f_{ub} = 480 \text{ N/mm}^2$$

$$f_y = 240 \text{ N/mm}^2$$

$$\text{Bolt value} = 28.97 \text{ kN}$$

Now, yielding capacity of plate:

$$T_{dg} = \frac{f_y \cdot A_g}{\gamma_{mo}}$$

A_g = gross area of least thickness

$f_e = 410$, $f_u = 410$, $f_y = 250 \text{ MPa}$ since $t < 20 \text{ mm}$

$$T_{dg} = \frac{250 \times (160 \times 8)}{1.10}$$

$$= 290.90 \text{ kN}$$

Rupture strength due to critical section

$$T_{dn} = \frac{0.9 A_n f_u}{\gamma_{m1}}$$

$$A_n = [b - n d_o] \times t$$

$$= [160 - 3 \times 18] \times 8$$

$$= 848$$

$$\text{So, } T_{dn} = \frac{0.9 \times 848 \times 410}{1.25}$$

$$= 250.33 \text{ kN}$$

→ no of bolt given to ¹ plate

$$\begin{aligned} \text{Total shearing capacity} &= 6 \times 28.97 \\ &= 173.82 \text{ kN} \end{aligned}$$

$$\begin{aligned} \text{Total bearing capacity} &= 6 \times 56.889 \text{ kN} \\ &= 341.334 \text{ kN} \end{aligned}$$

∴ strength of connection = 173.82 kN

for efficiency of connection,

$$\begin{aligned} \text{Strength of plate before drilling} &= \frac{0.9 A_n f_y}{\gamma_{m1}} \\ &= \frac{0.9 \times 160 \times 8 \times 410}{1.25} \\ &= 377.856 \text{ kN} \end{aligned}$$

$$\begin{aligned} \% \text{ efficiency} &= \frac{173.82}{377.856} \\ &= 46\% \end{aligned}$$

(c) calculate η :

$$V_{dsb} = 103.314 \text{ kN}$$

$$V_{dpb} = 116.352 \text{ kN}$$

$$\text{Bolt value} = 68.544 \text{ kN}$$

$$d = 20 \text{ mm}$$

$$d_o = 22 \text{ mm}$$

for Fe 410

$$f_u = 410 \text{ MPa}$$

$$f_y = 250 \text{ MPa} \quad t < 20 \text{ mm}$$

Then,

$$\begin{aligned} \text{yield capacity } (T_{dg}) &= \frac{f_y A_g}{\gamma_{m0}} \\ &= \frac{250 \times 200 \times 12}{1.10} \\ &= 545.45 \text{ kN} \end{aligned}$$

design.

Tearing Rupture strength

$$\begin{aligned} T_{dn} &= \frac{0.9 A_n f_u}{\gamma_{m1}} \\ &= \frac{0.9 \times (200 - 3 \times 22) \times 12 \times 410}{1.25} \\ &= 474.68 \text{ kN} \end{aligned}$$

$$\begin{aligned} \text{Total shearing capacity} &= 6 \times 103.314 \\ &= 619.884 \text{ kN} \end{aligned}$$

$$\begin{aligned} \text{Total Bearing} &= 6 \times 116.352 \\ &= 698.112 \text{ kN} \end{aligned}$$

$$\therefore \text{strength of connection} = \underline{474.68}$$

$$\begin{aligned} \text{Strength before drilling of plate} &= 0.9 A_n f_u \\ &\quad \gamma_{m2} \\ &= 708480 \end{aligned}$$

$$\eta = \frac{67}{100} = 67\%$$

Design bolted connection

To connect two members (200 x 12) mm, carrying an axial load of 200 kN using M20 bolt of Pr. Cl. 4.6 in lap connection.

Soln:-

$d = 20 \text{ mm}$

$d_o = 22 \text{ mm}$

$f_{ub} = 400 \text{ MPa}$

$f_u = 410 \text{ MPa}$

$f_y = 240 \text{ MPa}$

Ultimate/ design/ factor load
no modification.



axial load (P) = 200 kN. (working load)/service load:

∴ Design load = Partial safety factor × working load

$= 1.5 \times 200$

$= 300 \text{ kN}$

$n_s = 0$

$n_m = 1$

0

① shear strength strength of bolt (V_{dsb}) = $\frac{f_{ub} (n_p A_{nb} + n_s A_{sb})}{\sqrt{3} \gamma_m}$

$= \frac{400 \times (1 \times 0.78 \times \pi \times \frac{20^2}{4})}{\sqrt{3} \times 1.25}$

$= 45.27 \text{ kN}$

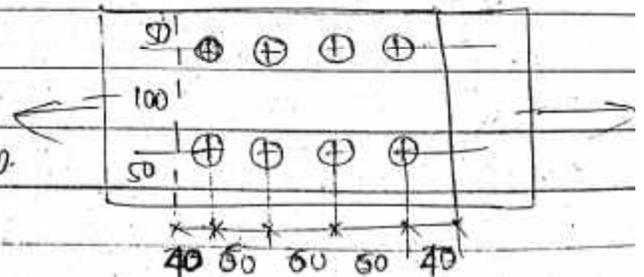
No. of Bolts = $\frac{\text{Design load}}{\text{Shear strength}}$

$= \frac{300}{45.27}$

$= 6.69$ near even no.

$= 8$ bolts

$= 8$ bolts



Now,

pitch (p) = $2.5d = 2.5 \times 20 \text{ mm}$

$= 50 \text{ mm}$

End distance (e) = $1.5 \times d_o$

$= 1.5 \times 22$

$= 33 \text{ mm}$

Bearing capacity :

$\frac{e}{3d_o}, \frac{p}{3d_o}, 0.25, 1, \frac{f_{ub}}{f_u}$
 $\frac{40}{3 \times 22}, \frac{60}{3 \times 22}, 0.25, 1, \frac{400}{410}$

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हुन पद

0.606, 0.95, 1, 0.97

$$\therefore k_b = 0.60$$

$$\therefore V_{pb} = \frac{2.5 \times 0.606 \times 20 \times 12 \times 400}{1.25}$$

$$= 116.352 \text{ kN}$$

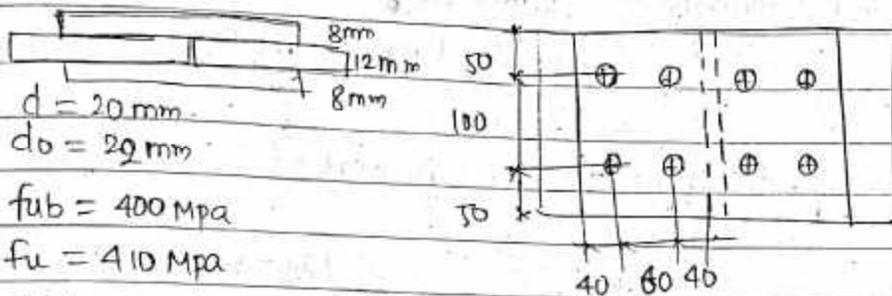
$$\text{Total bearing capacity} = 8 \times 116.352$$

$$= 930.816 \text{ kN} > 300 \text{ kN}$$

same eqn with coverplate of thickness 8mm in

① single cover butt joint

② Double " " "



$$d = 20 \text{ mm}$$

$$d_o = 29 \text{ mm}$$

$$f_{ub} = 400 \text{ MPa}$$

$$f_u = 410 \text{ MPa}$$

$$\text{axial load} = 200 \text{ kN}$$

$$\text{design load} = 1.5 \times 200$$

$$= 300 \text{ kN}$$

$$n_n = 1$$

$$n_s = 1$$

$$\text{shear strength of bolt} = (V_{dsb}) = \frac{f_{ub}}{\sqrt{3} \times 6m} (n_n A_{nb} + n_s A_{sb})$$

$$= \frac{400}{\sqrt{3} \times 1.25} \left(1 \times 0.787 \frac{d^2}{4} + 1 \times \frac{\pi d^2}{4} \right)$$

$$= \frac{400}{\sqrt{3} \times 1.25} \times 1.78 \times \frac{\pi \times 20^2}{4}$$

$$\therefore \text{No of bolts} = \frac{300}{103.314}$$

$$= 2.90$$

$$= 3$$

$$= 4$$

$$\text{pitch} = 2.5d = 50 \text{ mm}$$

$$\text{end distance} = 1.5d_o = 33 \text{ mm}$$

for Bearing capacity k_b

$$\frac{p}{3d_o}, \frac{p-0.25}{3d_o}, 1, \frac{f_u}{f_{ub}}$$

$$= 0.606, 0.650, 1, 0.97$$

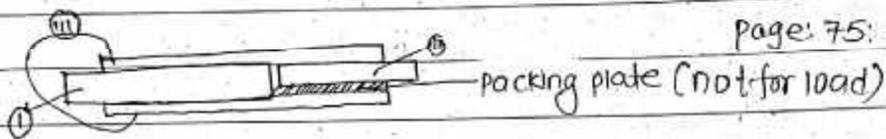
$$\therefore V_{dpb} = \frac{25 \times 0.606 \times 12 \times 20 \times 450}{1.25}$$

$$= 116.352 \text{ kN}$$

$$\text{Total bearing capacity} = 4 \times 116.352 \times 4$$

$$= 465.408 \text{ kN} > 300 \text{ kN}$$

for Buttjoints having different thickness of plate



Page: 75: 10.3.3.3

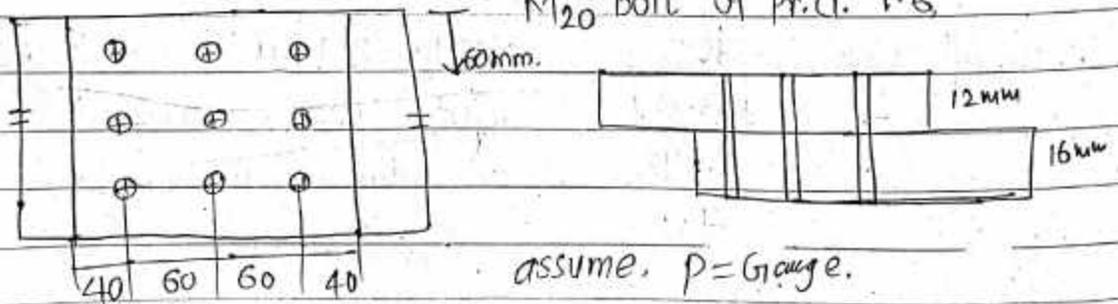
$$B_{pk} = 1 - 0.0125 t_{pk}$$

t_{pk} = thickness of packing plate.

$$\text{design. shear strength} = B_{pk} \times \frac{f_{ub}}{\sqrt{3} \gamma_m} (n_A A_{sb} + n_B A_{sb})$$

calculate strength of connection, efficiency of connection ^{per pitch}

M20 bolt of pr. cl. 4.6



assume, $p = \text{Gauge}$.

For, Tearing strength

$$T_{dg} = \frac{0.9 A_{nt} f_u}{\gamma_{m1}}$$

$$A_{nt} = (\text{Pitch shift} - ndh) \times t$$

n - for shifted pitch how many bolt lies.

Given:-

M20 bolt

$$d = 20 \text{ mm}$$

$$d_o = d_h = 22 \text{ mm}$$

for Pr. CI: 4.6

$$f_u = 410 \text{ MPa}$$

$$f_{yb} = 240 \text{ MPa}$$

$$f_{ub} = 450 \text{ "}$$

(a) for design shear strength per pitch length

$$V_{dsb} = \frac{1 \times f_{ub} \times (A_{nb} n_b + A_{sb} n_s)}{\sqrt{3} \gamma_{mb}}$$

$$= \frac{400 \times 1 \times 0.78 \times 77 d^2}{\sqrt{3} \times 1.25 \times 4}$$

$$= 45.264 \text{ kN}$$

(b) for design bearing capacity per pitch length.

② net strength of plate per pitch: (Tearing)

$$T_{dg} = \frac{0.9 A_{nt} f_u}{\gamma_{m1}}$$

$$= \frac{0.9 \times (60 - 22) \times 12 \times 410}{1.25}$$

$$= 134.611 \text{ kN}$$

$$V_{dpb} = \frac{1 \times 2.5 k_b d t (f_u \text{ or } f_{ub})}{1.25}$$

$$k_b = \frac{e}{3d_o} = 0.606$$

$$= \frac{1 \times 2.5 \times 0.606 \times 20 \times 12 \times 400}{1.25}$$

$$= 116.352 \text{ kN}$$

③ % strength of restriction per pitch = 45.264 kN

$$\text{Strength of plate before drilling} = \frac{0.9 p t \times f_u}{\gamma_{m1}}$$

$$= \frac{0.9 \times 60 \times 12 \times 410}{1.25}$$

$$= 212.544 \text{ kN}$$

$$\# \text{ efficiency } (\eta) = \frac{45.264}{212.544} = 21.29 \%$$

Design bolted connection to connect two member $250 \times 12 \text{ mm}^2$ carrying axial load of 200 kN, M20 bolt, Pr. Cl 4.6 in lap

(i) single cover butt joints:

Given

M20 bolt

$d = 20 \text{ mm}$

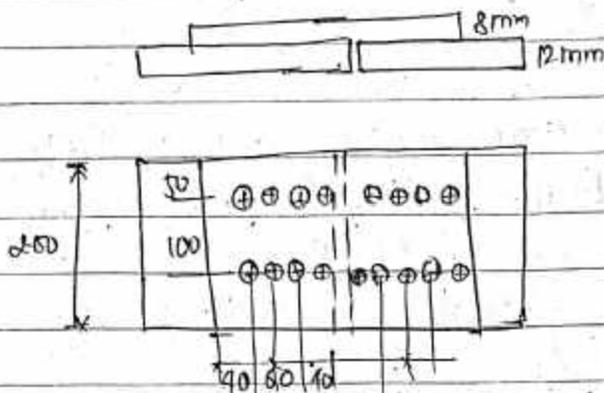
$d_o = 22 \text{ mm}$

for Pr. Cl: 4.6

$f_{ub} = 450 \text{ MPa}$

$f_{yb} = 240 \text{ "}$

$f_u = 410 \text{ "}$



(i) Design load = P.S.F x Working load

$$= 1.5 \times 200$$

$$= 300 \text{ kN}$$

(ii) Shear strength of bolt (V_{dsb}) = $\frac{f_{ub}}{\sqrt{3}} \times (n A_{nb} + n_s A_{sb})$

$$= \frac{1 \times 450 \times 0.785 \times 20^2}{\sqrt{3} \times 1.25} \times \frac{1}{4}$$

$$= 45.27 \text{ kN}$$

(iii) No. of bolts = $\frac{300}{45.27} = 6.62$ take, 8 bolts.

(iv) pitch = $2.5d = 2.5 \times 20 = 50 \text{ mm}$ take, $P = 60 \text{ mm}$

end. d = $1.5d_o = 1.5 \times 22 = 33 \text{ mm}$ $e = 40 \text{ mm}$

(v) Design bearing capacity = $V_{d, pb} = \frac{2.5 k_b d t f_{ub}}{1.25} = \frac{2.5 \times 0.606 \times 20 \times 8 \times 450}{1.25}$

$$k_b = \frac{e}{3d_o} \text{ or } \frac{f}{3d_o} - 0.25$$

$$0.606 \quad 0.65$$

$$= 77.568 \text{ kN}$$

$$\therefore \text{Total bearing capacity} = 4 \times 77.568 \times 2 \\ = 2 \times 310.272 \text{ kN} > 350 \text{ kN}$$

Hence,

provide 8 bolts of M20, Pr. Cl. 4.6 for single cover of $t = 8 \text{ mm}$
butt joints.

3)

10

Q

← find

section

11

High strength friction grip bolt

10.4, Page 176

Nominal shearing friction capacity of bolt (V_{nst}) = $\mu_f n_e K_h f_o$

Design

$$(V_{dst}) = \frac{V_{nst}}{\gamma_{mf}}$$

μ_f = coefficient of friction (0.55)

n_e = no. of friction plane

(parallel to load)

K_h = 1.0 for fasteners holes (clearance), 0.70 long slotted hole

γ = 0.85 for " in oversized and short slotted holes

F_o = min. bolt tension = $A_{nb} f_o$

A_{nb} = net area of bolt at thread

f_o = proof stress (0.70 f_{ub})

γ_{mf} = 1.10 (if slip resistance is designed for service load)

= 1.25 (" " " " " ultimate ")

2070/Bhadra:

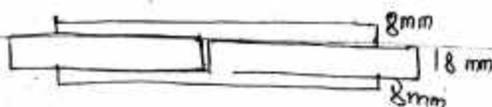
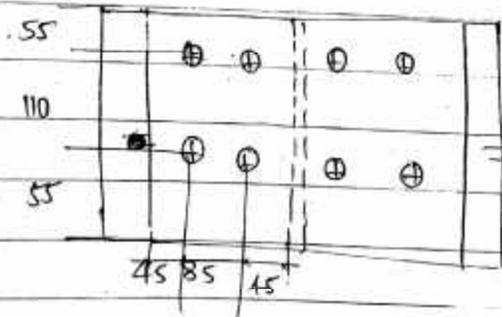
Two plates 18 mm thick are spliced (connect) by a cover plate of 8 mm using M18 bolt of pr. cl. 10.9, calculate ultimate load carrying capacity (strength) of connection

(i) if slip is permitted at ultimate load.

(ii) if slip is not " " " " " [friction type]

(iii) if slip is not " at working " [slip is permitted at ultimate load]

bearing,



So, ① friction type under working load.

$$\text{① Design shear friction capacity of bolt } (V_{dsf}) = \frac{\mu_f n_e K_n f_o}{\gamma_{mf}}$$

$$= \frac{0.55 \times 2 \times 1.0 \times 0.78 \times \pi \times \frac{18^2}{4} \times 0.70 \times 1000}{1.10}$$

$$= 138.94 \text{ kN.}$$

② friction type Ultimate load.

$$\text{② Design shear friction capacity of bolt } (V_{dsf}) = \frac{0.55 \times 2 \times 1.0 \times 0.78 \times \pi \times \frac{18^2}{4} \times 0.70 \times 1000}{1.25}$$

$$= 122.27 \text{ kN}$$

$$\text{③ design shear strength } (V_{dsb}) = \frac{1000 \times (1.78 \times \pi \times \frac{18^2}{4})}{\sqrt{3} \times 1.25}$$

$$= 209.20 \text{ kN}$$

④ design bearing strength $(V_{dpb}) \Rightarrow k_b$ can be

$$\frac{e}{3d_0}, \frac{P}{3d_0} - 0.25, 1, \frac{f_{ub}}{f_{ub}}$$

$$\text{or } \frac{45}{3 \times 20}, \frac{85}{3 \times 20} - 0.25, 1, \frac{410}{1000} \frac{1000}{410}$$

$$0.75, 1.16, 1, 0.410 \quad (2.44)$$

$$\text{So, } (V_{dpb}) = \frac{2.5 \times 0.75 \times 18 \times 16 \times 410}{1.25}$$

$$= 177.120 \text{ kN}$$

$$\text{⑤ Yielding strength } (T_{dg}) = \frac{f_y A_g}{\gamma_{mo}} = \frac{250 \times 220 \times 16 \times 2}{1.10}$$

$$= 800 \text{ kN} \quad \text{--- ①}$$

$$\text{⑥ Tearing strength at critical section } (T_{dn}) = \frac{0.9 A_{nt} f_u}{\gamma_{m1}} = \frac{0.9 \times (220 - 2 \times 20) \times 16 \times 410}{1.25}$$

$$= 850.176 \text{ kN} \quad \text{--- ②}$$

$$\text{Total shearing friction strength at working load} = 4 \times 138.94 = 555.76 \text{ KN} \quad \text{--- (iii)}$$

$$\text{at ultimate load} = 4 \times 12.267 = 489.068 \text{ KN} \quad \text{--- (iv)}$$

$$\text{Total shear capacity at bearing type bolt} = 836.29 \text{ KN} \quad \text{--- (v)}$$

$$\text{Total bearing capacity} = 4 \times 177.12 = 708.48 \text{ KN} \quad \text{--- (vi)}$$

(i) When slip is permitted at ultimate load:
 (Bearing type में काम जई, friction में काम जई ना।)

$$\text{ultimate load capacity} = \min \text{ of } T_{dg}, T_{dn}, \text{ (v) \& (vi)}$$

$$= 708.48 \text{ KN}$$

(ii) When slip is not permitted at ultimate load:

ie, friction type में काम जई।

$$\text{ultimate load capacity} = \min \text{ of } T_{dg}, T_{dn}, \text{ (iv) \& (vi)}$$

$$= 489.068 \text{ KN}$$

(iii) When slip is ^{not} permitted at working load.

(Bearing type में काम जई)

$$\therefore \text{working load capacity} = \min \text{ of } T_{dg}, T_{dn}, \text{ (iii) \& (v)}$$

$$= 555.76 \text{ KN}$$

Design bolt connection using M16 bolt of pr. ci. 8.8 to connect two plates 200x16 mm carrying a load of 300 KN at working condition.

If, (i) Slip is not permitted at working load

(ii) Slip is " " " " ultimate load.

design double cover butt joints of 10mm thick cover plate.

Now;

Given:

M16 bolt

$d = 16 \text{ mm}$

$d_o = 18 \text{ mm}$

$f_{ub} = 800 \text{ MPa}$

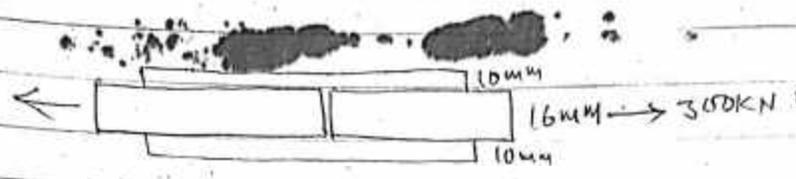
$f_{yb} = 400 \text{ MPa}$

Working load = 300 kN

Ultimate load = $300 \times 1.5 = 450 \text{ kN}$

Plate dimension = 200×16

Then,



Let, Fe 410 grade of steel

So, $f_u = 410 \text{ MPa}$

(i) For working load

Design shear friction

$$\text{Capacity} = (V_{dsf}) = \frac{0.5 \times 2 \times 1.0 \times f_u}{\gamma_{mf}}$$

$$f_u = A_n \cdot f_u$$

$$= 0.78 \times \frac{\pi d^2}{4} \times 0.7 \times f_{ub}$$

$$= 0.78 \times 87823.85$$

$$(V_{dsf}) = 87823.84 \text{ kN}$$

$$= 87.823$$

So, no. of bolts at working load

$$= \frac{300}{87.823}$$

$$= 3.41$$

$$= 3.41$$

$$= 4 \text{ bolts}$$

(ii) for ultimate load, $\gamma_{mf} = 1.25$

Design shear friction capacity

$$(V_{dsf}) = \frac{\mu_f \cdot K_n \cdot n \cdot f_{ub}}{\gamma_{mf}}$$

$$= \frac{0.55 \times 2 \times 2 \times 87823.85}{1.25}$$

$$= 77.284 \text{ kN}$$

So, no. of bolts at ultimate load

$$= \frac{300 \times 1.5}{77.284}$$

$$= 5.82$$

$$= 5.82$$

$$= 6 \text{ bolts}$$

1)

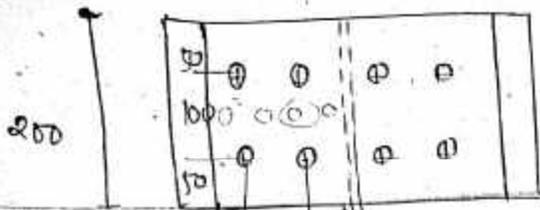
2)

3)

4)

5)

6)



at working condition

$$n_n = 1, n_s = 1$$

$$\begin{aligned} \textcircled{III} \text{ design shear strength } (V_{dsb}) &= \frac{f_{ub}}{\sqrt{3} \times \gamma_{mb}} (n_n A_{nb} + n_s A_{sb}) \\ &= \frac{800}{\sqrt{3} \times 1.25} \times 1.78 \times \pi \times \frac{16^2}{4} \\ &= \frac{1145248.75}{8.66025} \\ &= 132.241 \text{ KN} \end{aligned}$$

$$\textcircled{IV} \text{ Design bearing strength } (V_{dpb}) = \frac{2.5 K_b d t (f_u / f_{ub})}{1.25}$$

$$\text{for } K_b: \frac{p}{3d_o}, \frac{p}{3d_o} = 0.25, 1; \frac{f_{ub}}{f_u}$$

$$p \leq 2.5d = 2.5 \times 16 = 40 \text{ mm} \quad \therefore 0.740, 0.86, 1, 1.95$$

$$e \leq 1.7d_o = 1.7 \times 18 = 30.6 \text{ mm}$$

$$\text{take } p = 40 \text{ mm}$$

$$e = 40 \text{ mm}$$

$$\text{so } K_b = 0.740$$

$$\begin{aligned} \text{and, } (V_{dpb}) &= \frac{2.5 \times 0.74 \times 16 \times 16 \times 410}{1.25} \\ &= 155.340 \text{ KN} \end{aligned}$$

$$\textcircled{V} \text{ Yielding strength } (T_{dg}) = \frac{f_y A_g}{\gamma_{mo}} = \frac{450 \times 200 \times 16}{1.10} = 727.272 \text{ KN} \quad \textcircled{I}$$

(t = 20 mm)

$$\textcircled{VI} \text{ Tearing strength } (T_{dn}) = \frac{0.9 A_n f_u}{\gamma_{mf}} = \frac{0.9 \times (200 - 2 \times 18) \times 16 \times 410}{1.25} \quad \textcircled{II}$$

$$= 774.604 \text{ KN}$$

(Friction)

So, total shearing friction at ultimate load = $77.284 \times 4 = 309.137$ (iii)
total " " working load = $87.823 \times 4 = 351.292$ kN (iv)

(Bearing)

Total shearing capacity for bearing type bolt = $132 \times 241 \times 4 = 528.964$ (v)
Total bearing capacity for bearing " " = $155.340 \times 4 = 621.36$ kN (vi)

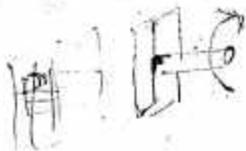
(i) When slip is not permitted at working load: (bearing type)

so,

Ultimate load capacity = min of (i), (ii), (v) and (vi)
= 351.292 kN

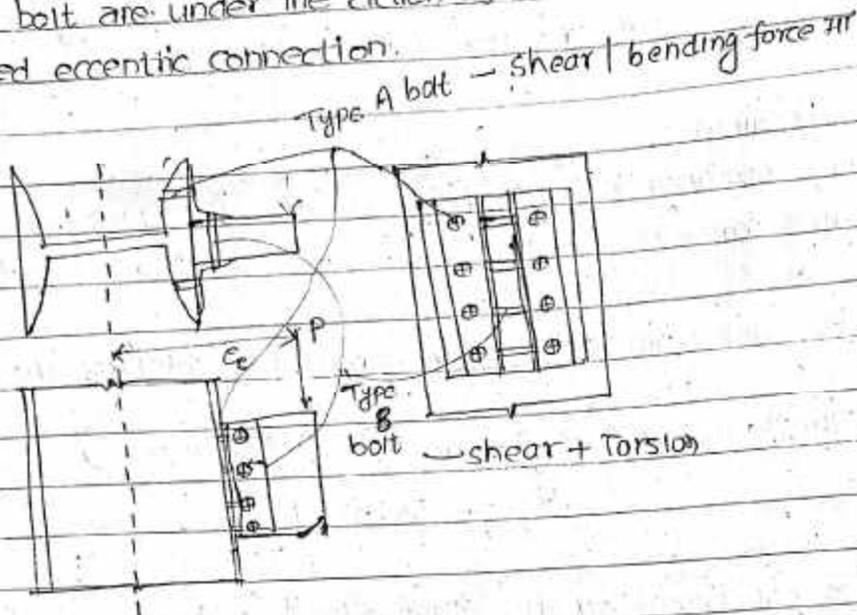
(ii) When slip is not permitted at ultimate load. (friction type)

Ultimate load capacity = min. of (i), (ii), (iii) and (iv)
= 309.196 kN



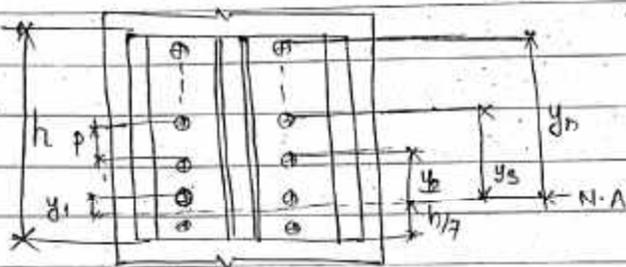
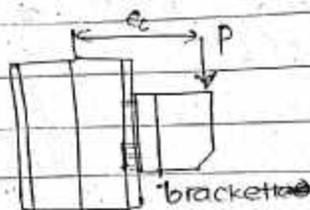
Eccentric connection:

If the bolt are under the action of moment, as well as shear, such connection is called eccentric connection.



Type A bolt is under bending moment & shear whereas type B bolt is under shear & torsion.

∴ Design of type - A bolt



We assume that neutral axis lies at $h/7$ from bottom bracket plate,

We also know that,

$$M = P \times e_c$$

$$M = [T_1 y_1 + T_2 y_2 + \dots + T_n y_n] \quad \text{--- (1)}$$

also from bending stress relation, we have,

$$T \propto y$$

$$\text{Hence, } \frac{T_1}{y_1} = \frac{T_2}{y_2} = \frac{T_3}{y_3} = \dots = \frac{T_n}{y_n}$$

$$\text{Or, } T_1 = \frac{T_n y_1}{y_n}, T_2 = \frac{T_n y_2}{y_n}, T_3 = \frac{T_n y_3}{y_n} \dots T_n = \frac{T_n y_n}{y_n}$$

Then,

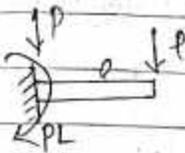
$$P \times e_c = 2 \left[\frac{T_n \cdot y_1^2}{y_n} + \frac{T_n \cdot y_2^2}{y_n} + \frac{T_n \cdot y_3^2}{y_n} + \dots + \frac{T_n \cdot y_n^2}{y_n} \right]$$

$$= 2 \frac{T_n}{y_n} [y_1^2 + y_2^2 + y_3^2 + \dots + y_n^2]$$

$$P \cdot e_c = 2 \frac{T_n}{y_n} \sum y_i^2$$

$$\text{or } T_n = \frac{P \times e_c \cdot y_n}{2 \sum y_i^2}$$

$$\therefore T_{\max} = \frac{P \times e_c \times y_{\max}}{2 \sum y_i^2}$$



Shear force on each bolt (V_{\max}) = $\frac{P}{N}$
 N - no. of total bolt

Then for safe design, following combined relation should be satisfied,

$$\left(\frac{T_{\max}}{T_{db}} \right)^2 + \left(\frac{V_{\max}}{V_{dsb}} \right)^2 \leq 1.0 \quad \text{Clause (10.3.6)}$$

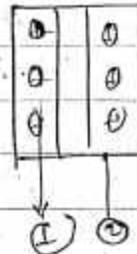
Note: No. of bolt required is given by $N = \sqrt{\frac{6 P \times e_c}{m \times p \times T_{db}}}$

P - applied load

p - pitch

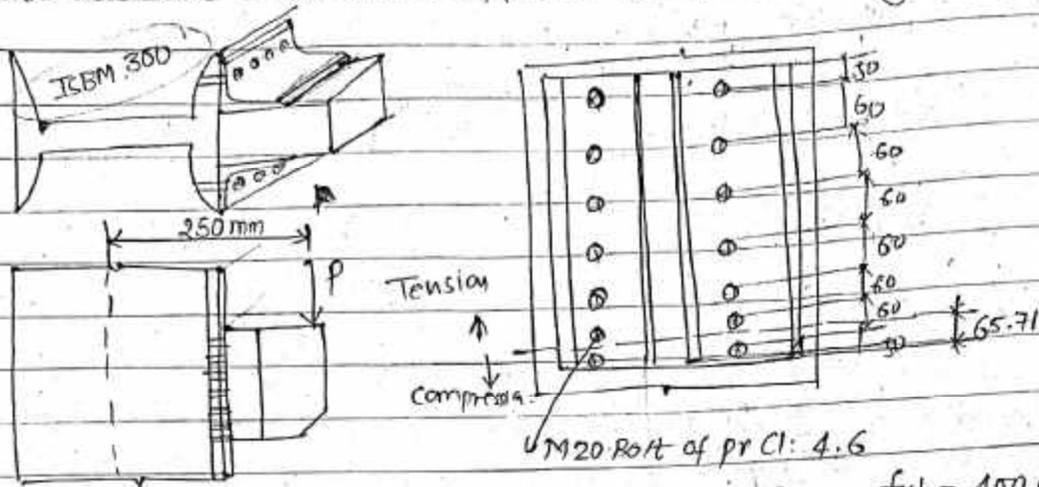
T_{db} - design tensile capacity

m = no. of line of bolt



m = 2

Calculate the load that can be applied on the following connection,



$$f_{ub} = 400 \text{ N/mm}^2$$

$$f_{yb} = 240 \text{ N/mm}^2$$

$$\begin{aligned} \text{Total height of bracket } (h) &= 50 \times 2 + 60 \times 6 \\ &= 360 + 100 \\ &= 460 \text{ mm} \end{aligned}$$

$$\text{Position of N.A.} = \frac{460}{7} = 65.71 \text{ mm}$$

$$\begin{aligned} \sum y_i^2 &= [44.29^2 + 104.29^2 + 164.29^2 + 224.29^2 + 284.29^2 + 344.29^2] \\ &= 289491.6246 \end{aligned}$$

$$\therefore y_{\max} = 344.29 \text{ mm}$$

$$\begin{aligned} T_{\max} &= \frac{P \times e_c \times y_{\max}}{2 \sum y_i^2} \\ &= \frac{P \times 250 \times 344.29}{2 \times 289491.6246} \end{aligned}$$

$$\text{(i) } T_{\max} = 0.1486P \quad \text{--- (i)}$$

$$\text{(ii) } V_{\max} = \frac{P}{N} = \frac{P}{14} = 0.071P \quad \text{--- (ii)}$$

$$\begin{aligned} \text{(iii) } V_{dcb} &= \frac{f_{ub}}{\sqrt{3} \times 1.25} \times \left(n_n A_{nb} + n_s A_{sb} \right) \\ &= \frac{400}{\sqrt{3} \times 1.25} \times 0.78 \times 71 \times \frac{20^2}{4} = 45.272 \text{ MPa} \end{aligned}$$

$$\textcircled{10} T_{db} = \frac{0.9 A_n f_u}{\gamma_{m1}} = \frac{0.9 \times A_n \times 410}{1.25}$$

$$A_n = (b - nd) \times t$$

Tensile strength T_{db}

$$0.9 f_{ub} A_{nb} \leq f_{yb} A_{sb} \frac{\gamma_{mb}}{\gamma_{m0}}$$

$$T_{dg} = \frac{f_y \cdot A_g}{\gamma_{m0}} = \frac{250 \times 460}{1.10} = 68.54 \text{ kN}$$

$$= \frac{0.9 \times 400 \times 0.787 \times 10^2}{1.25} = \frac{240 \times 7 \times 10^2}{4} \times \frac{1.25}{1.10}$$

$$= 88.215 \leq 85.679 \text{ kN}$$

Then,

$$\text{So, } T_{db} = \frac{85.679}{1.25}$$

$$= 68.543 \text{ kN}$$

we have,

$$\left(\frac{0.1486P}{68.54} \right)^2 + \left(\frac{0.071P}{45.272} \right)^2 \leq 100$$

Solving we get

$$P = 373.714 \text{ kN}$$

$$\text{So, Service load} = \frac{\text{design load}}{\text{FOS}}$$

$$= \frac{373.714}{1.5}$$

$$= 249.142 \text{ kN}$$

⊕ Design eccentric connection of an axial load of 150 kN at an eccentricity of 300 mm from center of column, using M16 bolt of pr. cl. 4.6

Soln:-

NAD

Given: $P = 150 \text{ kN}$ (service load)

$$\text{Design load } P_d = 150 \times 1.5 = 225 \text{ kN}$$

$$\text{no. of bolt } N = \sqrt{\frac{6P \times e_c}{m_p \times T_{db}}}$$

for design shear strength of bolt

$$V_{dsb} = \frac{f_{ub} \times (0.787 \times 16^2)}{\sqrt{3} \times 1.25}$$

$$= 28.917 \text{ kN}$$

T_{db} can be calculated as

$$0.9 \times f_{ub} \times A_{nb} < f_{yb} \times A_{sb} \times \frac{\gamma_{mb}}{\gamma_{mi}}$$

$$V_{max} = \frac{P}{N} = \frac{225}{10} = 22.5 \text{ kN}$$

(V_{sb})

$$0.9 \times 400 \times 0.787 \times \frac{16^2}{4} \leq 240 \times 77 \times \frac{16^2}{4} \times \frac{1.25}{1.10}$$

$$56.46 \leq 548367$$

$$\text{So, } T_{db} = \frac{54.83}{1.25} = 43.86 \text{ kN}$$

$$\text{pitch } (p) \geq 2.5d$$

$$\geq 2.5 \times 16$$

$$\geq 40 \text{ mm}$$

take 50 mm

$$\text{end distance } \geq 1.78d_0 = 1.5 \times 18 = 27$$

$$\geq 30 \text{ mm}$$

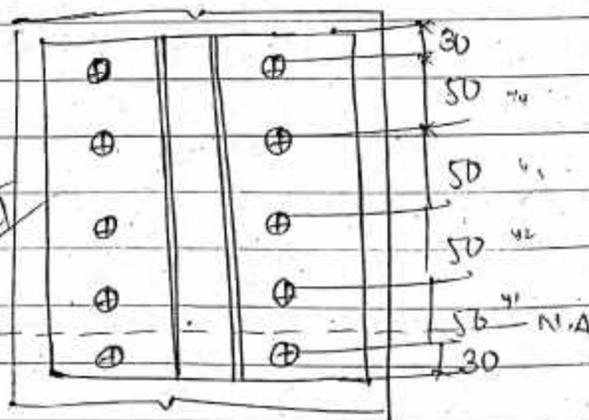
So,

$$n = \sqrt{\frac{6 \times 225 \times 300}{2 \times 50 \times 43.86}}$$

$$= 9.6$$

$$\approx 10$$

10 bolts



$$\text{Total height} = 260 \text{ mm}$$

$$\text{N.A} = \frac{260}{7} = 37.142$$

150
450
+40
540
7.17
11286

Then.

$$\sum y_i^2 = 42.858^2 + 92.858^2 + 142.858^2 + 192.858^2 + 222.858^2$$

$$= 11725.435 - 222.858^2$$

$$= 68059.74$$

$$y_{max} = 222.858 - 192.858$$

$$T_{max} = \frac{225 \times 300 \times 192.858}{2 \times 11725.435}$$

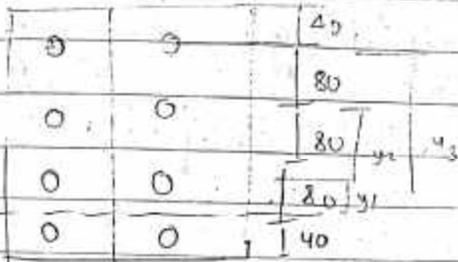
$$= 63.889 - 75.63 \text{ kN}$$

$$v_{max} = \frac{P}{N} = \frac{225}{10} = 22.5$$

$$\left(\frac{63.889}{43.86}\right)^2 + \left(\frac{22.5}{28.917}\right)^2 > 1 \text{ no ok}$$

$P = 80 \text{ mm}$
 $e = 40 \text{ mm}$

$n = 8$



$$h = 320$$

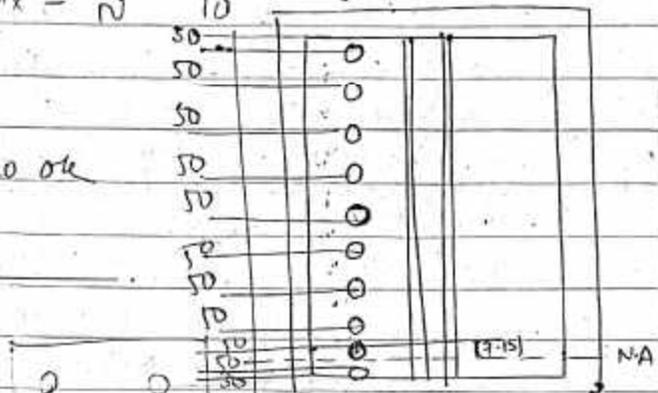
$$N.A = 45.914$$

$$\sum y_i^2 = 74.286^2 + 154.286^2 + 234.286^2 = 84212.50$$

$$y_{max} = 234.286$$

$$\text{So, } T_{max} = 33$$

$$k_b = \frac{e}{3d_o} = 0.55$$



$P = 50 \text{ mm}$
 $e = 30 \text{ mm}$

$$h = 510$$

$$N.A = h/2 = 255$$

$$\therefore y_{max} = 407.15 \text{ mm}$$

$$\sum y_i^2 = 602326.225$$

$$\therefore T_{max} = 22.81 \text{ kN}$$

$$\text{So, } \left(\frac{22.81}{43.86}\right)^2 + \left(\frac{22.5}{28.917}\right)^2 = 0.876 < 1$$

OK!

for bearing:

$$V_{dpb} = 2.5 \times k_b \times d \times t_{ub}$$

$$= 1.25$$

Eccentric connection (Type-B)

(parallel)

Type B bolt under shear & Torsion

Then:

$$M = P \times e$$

It is resisted by shear developed on each bolt at r to radius vectors.

Then,

$$M = r_1 \times V_{T1} + r_2 \times V_{T2} + r_3 \times V_{T3} + \dots + r_n \times V_{Tn}$$

also, $V_T \propto r$

$$\text{So, } \frac{V_{T1}}{r_1} = \frac{V_{T2}}{r_2} = \dots = \frac{V_{Tn}}{r_n}$$

$$\text{So, } V_{T1} = \frac{V_{Tn} r_1}{r_n} \quad V_{T2} = \frac{V_{Tn} r_2}{r_n}$$

$\sigma \propto y$

$$V_{Tn} \propto r$$

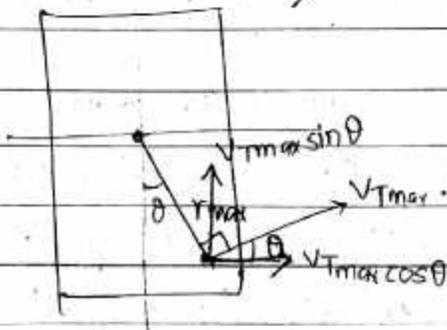
(Bending stress) behave $\propto r$

direction shear $\propto r$ along θ (bolt)

$$M = \frac{V_{Tn}}{r_n} r_1^2 + \frac{V_{Tn}}{r_n} r_2^2 + \frac{V_{Tn}}{r_n} r_3^2 + \dots + \frac{V_{Tn}}{r_n} r_n^2$$

$$= \frac{V_{Tn}}{r_n} [r_1^2 + r_2^2 + \dots + r_n^2]$$

$$M = \frac{V_{Tn} \times \sum r_i^2}{r_n}$$



$$\therefore V_T \cdot V_{Tn} = \frac{M \times r_n}{\sum r_i^2}$$

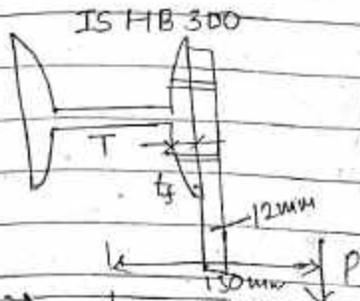
$$V_{Tmax} = \frac{M \times r_{max}}{\sum r_i^2}$$

Vertical Shear force on each bolt (V) = $\frac{P}{N}$

$$\text{Resultant (R)} = \sqrt{V_x^2 + V_y^2}$$

$$V_y = V + V_{Tmax} \sin \theta$$

calculate max. value of load p, that can be applied in the following connection



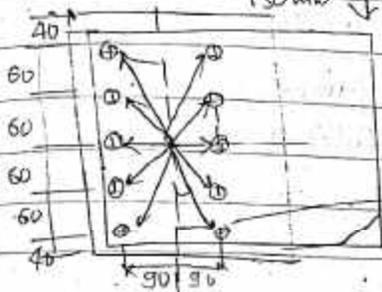
Now,

$$d = 16 \text{ mm}$$

$$d_o = 18 \text{ mm}$$

$$f_{ub} = 400 \text{ MPa}$$

$$f_{yb} = 240 \text{ MPa}$$



(a) Design shear capacity of bolt

$$V_{dsb} = \frac{f_{ub} \times 0.787 d^2}{\sqrt{3} \times 1.25 \times 4}$$

$$= \frac{400 \times 0.787 \times 16^2}{\sqrt{3} \times 1.25 \times 4}$$

$$= 28.974 \text{ kN} \quad \text{--- (i)}$$

$$V_{dsb} \leq \text{bolt value}$$

(b) Bearing capacity, k_b can be found as

$$\frac{e}{3d_o}, \frac{p}{3d_o} - 0.25, 1, \frac{f_u}{f_{ub}}$$

$$\frac{40}{3 \times 18}, \frac{60}{3 \times 18} - 0.25, 1, \frac{410}{240}$$

$$0.740, 0.86, 1, 0.970$$

$$k_b = 0.740$$

for ISHB, 300 63 kg, thickness of flange = 10.6 mm

$$V_{dpb} = 2.5 \times 0.740 \times 16 \times 10.6 \times 400$$

$$1.25$$

$$= 100.403 \text{ kN} \quad \text{--- (ii)}$$

So, Bolt value = min. of (i) & (ii)

$$= 28.974 \text{ kN}$$

$$\text{Then, } \sum r_i^2 = 2 \times 90^2 + 4 \times 108.16^2 + 4 \times 150^2 = 152994.34$$

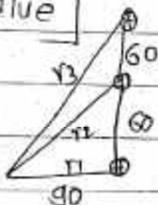
from 5 A

ISHB. 300 58.8

300 63.0

X-section - T

flange thickness = t_f



$$r_1 = 90$$

$$r_2 = 108.16$$

$$r_3 = 150$$

← find

section 11

$$r_{max} = \sqrt{150 \times 150}$$

$$\therefore V_{Tmax} = \frac{P e_c \times r_{max}}{S_n^2}$$

$$V_{Tmax} = \frac{P \times 150 \times 150}{152994.34} = 0.147P$$

$$V_{Tmax} \sin \theta = 0.147P \sin \theta = 0.08818P$$

$$V = \frac{P}{N} = \frac{P}{10} = 0.1P$$

$$V_y = V + V_{Tmax} \sin \theta = 0.18818P$$

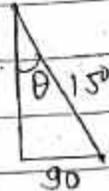
$$\text{SO, } R = \sqrt{V_x^2 + V_y^2} = \sqrt{(0.1176P)^2 + (0.18818P)^2}$$

$$= P \times 0.222$$

$$\text{Since, } R \leq 28.97$$

$$0.222P \leq 28.97$$

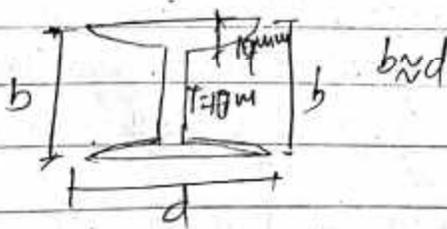
$$\therefore P \leq 131.68 \text{ kN}$$



$$\therefore \theta = \sin^{-1}\left(\frac{90}{150}\right) = 36.87^\circ$$

$$V_x = V_{Tmax} \cos \theta = 0.1176P$$

Design bolted connection to carry an axial load of 180 kN at a eccentric distance of 250 mm applied parallel to flange. Use M20 bolt of pr. ci 4.6. The column SC 250



The thickness of bracket is 16 mm

$$n = \sqrt{\frac{6Pe}{m p v d s b}}$$

$$t_b = 16 \text{ mm}$$

Soln:-

Given:

Axial load (W.L) = 180 kN

Design load = 270 kN

Pr. Cl: 4.6

$f_{ub} = 400 \text{ MPa}$

$f_{yb} = 240 \text{ MPa}$

$f_u = 410 \text{ MPa}$ for Fe 410

eccentric distance 250 mm

column is EC 250

$t_f = 19 \text{ mm}$

$d = 20 \text{ mm}$, $d_o = 22 \text{ mm}$

bracket thickness = 16 mm

$$\text{Design shear strength of bolt } (V_{dsb}) = \frac{400}{\sqrt{3} \times 1.25} \times \left(0.78 \times \pi \times \frac{20^2}{4} + 0 \right)$$

$$= 45.272 \text{ kN}$$

$$\text{no. of bolts } n = \sqrt{\frac{6 P e_c}{m p v_{dsb}}}$$

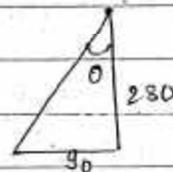
$$\text{Pitch } (p) \geq 2.5 d = 50 \text{ mm}$$

$$\text{end distance } e \geq 1.5 d_o = 1.5 \times 22 = 33 \text{ mm}$$

take pitch = 60 mm

$$e_{nd} = 40 \text{ mm}$$

$$\therefore n = \sqrt{\frac{6 \times 270 \times 250}{2 \times 60 \times 45.272}} = 8.03 \approx 9$$



$$\tan \theta = \frac{90}{280}$$

$$\therefore \theta = 20.55^\circ$$

section II

(ii) Bearing capacity can be found as for K_b

$$V_{dpb} = \frac{2.5 \times 0.606 \times 20 \times 16 \times 400}{1.25}$$

$$= 155.136 \text{ kN}$$

$$\Rightarrow \frac{40}{3 \times 22}, \frac{60}{3 \times 22} - 0.25, 1, \frac{400}{4 \times 0}$$

$$0.606, 0.659, 1, 0.9756$$

Bolt value = 45.212 kN

$$\text{For, } V_{Tmax} = \frac{P e_c \Gamma_{max}}{\sum r_i^2}$$

$$\Gamma_{max} = 294.108 \times 256.32$$
$$\sum r_i^2 = 2 \times 90^2 + 4 \times 108.17^2 + 4 \times 150^2 + 201.246^2 \times 4 + 4 \times 256.32^2$$
$$= 577802.57$$

$$\text{① } \therefore V_{Tmax} = \frac{270 \times 250 \times 256.32}{577802.57} = 29.94 \text{ kN}$$

$$\text{② } V_y = V + V_{Tmax} \sin \theta = \frac{P}{N} + 29.94 \sin \theta = 45.50 \text{ kN}$$

$$\text{③ } V_x = V_{Tmax} \cos \theta = 28.034 \text{ kN}$$

$$\text{④ } R = \sqrt{V_x^2 + V_y^2} = 38.1236 \text{ kN}$$

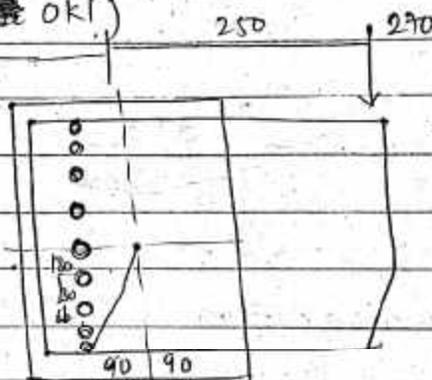
Since

$R \leq$ Bolt value (OK)

~~No need~~

Redesigning.

for pitch $p = 80 \text{ mm}$
 $e = 40 \text{ mm}$



$$\Gamma_{max} = 332.41 \text{ mm}$$

$$\sum r_i^2 = 913860$$

$$\therefore V_{Tmax} = \frac{270 \times 250 \times 332.41}{913860} = 24.55 \text{ kN}$$

$$\theta = \tan^{-1} \left(\frac{90}{320} \right)$$
$$= 15.70^\circ$$

$$V = \frac{P}{N} = \frac{270}{9} = 30 \text{ kN}$$

$$V_y = V + V_{Tmax} \sin \theta = 36.64 \text{ kN}$$

$$V_x = V_{Tmax} \cos \theta = 23.64 \text{ kN}$$

$$R = \sqrt{V_x^2 + V_y^2} = 43.60 \text{ kN}$$

So, $R \leq$ Bolt value is satisfied.

Hence, provide 18 M20 Bolt of Prcl: 4.6 with pitch = 80 mm, end distance 40 mm
with bolt value = 45.272 kN

215 जोड़कर दिखा

CH-4 connection Design:

Welded connection

→ connects two metal plates

advantage and disadvantage

rigid connection

can be jointed any shape

high efficiency $\approx 100\%$

No drillings

Economic

light in weight

skilled manpower

brittle joint

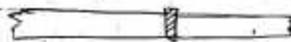
Electricity

no better performance in fatigue

Maintenance cost is high

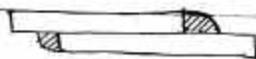
Types of welded connection:

1) Butt weld (groove weld)



Rectangular Butt joints

2. fillet weld:



Others:



Double-tee weld



single Tee-weld

billet weld:

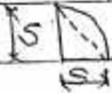
⇒ Size of fillet weld: (S)

① Max weld size depends upon thickness of thinner plate

for rectangular = $t - 1.5$

for rounded = $\frac{3}{4} \times t$

t = thickness of thinner plate.

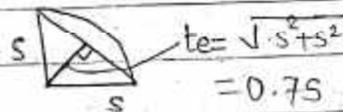


② Min. size of weld depends upon the thickness of

thicker plate given by table 2.1

page: 78

Throat thickness (t_e): It is the effective size of weld.

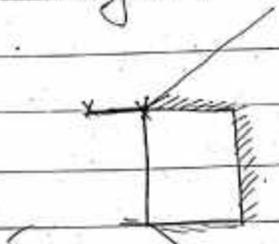


$$t_e = \sqrt{s^2 + s^2} \\ = 0.7s$$

$$t_e = K \times s \text{ constant}$$

K - constant given by Table 22, for give angle betⁿ fusion face

effective length of weld: It is the length of weld of full size / Area of weld.



$$l_e = l_w - 2s$$

l_w = overall length of weld

End return:



Extra length of weld provided to opposite side of welding

$$\text{effective area} = A_e = l_e \times t_e$$

gusset plate - it can't take strength

tack bolt only for assist connection
extra bolt to meet design specification

Page (78-79)

overlap: common length of two plates: $\geq 90\text{mm}$

$\geq 4t \rightarrow t$ thickness of thinner plate

Calculation of strength

a) Design strength of weld (f_{wd}) = $\frac{f_{uw}}{\gamma_{mw}}$

= $\frac{f_u}{\sqrt{3} \gamma_{mw}}$

$\gamma_{mw} \rightarrow$ Table 5

1.25 shop

1.50 field

Design welded connection to connect the plates $120 \times 12\text{mm}$ to a gusset plate of thickness 20mm to carry an axial load of 600kn by fillet welds:

assume field fabrication ($\gamma_{mw} = 1.50$)

$f_u = 410\text{Mpa}$

A) size of weld

1) Min size of weld (S_{min}) = 5mm for $t = 10-20\text{mm}$ of thick plate.

2) Max size of weld (S_{max}) = $t - 1.5 = 12 - 1.5 = 10.5\text{mm}$
adopt, $S = 8\text{mm}$

B) Effective throat thickness (t_e) = $0.7S = 0.7 \times 8 = 5.6\text{mm}$

c) effective length of throat weld

d) Design strength of weld (f_{wd}) = $\frac{f_u}{\sqrt{3} \gamma_{mw}} = \frac{410}{\sqrt{3} \times 1.50} = 157.81\text{Mpa}$

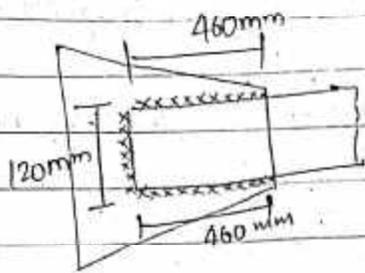
Now, P_u (ultimate load) = $A_e \times f_{wd}$

$600 \times 10^3 \times 1.5 = L_e \times 157.81$

$\therefore L_e = 1018.403\text{mm}$

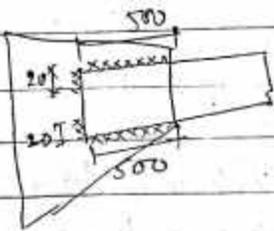
overlap $\geq 40\text{mm}$

$\geq 4 \times 12 = 48\text{mm}$



$$\begin{aligned}
 l_w &= l_e + 2s \\
 &= 1018.403 + 2 \times 8 \\
 &= 1034.403 \text{ mm} \\
 &= \frac{1034.403 - 120}{2} \\
 &= 457 \text{ mm}
 \end{aligned}$$

अतः



take $\approx 460 \text{ mm} > 480 \text{ mm}$.

Design welded connection to connect an angle ISA 100x100x10 mm to a gusset plate of thickness 16 mm, coming an axial load of 100 kN if not state (- such that the load transfer through the CG of angle)

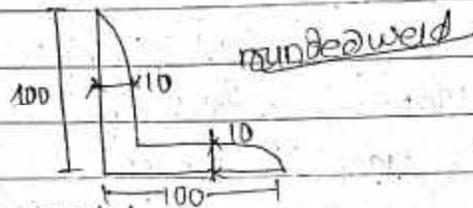
Soln:

for angle: ISA 100x100x10

$$C_x = C_y = 284 \text{ mm}$$

$$\text{axial load} = P = 100 \text{ kN}$$

$$\text{Ultimate load } P_u = 100 \times 1.5 = 150 \text{ kN}$$



Now,

size shape of weld $\Rightarrow S_{\max} = \frac{3}{4} \times t = \frac{3}{4} \times 10 = 7.5 \text{ mm}$

$$S_{\min} = 5 \text{ mm}$$

$$\text{take } s = 7 \text{ mm}$$

$$\text{Throat thickness } (l_e) = 0.7s = 0.7 \times 7$$

$$= 4.9 \text{ mm}$$

$$\text{Design stress of weld} = \frac{f_u}{\sqrt{3} \times 1.50} = \frac{410}{\sqrt{3} \times 1.50} = 157.81 \text{ Mpa}$$

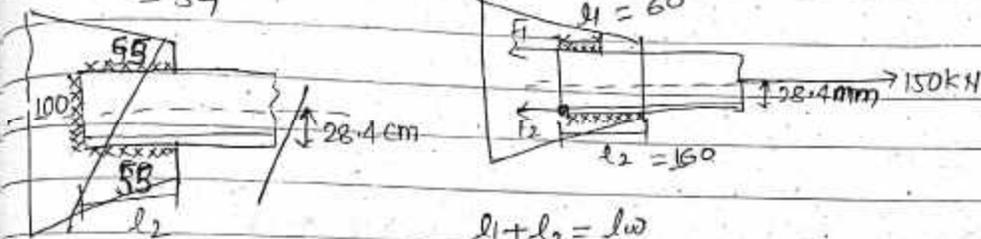
$$\text{ultimate load} = A_e \times f_{wd} = l_e \times t_e \times f_{wd}$$

$$\therefore l_e = \frac{150 \times 10^3}{4.9 \times 157.81} = 193.99 \text{ mm}$$

$$\begin{aligned}
 l_w &= l_e + 2s \\
 &= 193.99 + 2 \times 7 \\
 &= 193.99 + 14 \\
 &= 194 + 14 \\
 &= 208 \text{ mm}
 \end{aligned}$$

$$\begin{aligned}
 \text{Overlap} &\Rightarrow > 40 \text{ mm} \\
 &\geq 4 \times 10 = 40 \text{ mm}
 \end{aligned}$$

$$\begin{aligned}
 &= \frac{208 - 100}{2} \\
 &= \frac{108}{2} \\
 &= 54
 \end{aligned}$$



$$l_1 + l_2 = l_w$$

$$F_1 = l_1 \times t_e \times f_{wd}$$

$$F_2 = l_2 \times t_e \times f_{wd}$$

taking moment about bottom of angle

$$150 \times 284 = l_1 \times 1.9 \times 157.81 \times 100$$

$$\therefore l_1 = 55 \text{ mm}$$

$$\text{take } l_1 = 60 \text{ mm}$$

$$\begin{aligned}
 l_2 &= 208 - 60 \\
 &= 148
 \end{aligned}$$

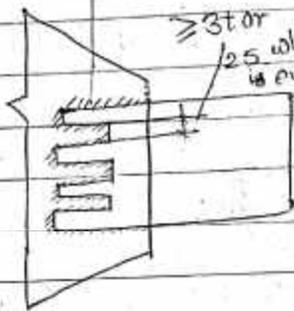
$$\text{take } l_2 = 160 \text{ mm}$$

Welded connection

Slot and plug connection.



or,



if the length of weld required is not available special weld are done as shown named plug weld.

21.12 (theory rev)

Design fillet weld to connect a tie member 120×12 mm to a gusset plate of 16 mm ^{thickness} carrying factored axial load of 900 kN if the overlap is restricted to 200 mm. (shop)

Given:-

Pull (ultimate load) = 900 kN

Size of weld \Rightarrow

$$S_{max} = \frac{3}{4} \times t = \frac{3}{4} \times 12 = 9 \text{ mm} \quad t = 1.5$$

$$= 12 - 1.5 = 10.5 \text{ mm}$$

$S_{min} = 5$ mm

take $s = 7$ mm

so,

throat thickness = $t_e = 0.7s$
 $= 0.7 \times 7$
 $= 4.9$ mm

Design stress of weld = $\frac{f_u}{\sqrt{3} \times 1.25} = \frac{410}{\sqrt{3} \times 1.25} = 189.37$

$$\text{ultimate load} = A_e f_w d$$

$$= l_e t_e f_w d$$

$$\therefore l_e = \frac{950 \times 10^3}{4.9 \times 189.37}$$

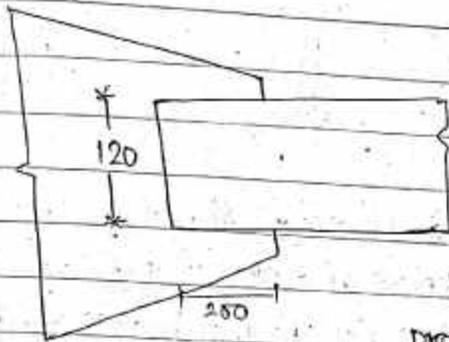
$$= 969.91 \text{ mm}$$

$$\therefore l_w = l_e + 2s = 969.91 + 2 \times 4.9$$

$$= 983.91 \text{ mm}$$

Overlap $\geq 40 \text{ mm}$

$$\geq 4 \times 12 = 48 \text{ mm}$$



Since, the length of weld required is $>$ ^{length} available in fillet weld.

So,

$$\text{Slot weld} = 983.91 - (120 + 250 \times 2)$$

$$= 463.91 \text{ mm}$$

provide, no. of slot required = 2 slot

(width of slot)

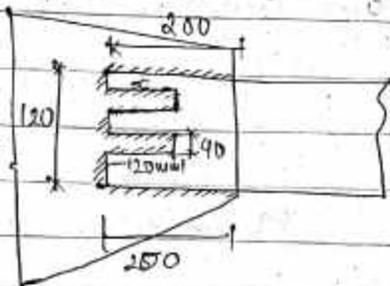
$$w_t \geq 3t = 3 \times 12 = 36 \text{ mm}$$

$$\geq 25$$

$$= 25 \text{ mm}$$

of $120 \times 40 \text{ mm}$

\therefore provided slot weld is



k # Butt weld or groove weld:

It is a end to end connection

Types

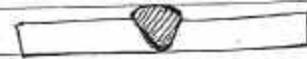
(i) Single U-weld



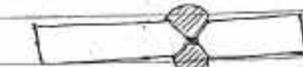
(ii) Double U-weld



(iii) Single V-weld



(iv) Double-V-weld



(v) Tee weld.



(vi) Double Tee.



→ All the design criteria are similar to the fillet weld except throat thickness
→ Throat thickness is taken as equal to thickness of thinner plate in case of complete penetration. (all double weld) and $(\frac{7}{8})$ of the thickness of thinner plate, in incomplete penetration.

But throat thickness is taken as $(\frac{5}{8})$ of thickness of thinner plate for design consideration in incomplete penetration.

Design connection betⁿ 2 plates 200×10 mm carrying ^{axial} factored load of 120 kN

(i) Single U-weld

(ii) Double U-weld

(a) Given:

for $S, S_{max} =$

$$P_u = 120 \text{ kN}$$

$$t = 10 \text{ mm}$$

Now, in Sing U-weld.

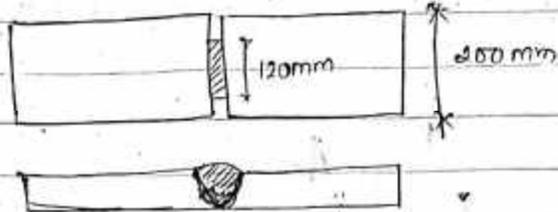
$$\text{Throat thickness} = \frac{5}{8} \times t = \frac{5}{8} \times 10 = 6.25 \text{ mm}$$

$$f_{wd} = \frac{f_u}{\sqrt{3} \times 1.25} = \frac{410}{\sqrt{3} \times 1.25} = 189.37 \text{ kN}$$

Then:

$$P_u = l_e t e f_w d$$

$$\therefore l_e = \frac{120 \times 1000}{6.35 \times 189.37} \\ = 101.38 \text{ mm}$$



$$l_w = l_e + 2t$$

$$= 101.38 + 2 \times 10$$

$$= 121.38 \text{ mm}$$

take, $l_e = 120 \text{ mm}$

⊕ for double channel.

Given:

$$P_u = 120 \text{ kN}$$

$$t = 10 \text{ mm}$$

$$\text{⊕ } f_w d = \frac{f_u}{\sqrt{3} \times 1.25} = \frac{410}{\sqrt{3} \times 1.25} = 189.37 \text{ kN}$$

$$\text{thread thickness} = \frac{7}{16} \times 10 = 10.00 \text{ mm}$$

$$\therefore P_u = l_e t e f_w d$$

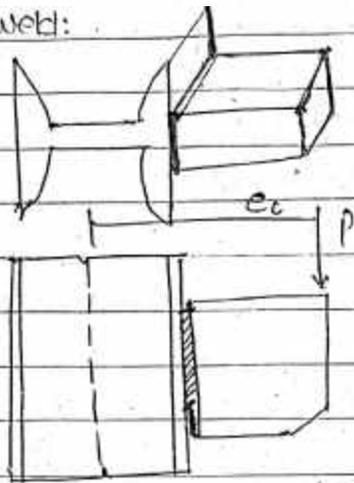
$$l_e = \frac{120 \times 1000}{10.00 \times 189.37} \\ = 63.42 \text{ mm} \\ = 63.37 \text{ mm}$$



Eccentric connection:

* Perpendicular to flange [weld under bending & shear]

(a) Butt weld:



$$Z = \frac{bd^2}{6}$$
$$= \frac{te \times tw^2}{6}$$

design stress of weld $f_{wd} = \frac{f_u}{\sqrt{3} \times \gamma_{mw}}$

weld is under bending stress and shear stress

(a) shear stress in weld (q) = $\frac{P}{lw \times te}$

(b) Bending stress in weld (f_b) = $\frac{M}{Z}$

$$= \frac{M}{\frac{te \times tw^2}{6}}$$

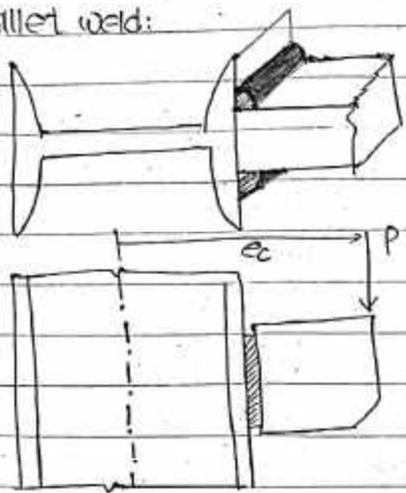
$$\therefore f_b = \frac{6M}{te \times tw^2} = \frac{6Pec}{te \times tw^2}$$

∴ Resultant stress = $\sqrt{f_b^2 + 3q^2} \leq f_{wd}$

(ii) for design:

length of weld required (lw) = $\sqrt{\frac{6Pec}{te \times (f_u/\gamma_{mw})}}$

(b) fillet weld:



a) design shear stress of weld (f_w)

$$= \frac{f_y}{\sqrt{3} \sigma_{mw}}$$

weld is under bending and shear

b) shear stress in weld = $\frac{P}{2lwte} = q$

c) Bending stress (f_b) = $\frac{M}{2Z} = \frac{6Pec}{2lwt^2}$

Resultant stress = $\sqrt{f_b^2 + 3q^2} \leq f_{wd}$

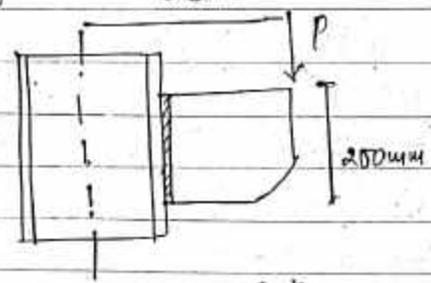
Now;

for design

length of weld (lw) = $\sqrt{\frac{6Pec}{2te(\sigma_{mw})}}$

Calculate max. value of load P that can be applied in following connector

Given;



$t_e = 4.9 \text{ mm}$

Given

$e_c = 250 \text{ mm}$

$lw = 200 \text{ mm}$

$t_e = 4.9 \text{ mm} = 0.75$

size of weld = 7mm

shear stress in weld (q) = $\frac{P}{2lwte}$

= $\frac{P}{2 \times 200 \times 4.9}$

= $5.1 \times 10^{-4} P$

$$\begin{aligned} \text{Bending stress (} f_b \text{)} &= \frac{M}{Z} \\ &= \frac{6 P e_c}{2 \times t_e l_w^2} = \frac{6 \times P \times 250}{2 \times 4.9 \times 200^2} \\ &= 3.82 \times 10^{-3} P \end{aligned}$$

$$\begin{aligned} \text{Resultant stress (} R \text{)} &= \sqrt{3f_t^2 + f_b^2} \\ &= P \times \sqrt{3 \times (5.1 \times 10^{-4})^2 + (3.82 \times 10^{-3})^2} \\ &= 3.92 \times 10^{-3} P \end{aligned}$$

$$\text{design stress of weld (} f_{wd} \text{)} = \frac{410}{\sqrt{3} \times 1.25} = 189.37 \text{ KN}$$

for safe design

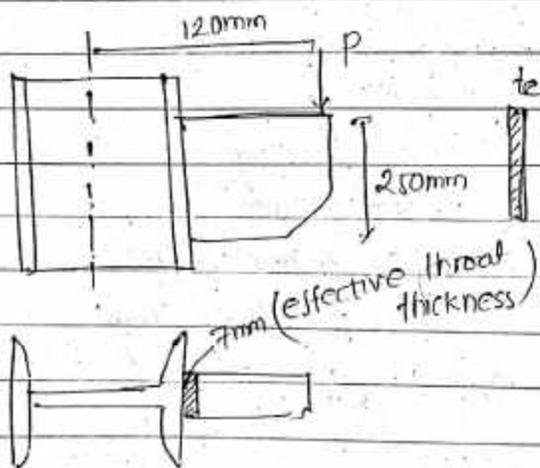
$$R \leq f_{wd}$$

$$3.92 \times 10^{-3} P \leq 189.37$$

$$\therefore P_u \leq 48.30 \text{ KN}$$

$$\therefore \text{Working load (} P \text{)} = 32.21 \text{ KN}$$

#



Solⁿ.

Given:

$$\text{load} = P$$

$$e_c = 120 \text{ mm}$$

$$t_e = 7 \text{ mm}$$

$$l_w = 250 \text{ mm}$$

design shear stress in weld,

$$f_{wd} = \frac{f_u}{\sqrt{3} \times 1.25} = \frac{410}{\sqrt{3} \times 1.25}$$

$$= 189.37 \text{ KN}$$

$$\begin{aligned} \text{Bending stress } (f_b) &= \frac{M}{Z} \\ &= \frac{6Pec}{t_e l_w^2} \\ &= \frac{6 \times P \times 120}{7 \times 250^2} \\ &= 1.645 \times 10^{-3} P \end{aligned}$$

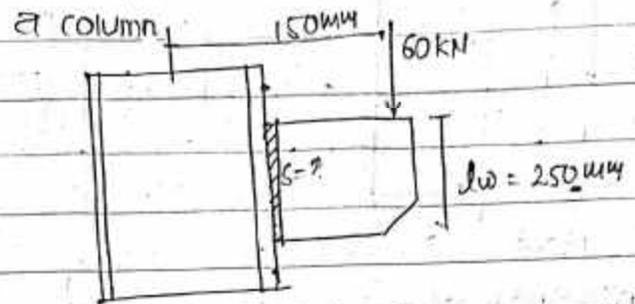
$$\begin{aligned} \text{Shear stress } (q) &= \frac{P}{l_w t_e} \\ &= \frac{P}{250 \times 7} \\ &= 5.714 \times 10^{-4} P \end{aligned}$$

$$\begin{aligned} R &= \sqrt{f_b^2 + 3q^2} \\ &= P \times 4.75 \times 10^{-3} \end{aligned}$$

For safe design,
 $R \leq f_{wd}$

$$\begin{aligned} P \times 4.75 \times 10^{-3} &\leq 189.37 \\ \text{or, } P &\leq \frac{189.37 \times 10^3}{4.75} \\ \therefore P &\leq 39.873 \text{ kN} \end{aligned}$$

Determine the size of fillet weld required to join a bracket plate with a flange of a column.



Now, Given

$$\begin{aligned} P &= 60 \text{ kN} \\ e_c &= 150 \text{ mm} \\ t_e &= 0.7s \\ l_w &= 250 \text{ mm} \end{aligned}$$

(a) design shear stress of weld $f_{wd} = \frac{f_u}{\sqrt{3} \times 1.25} = 189.37 \text{ kN}$

b) shear stress $(q) = \frac{P}{2 t_e l_w} = \frac{60}{2 \times t_e \times 250} = \frac{0.12}{t_e}$

c) Bending stress $(f_b) = \frac{6Pec}{2 t_e l_w^2} = \frac{0.432}{t_e}$

$$\begin{aligned} R &= \sqrt{f_b^2 + 3q^2} = \frac{1}{t_e} \times \sqrt{0.12^2 + 0.432^2} \\ &= \frac{0.479}{t_e} \end{aligned}$$

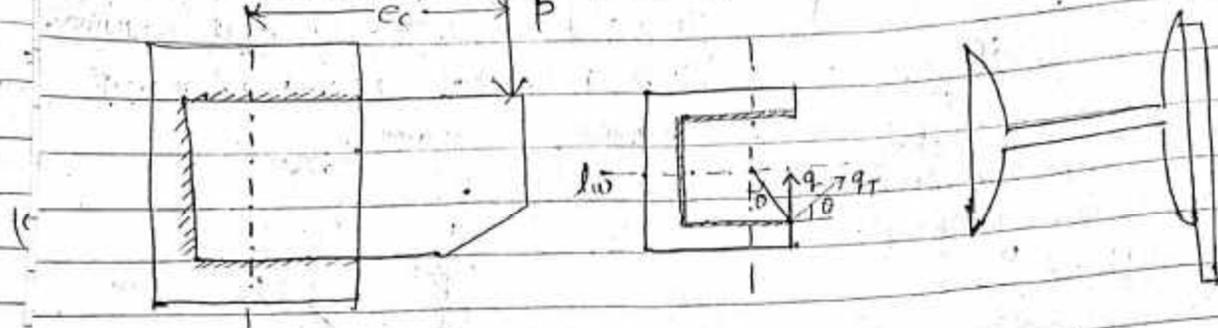
e) so, $R \leq f_{wd}$

$$\text{or, } \frac{0.479}{t_e} \leq 189.37$$

$$\therefore t_e \geq 2.53 \text{ mm}$$

$$\& s = \frac{t_e}{0.7} = 3.61 \text{ mm}$$

Welded connection. When load applied parallel to flange



Here,

(a) Vertical Shear stress in weld $(q) = \frac{P}{l \cdot s}$ $\left(\frac{T}{I_p} = \frac{T}{R}\right)$

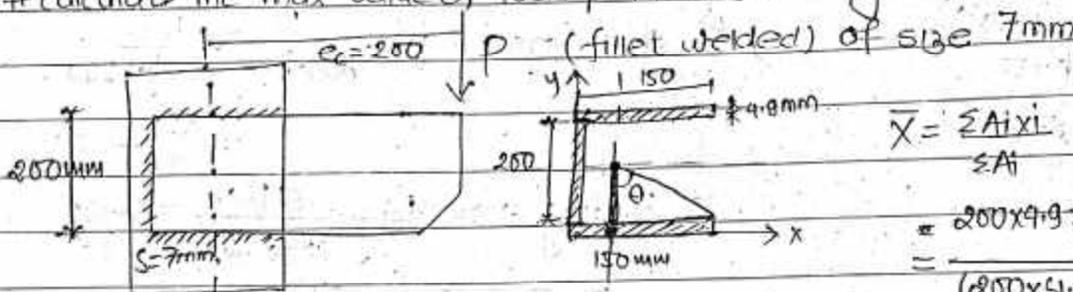
(b) Torsional stress in weld $(q_T) = \frac{P \cdot e_c \cdot r_{max}}{I_p}$

(c) Shear stress along x-axis $(\sigma_x) = q_T \cos \theta$

$\therefore \sigma_y = q_T \sin \theta + q$

(d) Resultant stress $(\sigma) = \sqrt{\sigma_x^2 + \sigma_y^2} \leq f_{wd}$

Calculate the max value of load p in the following eccentric connection:



$s = 7 \text{ mm}$

$e = 0.7s = 0.7 \times 7$

$= 4.9 \text{ mm}$

$$\bar{x} = \frac{\sum A_i x_i}{\sum A_i}$$

$$= \frac{200 \times 4.9 \times \frac{4.9}{2} + 2 \times 150 \times 4.9 \times \frac{150}{2}}{(200 \times 4.9) + (2 \times 150 \times 4.9)}$$

$= 45.98 \text{ mm}$

Due to symmetry, $\bar{y} = 104.9 \text{ mm}$

$$I_{xx} = \frac{4.9 \times 200^3}{12} + \frac{2 \times 150 \times 4.9^3}{12} + 200 \times 4.9 \times \left(\frac{4.9}{2} - 45.98\right)^2$$

$$+ 2 \times 150 \times 4.9 \times \left(\frac{150}{2} - 104.9\right)^2$$

$= 18698731.57 \text{ mm}^4$

$$I_{yy} = \frac{200 \times 4.9^3}{12} + \frac{2 \times 150 \times 4.9^3}{12} + 200 \times 4.9 \times \left(\frac{4.9}{2} - 45.98\right)^2$$

$$+ 2 \times 150 \times 4.9 \times \left(\frac{150}{2} - 45.98\right)^2$$

$$I_p = I_{xx} + I_{yy}$$

$$= 24551881.86 \text{ mm}^4$$

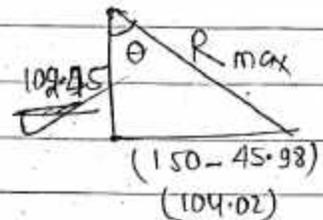
$$V. \text{ Shear stress in weld } (q) = \frac{P_u}{t \times l_w}$$

$$= \frac{P_u}{4.9 \times 500}$$

$$= 4.0816 \times 10^{-4} P$$

$$\text{Torsional stress in weld } (q_T) = \frac{P_u \times 200 \times r_{\max}}{24551881.86}$$

$$= 1.189 \times 10^{-3} P_u$$



So, σ (Resultant) can be calculated as,

$$\sigma_x = q_T \cos \theta = 8.343 \times 10^{-4} P_u$$

$$\sigma_y = 4.0816 \times 10^{-4} P_u + 8.272 \times 10^{-4} P_u$$

$$= 1.255 \times 10^{-3} P_u$$

$$\therefore R_{\max} = \sqrt{109.45^2 + 104.02^2}$$

$$= 146.03$$

$$\theta = 45.44^\circ$$

$$\text{So, } \sigma = P_u \times 1.507 \times 10^{-3}$$

$$\text{Then, design shear stress } (f_{wd}) = \frac{f_y}{\sqrt{3} \times 1.25}$$

$$= \frac{410}{\sqrt{3} \times 1.25}$$

$$= 189.37 \text{ kN}$$

for safe design

$$\text{So, } \sigma \leq f_{wd}$$

$$1.507 \times 10^{-3} P_u \leq 189.37$$

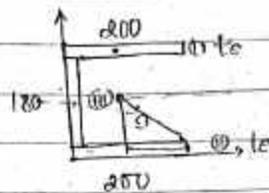
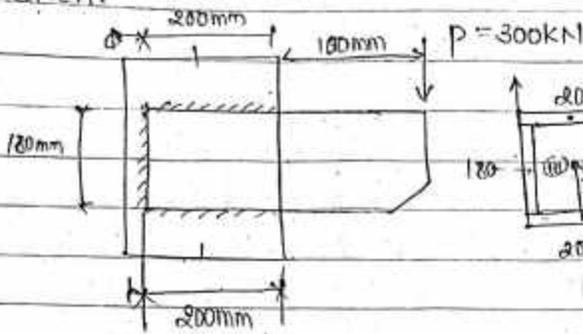
$$\therefore P_u \leq 125.6 \text{ kN}$$

$$\therefore \text{working load} = \frac{125.6}{1.5}$$

$$\therefore P = 83.757 \text{ kN}$$

Calculate the size of weld required in following connection:

Given:



Section	Area	\bar{x}	\bar{y}
(i)	$400te$	100 ($\frac{200}{2}$)	$\frac{te}{2}$
(ii)	$200te$	$\frac{1}{2} \times 100$	$\frac{te}{2}$
(iii)	$180te$	$\frac{200te}{2}$	$(te+90)$
580te			

$$\text{So, } \bar{x} = \frac{100 \times 200te + 100 \times 200te + 180te \times \frac{200te}{2}}{580te}$$

$$= \frac{(40000 + 180te)}{580}$$

$$= (68.96 + 0.31te) = 68.96 + 0.16te$$

$$\bar{y} = (te + 90) \approx 90 \quad \approx 68.96 \text{ mm}$$

$$I_{xx} = 2 \times \frac{200 \times te^3}{12} + 2 \times 200te \times \left[\frac{te}{2} - te - 90 \right]^2 + 200 \times te \times \left(180 + \frac{te}{2} - te - 90 \right)^2$$

$$= 200 \times te \times 90^2 + 200 \times te \times 90^2 + \frac{te \times 180^3}{12} + (te + 90 - te - 90)^2 \times 180te$$

$$= 3240000te + 486000te$$

$$= 3726000te$$

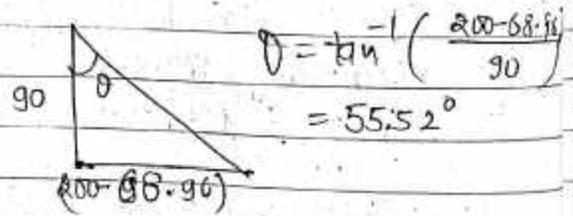
$$I_{yy} = \frac{180te^3}{12} + 180 \times te \times 68.97^2 + 2 \times \left[\frac{te \times 200^3}{12} + 200 \times te \times (68.97 - 100)^2 \right]$$

$$= 2574964.4te$$

$$I_p = I_{xx} + I_{yy} = 6300964.4te$$

$$r_{max} = \sqrt{90^2 + (200 - 68.96)^2}$$

$$= 158.970$$



$$\theta = \tan^{-1} \left(\frac{200 - 68.96}{90} \right)$$

$$= 55.52^\circ$$

$$e_c = (100 + 200 - 68.96)$$

$$= 231.04$$

$$P = 300 \text{ kN}$$

$$\theta = 55.52^\circ$$

Then,

$$\begin{aligned} \text{Vertical shear stress } (q) &= \frac{P}{t \times l_w} \\ &= \frac{300}{t \times 580} \\ &= \frac{0.5172}{t} \end{aligned}$$

$$\begin{aligned} \text{Torsional stress } (q_t) &= \frac{P e_{\text{max}}}{I_p} \\ &= \frac{300 \times 231.04 \times 158.97}{6350464.4 t} \\ &= \frac{1.74}{t} \end{aligned}$$

$$\begin{aligned} q_{\text{max}} = \sigma_x &= q_t \cos \theta \\ &= \frac{1.74}{t} \times \cos 55.52^\circ \\ &= \frac{0.9907}{t} \end{aligned}$$

$$\begin{aligned} \sigma_y &= q_t \sin \theta + q \\ &= \frac{1.434}{t} + \frac{0.5172}{t} \\ &= \frac{1.952}{t} \end{aligned}$$

$$\therefore R = \sqrt{\sigma_x^2 + \sigma_y^2} = \frac{2.188}{t}$$

for safe design

$$R \leq \text{fwd}$$

$$\frac{2.188}{t} \leq 189.37$$

$$\therefore t \leq 11.55 \text{ mm}$$

$$\text{so, } t = 0.75$$

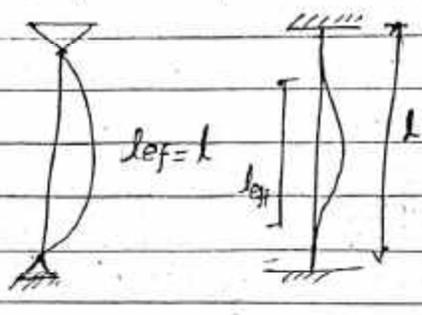
$$\therefore S = 16.51 \text{ mm}$$

CH:6 Compression member

if a structural member is under axial compression as a major action sometimes as accompanied by moment is called compression member.
 eg. column, post, vertical member of truss are under axial loading.

Effective length:

It is length betⁿ two points of zero rotation
 It depends upon boundary condition.

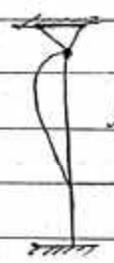


① effective length is given by table.
 It is 800

$$l_{eff} = k \cdot L$$

$$l_{eff} = 0.65L$$

Generally



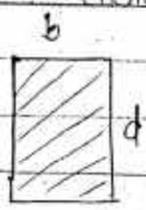
② Radius of gyration: It is a physical quantity whose square multiplied by area gives MOI

ie,

$$r^2 \times A = I$$

$$\therefore r = \sqrt{\frac{I}{A}}$$

Slenderness ratio (λ): It is the ratio of effective length to least lateral dimension. In case of steel structure slenderness ratio is taken



as effective length to min. radius of gyration.

$$\lambda = \frac{l_{eff}}{r_{min}}$$



$$l_e = \frac{l_{eff}}{b}$$

Buckling :- It is the lateral bending observed in compression member. Most of compression members are failed by buckling

Types of compression members:

- 1) column
- 2) Post
- 3) strut
4. struts → standhions

Types of buckling

- a) flexural
- b) Torsional
- c) flexural-torsional



Design of compression member:-

a) Design compressive strength:

$$\text{load carrying capacity (Pd)} = f_{cd} \times A$$

f_{cd} = Design compressive strength

calculation of f_{cd}

Method: ① 7.1.2.1

$$f_{cd} = \frac{f_y / \gamma_{m0}}{\phi + [\phi^2 - \lambda^2]^{0.5}}$$

α - Imperfection factor.

Table: 7 clause 7.1.1

$$\phi = 0.5 [1 + \alpha(1 - 0.2) + \lambda^2]$$

Buckling class a b c d

$$\lambda = \sqrt{f_y / f_{cc}}$$

α 0.21 0.34 0.49 0.71

$$f_{cc} = \frac{\pi^2 E}{(\frac{KL}{r})^2}, E = 2 \times 10^5 \text{ N/mm}^2$$

Buckling class: table 10

$$\gamma_{m0} = 1.1 \text{ for buckling}$$

Method ② f_{cd} is calculated from: table: 9 as per buckling class and

Slenderness ratio, $f_y \Rightarrow$ generally 250 MPa

a, b, c, d → class

$$\frac{KL}{r} \Rightarrow$$

Calculate load carrying capacity of SC-250 having unsupported length of 5m. One end of column is restrained against both rotation & translation while other is free on rotation but restrained against translation.
 Use: Grade of steel: Fe-410.

from IS: 808-1989

For SC-250

$$A = 109 \text{ cm}^2$$

$$D = 250 \text{ mm}$$

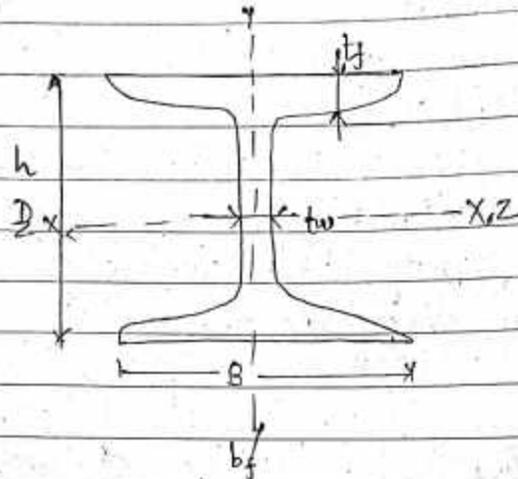
$$B = 250 \text{ mm}$$

$$T = t_f = 17 \text{ mm}$$

$$t = t_w = 10 \text{ mm}$$

$$r_x = 10.7 \text{ cm}$$

$$r_y = 5.46 \text{ cm}$$



Design compressive strength

for x or z axis

$$\frac{h}{b_f} = \frac{D}{B} = 1 < 1.2$$

$$t_f = 17 < 100 \text{ mm}$$

axis

so, z-z axis

Y-Y axis:

buckling class

b

c

Buckling class

b X-X axis

c Y-Y axis

along X-X axis:

$$K = 0.8$$

$$\lambda = \sqrt{\frac{f_y}{f_{cc}}} = \sqrt{\frac{250}{\frac{\pi^2 \times 2 \times 10^5}{(0.8 \times 5000)^2}}} = 0.42$$

$$\alpha = 0.34$$

$$\phi = 0.5 [1 + \alpha(0.42 - 0.2) + 0.42^2]$$

$$= 0.5 [1 + 0.34 \times 0.22 + 0.42^2] = 0.626$$

Then

$$f_{cd} = \frac{f_y / \gamma_{mo}}{[\Phi + (\Phi^2 - \lambda^2)^{0.5}]}$$
$$= \frac{250}{1.10 [0.626 + (0.626^2 - 0.42^2)^{0.5}]}$$
$$= 208.58 \text{ N/mm}^2 \leq f_y / \gamma_{mo}$$
$$= 208.58 \leq 227.27 \text{ N/mm}^2 \quad (\text{OK!})$$

along \bar{y} - \bar{y} axis:

$$K = 0.8$$
$$\lambda = \sqrt{\frac{250}{\frac{0.8 \times 10^5}{54.60}}} = 146.0824$$

$$d_c = 0.49$$

$$\Phi = 0.5 \left[1 + 0.49 \left(\frac{146.0824}{200} - 0.20 \right) + \frac{146.0824^2}{200^2} \right]$$
$$= 1.8745 = 0.9923$$

$$\therefore f_{cd} = \frac{250}{1.10 \left[1.8745 + (1.8745^2 - 146^2)^{0.5} \right]}$$
$$= \frac{250}{1.10 [0.9923 + (0.9923^2 - 0.824^2)^{0.5}]}$$
$$= 147.066 \leq 227.27 \text{ kN/mm}^2$$

Method (ii) along x-x axis, class: b

$$\text{Slenderness } (\lambda_x) = \frac{L_{eff}}{r_x} = \frac{0.8 \times 5000}{107} = 37.38$$

(c)
$$(\lambda_y) = \frac{L_{eff}}{r_y} = \frac{0.8 \times 5000}{54.6} = 73.26$$

from table:

λ	fd	
30	216	$\frac{y_2 - y_1}{x_2 - x_1} = \frac{y - y_1}{x - x_1}$
37.38	??	$\frac{206 - 216}{40 - 30} = \frac{y - 216}{37.38 - 30}$
40	206	

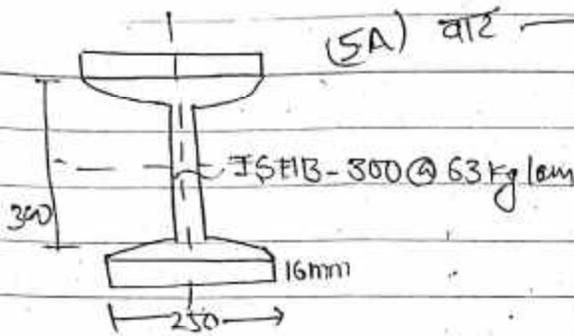
$$\therefore y = 208.62 \text{ N/mm}^2$$

along Y-Y axis, class: C

λ	fd
70	152
80	136
73.26	146.784

$$\therefore fd = 146.784 \text{ N/mm}^2$$

Calculate ultimate load carrying capacity of section (following builtup) of length 7m if both ends are fixed.



(SA) at \rightarrow

For ISHB 300 @ 63 kg/m

$$D = 300 \text{ mm}$$

$$B = 250 \text{ mm}$$

$$t_f = T = 10.6 \text{ mm}$$

$$t_w = t = 9.4 \text{ mm}$$

$$I_{xx} = 13000 \text{ cm}^4$$

$$I_{yy} = 2250 \text{ cm}^4$$

$$r_x = 12.7 \text{ cm}$$

$$r_y = 5.29 \text{ cm}$$

$$A = 80.2 \text{ cm}^2$$

$$I_{xx}' = [I_{xx} + Ah^2]_{\text{HS}} + [I_{xx} + Ah^2]_{\text{plate}} \times 2$$

$$= 13000 \times 10^4 + \left[\frac{250 \times 16^3}{12} + 250 \times 16 \times (150 + 8)^2 \right] \times 2$$

$$= 32988.27 \times 10^4 \text{ mm}^4$$

$$I_{yy}' = 2250 \times 10^4 + 0 + \frac{16 \times 250^3}{12} \times 2$$

$$= 6416.67 \times 10^4 \text{ mm}^4$$

$$\text{So, } I_{yy}' < I_{xx}'$$

$$r_y' = \sqrt{\frac{I_{yy}'}{A'}} =$$

$$A' = 80.2 \times 10 + 250 \times 16 \times 2$$

$$= 160.2 \times 10^2 \text{ mm}^2$$

$$= \sqrt{\frac{6416.67 \times 10^4}{160.2 \times 10^2}}$$

$$= 63.29 \text{ mm}$$

for Builtup class : Buckling class is C Page: 44

So,

for Buckling class: C, $\alpha = 0.49$

for both end fixed, effective length = $0.65L$

$$\lambda = \sqrt{\frac{5y}{f_{cc}}} = \sqrt{\frac{250}{f_{cc}}}$$

$$f_{cc} = \frac{\pi^2 E}{\left(\frac{KL}{r}\right)^2}$$

$$= \frac{\pi^2 \times 2 \times 10^5}{\left(\frac{0.65 \times 7000}{63.29}\right)^2} =$$

$$\therefore f_{cc} =$$

$$\therefore \lambda = \sqrt{\frac{250}{381562}} = 0.809$$

$$\alpha = 0.49$$

$$\phi = 0.5 \left[1 + 0.49 (0.809 - 0.2) + 0.809^2 \right]$$

$$= 0.976$$

$$\therefore f_{cd} = \frac{f_y / \gamma_{mo}}{\left[\phi + (\phi^2 - \lambda^2)^{0.5} \right]} = \frac{250}{1.10 \left[0.976 + (0.976^2 - 0.809^2)^{0.5} \right]}$$

$$= 149.327 \text{ MPa}$$

Method (III)

along Y1 axis: class: C

$$\text{Slenderness } (\lambda) = \frac{l_{eff}}{r} = \frac{0.65 \times 7000}{63.29}$$

$$= 71.891$$

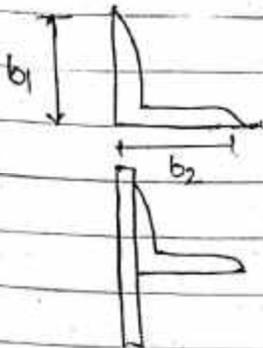
from table:

λ	f_{cd}	f_{cd}
70	0.670	152 MPa
71.891	?	148.974 MPa
80	0.600	136 MPa

$$\therefore f_{cd} \text{ at } 71.891 = 0.657$$

$$f_{cd} = 148.974 \text{ MPa}$$

Angle section : pag 147 7.5.1.2 [one leg loaded]
[use Method I]



$$\lambda_e = \sqrt{k_1 + k_2 A_w^2 + k_3 \lambda_\phi^2}$$

for loaded through one leg:

k_1, k_2, k_3 from table: 12

$$\lambda_w = \left(\frac{L}{r_w}\right)$$

$$\frac{E \sqrt{\pi^2 E}}{250}$$

$r_w \rightarrow$ radius of gyration (min)
about minor axis:

$$\lambda_\phi = \frac{(b_1 + b_2)/2t}{E \sqrt{\pi^2 E}} \cdot 250$$

$$\frac{E \sqrt{\pi^2 E}}{250}$$

aru process same:

(ISA)

calculate load carrying of $110 \times 110 \times 10$ mm of length $l=3$ m between support center is provided with 3 nos. bolt at each end and this hinged supported and both end.

soln:

For ISA $110 \times 110 \times 10$ table (5.1)

$$A = 19.8 \text{ cm}^2 = 2110 \text{ mm}^2$$

$$r_{vw} = 21.6 \text{ mm}$$

From table 12,

$$k_1 = 0.70 \quad \text{so, } \lambda_w \Rightarrow \frac{L}{r_{vw}} = \frac{3000}{21.6} = 138.889$$

$$k_2 = 0.60$$

$$k_3 = 500$$

$$\lambda_{vw} = \frac{138.889}{\left(\frac{250}{250}\right)^{0.5} \times \sqrt{\frac{\pi^2 \times 2 \times 10^5}{250}}}$$

$$= 1.563$$

$$\lambda_\phi = \frac{(110 + 110) \times (110 + 110)}{2 \times 10 \times \sqrt{\frac{\pi^2 \times 2 \times 10^5}{250} \times 1}}$$

$$= 0.124$$

$$\text{So, } \lambda_e = \sqrt{0.70 + 0.60 \times 1.563^2 + 5 \times 0.124^2}$$

$$= 1.498$$

for angle: Buckling class: C

$$\text{So, } \alpha = 0.49$$

Then using Method (I)

$$\phi = 0.5 \left[1 + 0.49 (1.498 - 0.2) + 1.498^2 \right]$$

$$= 1.949$$

$$f_{cd} = \frac{250}{1.10 \times \left[1.949 + \left[1.949^2 + 1.498^2 \right]^{0.5} \right]}$$

$$= 73.590 \text{ MPa}$$

$$= 71.637 \text{ MPa}$$

$$\therefore P = f_{cd} \times A = 151.1475 \text{ kN}$$

Design: compression member using single unequal angle to carry factored compression of 120 kN, if C-C length of column is 8-m
if not state: let fixed end.

$$\text{no of bolt} \geq 2$$

Soln:-

$$P = 120 \text{ kN}$$

$$\text{area required} = \frac{P}{f_{cd}} = \frac{P}{(0.4 \text{ to } 0.6) f_y}$$

$$= \frac{120 \times 1000}{0.4 \times 250}$$

$$= 12 \text{ cm}^2$$

from Table: taking, section of unequal angle:

6.1

ISA: 89.0 x 60 x 10

load carrying capacity $\geq 120 \text{ kN}$

Then,

$$A = 14 \text{ cm}^2$$

$$r_w = 1.27 \text{ cm}$$

for both ends fixed:

$$k_1 = 0.20$$

$$k_2 = 0.35$$

$$k_3 = 2.0$$

$$\lambda_w = \frac{3.500}{1.27} \times \frac{1}{\sqrt{\frac{\pi^2 \times 2 \times 10^5}{250}}}$$
$$= 0.0031 \times 1000 = 3.104$$

$$\lambda_\phi = \frac{(90 + 60)}{2 \times 10} \times \frac{1}{\sqrt{\frac{\pi^2 \times 2 \times 10^5}{250}}}$$
$$= 0.084$$

$$\text{So, } \lambda_e = \sqrt{0.20 + 0.35 \times 3.104^2 + 2.0 \times 0.084^2}$$
$$= 1.925$$

so, buckling class = C, $\alpha = 0.49$

$$\therefore \phi = 0.5 [1 + 0.49(1.925 - 0.2) + 1.925^2]$$
$$= 2.776$$

$$\text{so, } f_{cd} = \frac{250}{110 \times [2.776(2.776^2 - 1.925^2)]^{0.5}}$$
$$= 47.585 \text{ N/mm}^2 \text{ (not OK)}$$

$$P = f_{cd} \times A = 66.619 \text{ kN} < 120 \text{ kN} \text{ not OK}$$

again, taking IS:

angle:

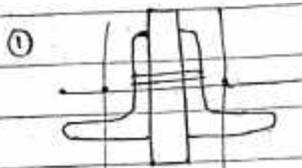
IS: 125 x 95 x 10



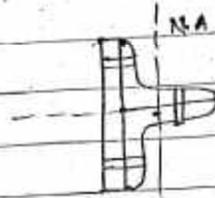
Angle section

Double angle section:

- ① Angle section connected to opposite side of gusset plate.
- ② " " " " " " " " on same " " " " " "



7.5.2.1



7.5.2.2

calculate load carrying capacity of two ISA 100x100x12 of unsupported length 4m, if angles are connected -

- ① on same sides of gusset plate of 16mm thick.
- ② on opposite " " " " " " " "

Solⁿ: for ISA 100x100x12

$$\text{Area} = 226 \text{ cm}^2$$

$$C_x = C_y = 2.92 \text{ cm}$$

$$r_x = 3.03 \text{ "}$$

$$r_y = 3.03 \text{ "}$$

$$r_{min} = 1.94 \text{ cm}$$

$$I_{xx} = I_{yy} = 207 \text{ cm}^4$$

Now,

$$\lambda_{uv} = \frac{l}{r_{uv}} = \frac{4000}{19.9}$$

$$E \sqrt{\frac{\pi^2 E}{250}}$$

$$1 \times \sqrt{\frac{\pi^2 \times 2 \times 10^5}{250}}$$

$$= 0.0023 \times 1000 = 2.3$$

$$\lambda_{\phi} = \frac{(b_1 + b_2)}{\alpha t \times E \sqrt{\frac{\pi^2 E}{250}}} = \frac{200}{2 \times 12 \times 1 \times \sqrt{\frac{\pi^2 \times 2 \times 10^5}{250}}}$$

$$= 0.0937$$

$$\lambda_e = \sqrt{k_1 + k_2 \lambda_{uv}^2 + k_3 \lambda_{\phi}^2} = \sqrt{0.20 + 0.35 \times 2.3^2 + 20 \times 0.0937^2} = 1.492$$

$$k_1 = 0.20$$

$$k_2 = 0.35$$

$$k_3 = 20$$

} for fixed end

for free

for built up member, buckling class = C

$$\text{so } \alpha = 0.49$$

so

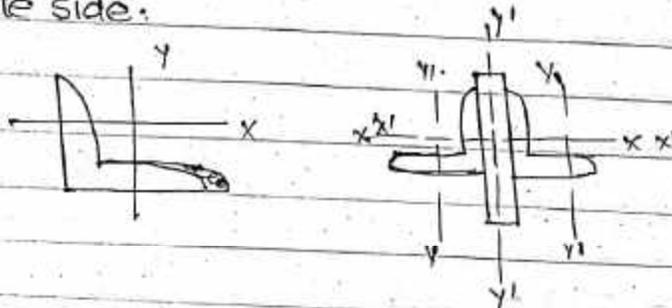
$$\phi = 0.5 \left[1 + 0.49(1.492 - 0.2) + 1.492^2 \right] \\ = 1.93$$

$$\text{so } f_{cd} = \frac{250}{1.10 \times [1.93 + (1.93^2 - 1.492^2)^{0.5}]} \\ = 72.05$$

$$\text{so, load carrying capacity} = f_{cd} \times A = 72.05 \times A \\ = 162.8 \text{ kN}$$

$$\text{Total load carrying capacity} = 2 \times 162.8 \\ = 325.6 \text{ kN}$$

Opposite side:



$$I_{x'x'} = 2 \times 207 = 414 \text{ cm}^4$$

$$I_{y'y'} = 2 \left[207 + 22.6 \times (2.92 + 1.6)^2 \right] \\ = 2 \left[I_{yy} + A \times \left(C_x + \frac{t}{2} \right)^2 \right]$$

$$= 1039.49 \text{ cm}^4$$

$$r_{x'} = \sqrt{\frac{414}{2 \times 22.6}} = 3.03 \text{ cm}$$

$$r_{y'} = \sqrt{\frac{1039.49}{2 \times 22.6}} = 4.796 \text{ cm}$$

Y axis wala measure jarikoi

$$L = L \text{ to gusset plate} = kly$$

$$L = l \text{ to } \dots = ky \quad kly$$

Now,

$$kly = 1 \times 4 = 4 \text{ m}$$

$$kly = 0.85 \times 4 = 3.4 \text{ m}$$

Then,

$$\lambda_x = \frac{kly}{r_x} = \frac{3.4 \times 100}{3.03} = 112.21$$

$$\lambda_y = \frac{400}{4.796} = 83.403$$

Now, buckling class is c

$$\alpha = 0.49$$

from table 9C

along x-axis

along y axis

110 94.6

120 83.7

$$\text{So, at } \lambda_x = 112.21$$

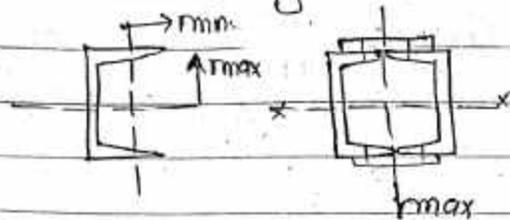
$$\therefore f_{cd} = 92.19$$

$$\begin{aligned} \therefore \text{load carrying capacity} &= f_{cd} \times A \\ &= 92.19 \times 22.6 \times 10^2 \\ &= 208.35 \text{ kN} \end{aligned}$$

$$\begin{aligned} \text{So, Total load carrying capacity} &= 2 \times 208.35 \\ &= 416.703 \text{ kN} \end{aligned}$$

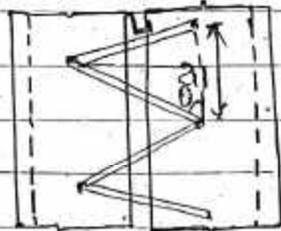
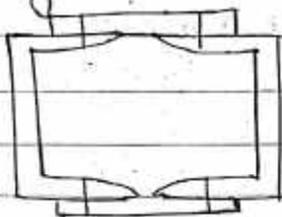
Built up column:

Two or more rolled section are connected together such that weaker axis becomes the stronger one & vice versa.

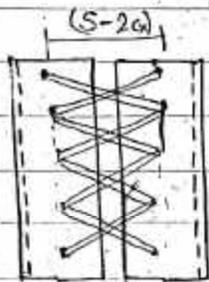


Lacing system: It is used to connect two section of built up column and carries shear developed due to lateral displacement caused by axial loading

loading



single lacing system



double lacing system

$$\sin \theta = \frac{S-2c_x}{L}$$

$$\therefore L = (S-2c_x) \csc \theta$$

$$\tan \theta = \frac{S-2c_x}{\left(\frac{a}{2}\right)}$$

$$\therefore a = 2(S-2c_x) \cot \theta$$

Design specification:

- # Lacing should be mirror image of one another on both sides of column.
- # effective slenderness ratio is taken as 1.05 times most critical slenderness ratio of column to consider shear deformation
- # width of lacing bar is taken as greater than 3 times nominal diameter of bolt used.
- # Thickness of lacing bar shouldn't be less than $\left(\frac{1}{40}\right)^{\text{th}}$ the length of lacing bar: in case of single lacing & $\left(\frac{1}{60}\right)^{\text{th}}$ in case of double lacing.

* Angle of inclination is taken betⁿ 40 to 70°.

(Transition of load is smooth)

* Spacing $[a]$ of lacing bar should be such that $\frac{a}{r_1} \leq 0.7 \times \text{critical slenderness ratio}$

$$\leq 50$$

r_1 - Individual radius of gyration

* Lacing should be able to carry 2.5% of axial load.
[Shear force = 2.5% of axial load] during buckling

* Slenderness ratio of lacing shouldn't be greater than 145.

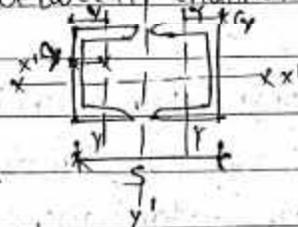
Design steps laced column:

1. Calculate required sectional area of column by,

$$A_{\text{req}} = \frac{P}{(0.4 + 0.6) f_y}$$

2. Select channel section such that $A \geq \frac{A_{\text{req}}}{2}$

3. Calculating spacing between channel section such that: $I_{y'y'} \geq I_{x'x'}$



$$2 [I_{xx} + A \times (s/2 - r_x)^2] \geq 2 I_{xx}$$

4. Check load carrying capacity of column.

5. adopt angle of inclination

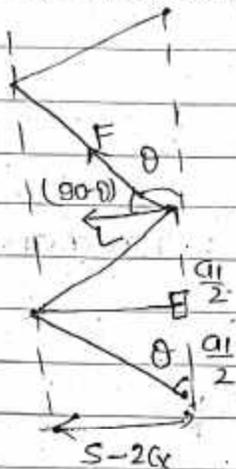
6. Calculate length of lacing & spacing of lacing & also check for spacing of lacing, $\left[\frac{a}{r_1} \right]$ criteria



7. Calculate width and thickness of lacing bar.
8. Calculate load carrying by lacing bar.
9. Check for compressive strength of "
10. Check for Tensile strength of "
11. connection design.
12. Design of tie plate.

Calculation of shear force:

$$V = 2.5\% \text{ of axial load}$$

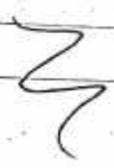


$$F \cos(90 - \theta) = \frac{V}{2}$$

$$\therefore F = \frac{V}{2 \sin \theta}$$

for double lacing

$$F = \frac{V}{4 \sin \theta}$$



Design builtup column of 7m unsupported length carrying factored axial load of 1500 kN also design lacing system to connect two channels back to back using bolted connection.

Soln:

Step 1:

$$\text{Area} = \frac{P}{0.6fy} = \frac{1500 \times 10^3}{0.6 \times 250} = 10,000 \text{ mm}^2$$

Step 2: Select channel section such that

$$A \geq \frac{\text{Area}}{2} = 5000 \text{ mm}^2$$

individual channel

from GA, taking

MCP 300 @ 46 kg/m (stopping flange channel)

$$\text{SO, } A = 58.8 \text{ cm}^2$$

Step 2 contd: $D = h = 300 \text{ mm}$

$$B = b_f = 94 \text{ mm}$$

$$t_f = T = 13.6 \text{ mm}$$

$$t = t_w = 12 \text{ mm}$$

$$r_x = 11.2 \text{ cm}$$

$$r_y = 2.68 \text{ cm} \text{ \& } 2.52 \text{ cm}$$

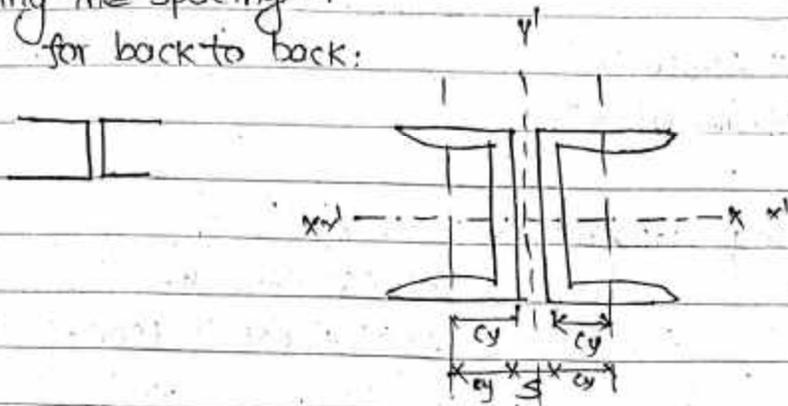
$$I_{xx} = 7370 \text{ cm}^4$$

$$I_{yy} = 424 \text{ cm}^4$$

$$A = 58.8 \text{ cm}^2$$

$$C_y = 2.22 \text{ cm} = 2.22 \text{ cm}$$

Step: 3, finding the spacing:
for back to back:



$$I_{y'y'} \geq I_{x'x'}$$

$$\sqrt{[I_{yy} + A x^2]} > \sqrt{[I_{xx} + A x'^2]}$$

or $37500 + 5850 \times \frac{(S+2cy)^2}{2} > 7350 \times 10^4$

$$h_{y'} = (S + 2cy)$$

$$\text{or } \frac{(S + 2cy)^2}{2} \geq \frac{0.335 \times 6975 \times 10^4}{5850}$$

$$\text{or } S > 173.243 \text{ mm}$$

$$\therefore S = 180 \text{ mm}$$

Step: 4:

$$\lambda = \frac{KL}{r_{\min}} = \frac{0.65 \times 7000}{r_x}$$

$$\lambda_{\text{actual}} = 40.625$$

$$\lambda_{\text{design}} = 1.05 \times 40.625$$

$$= 42.656$$

For built up section, buckling class is C

$$\therefore \alpha = 0.49$$

Step 5: adopt angle of inclination: $\theta = 60^\circ$

7 ~~Step~~ from table 9(c)

f_d for $\lambda = 42.656$

$$\therefore f_d = 194.016 \text{ N/mm}^2$$

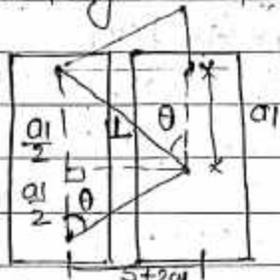
10

$$\text{load carrying capacity} = f_d \times A$$

$$= 194.016 \times 58.8 \times 10^2$$

$$= 2231.63 \text{ kN} > 1500 \text{ kN OK!}$$

Step: 6 calculate length & spacing of lacing:



$$\text{Now, } \tan \theta = \frac{s+2c}{a_1/2}$$

$$\therefore a_1 = \frac{2(s+2c)}{\tan \theta}$$

$$= 279.97 \text{ mm}$$

$$\text{So, } \sin \theta = \frac{s+2c}{L}$$

$$L = 279.97 \text{ mm}, 259.11 \text{ mm}$$

$$\text{also, } \frac{a_1}{r_1} = \frac{279.11}{25.2} = 10.289 \leq 50$$

$$\leq 0.7 \times 42.65 = 29.855$$

7: Calculate width & thickness of lacing bar:

adopt M20 bolts of Pr. cl. 4.6

$$\text{so, } f_{ub} = 400 \text{ Mpa}$$

$$f_{yb} = 240 \text{ Mpa}$$

$$\begin{aligned} \text{width of lacing bar} &\geq 3d = 3 \times 20 \\ &= 60 \text{ mm} \\ &\approx 80 \text{ mm} \end{aligned}$$

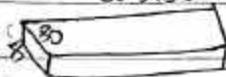
$$\text{thickness} = \frac{1}{40} \times l$$

$$= \frac{259.11}{40}$$

$$= 6.5 \text{ mm}$$

$$\approx 8 \text{ mm}$$

adopt lacing bar of 80 x 8 mm.



for single lacing $l_{eff} = l = 80 \text{ mm}$

$$I_{min} = \frac{bd^3}{12} = \frac{80 \times 8^3}{12} = 3413.33$$

$$\begin{aligned} r_{min} &= \sqrt{\frac{I_{min}}{A}} = \sqrt{\frac{6t^3}{12bt}} = \frac{t}{\sqrt{12}} \\ &= \frac{8}{\sqrt{12}} = 2.31 \text{ mm} \end{aligned}$$

$$\begin{aligned} \lambda &= \frac{KL}{r_{min}} = \frac{1 \times 259.11}{2.31} \\ &= 112.19 \text{ mm} < 145 \text{ mm OK!} \end{aligned}$$

Step: 8:

$$V = 2.5\% \text{ of axial load}$$

$$= \frac{2.5}{100} \times 1500$$

$$= 37.5 \text{ kN}$$

$$F = \frac{V}{2 \sin \theta} = \frac{37.5}{2 \times \frac{\sqrt{3}}{2}}$$

$$= 21.65 \text{ kN}$$

Step: 9 From table 9C (Page 94 and Table 10]

2nd last solid bar

buckling class c

$$\alpha = 0.49$$

$$\lambda = 112.2$$

$$\therefore f_{cd} = 92.202 \text{ N/mm}^2$$

$$\therefore \text{load carrying} = 92.202 \times 80 \times 8$$

$$\text{capacity} = 59.00 \text{ kN} > 21.65 \text{ kN (OK!)}$$

Step: 10: check tensile strength of bar.

$$\text{yielding } T_{dg} = \frac{A_s f_y}{\gamma_{m0}} = \frac{80 \times 8 \times 250}{1.10}$$

$$= 145.45 \text{ kN} > 26.15 \text{ kN. OK!}$$

Step 11:- for M20 bolt of pr. cl 4.6

$$n_n = 1$$

$$V_{dsb} = \frac{450 \times 0.78 \times 1 \times 20^2}{\sqrt{3} \times 1.25 \times 4}$$

$$= 45.27 \text{ kN}$$

यति मात्र जरैनी बुझ

Bearing capacity :- $V_{dpb} = \frac{2.5 K_b d l (f_u / f_{ub})}{1.25}$

assume $K_b = 0.5$

$$= \frac{2.5 \times 0.5 \times 20 \times 8 \times 400}{1.25}$$

$$= 64 \text{ kN}$$

So, Bolt value = 45.27 kN

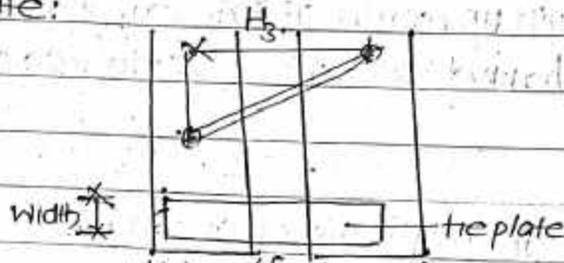
So no of bolt = $\frac{\text{load}}{\text{Bolt value}}$

$$= \frac{21.65}{45.27}$$

$$= 0.478 \approx 1$$

Provide 1 M20 bolt of grade 4.6 for lacing bar:

Step: 12 Design of tie plate:



width of tie plate $\geq (S + 2c_y)$

$$\geq 224.8$$

$$\approx 230 \text{ mm}$$

thickness $\geq \frac{1}{50} \times (S + 2c_y)$

$$\geq \frac{224.8}{50}$$

$$\geq 4.5 \text{ mm}$$

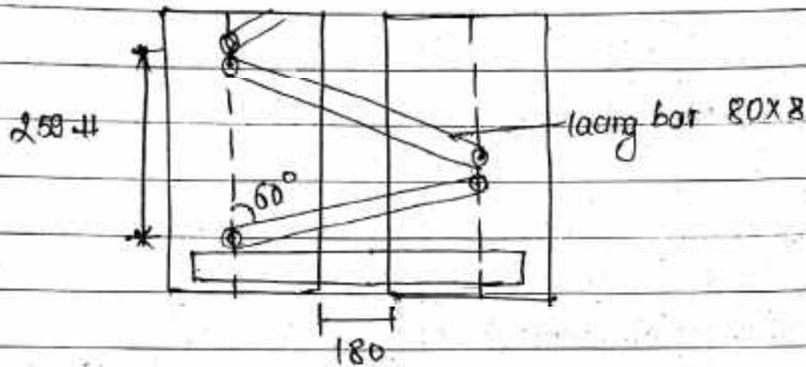
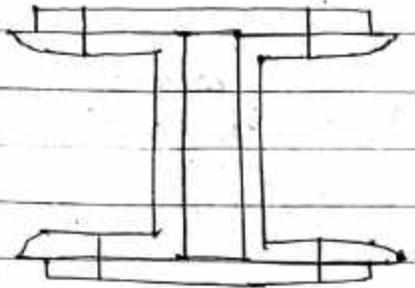
$$\geq 8 \text{ mm}$$

total length = $S + 2 \times B$

$$= 180 + 2 \times 94$$

$$= 368 \text{ mm}$$

provide tie plate of length 360 x 230 x 8 mm, 4/4 mm gap between ends



Design a built up column of 10m carrying factored load of 1000kN, using two channel section face to face or toe to toe.

Soln:-

Step 1 Calculate area required of column,

$$\therefore \text{Area} = \frac{P}{0.6fy} = \frac{1000 \times 10^3}{0.6 \times 250} = 6666.67 \text{ mm}^2$$

step: 2. select channel section such that,

$$\begin{aligned} A &\geq \frac{\text{Area}}{2} \text{ of individual channel} \\ &\geq \frac{6666.67}{2} \\ &\geq 3333.33 \text{ mm}^2 \\ A &\geq 3333 \text{ cm}^2 \end{aligned}$$

from table 6A, taking sloping flange channel

MC. 225 @ 30.7 kg/m

$$A = 39 \text{ cm}^2$$

$$I_{yy} = 219 \text{ cm}^4$$

$$D = 225 \text{ mm}$$

$$r_x = 8.71 \text{ cm}$$

$$B = 82 \text{ mm}$$

$$r_y = 2.37 \text{ cm}$$

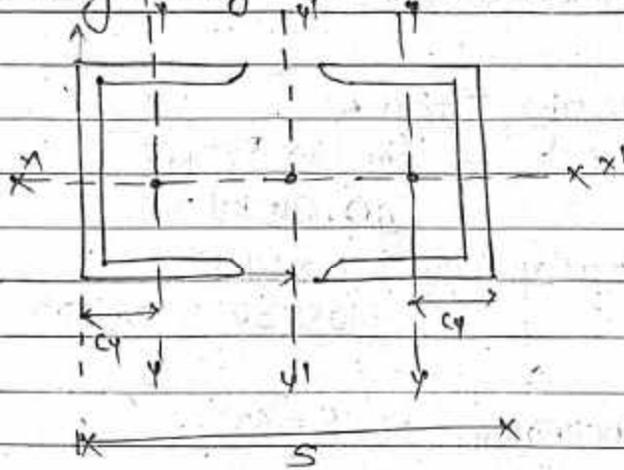
$$t_w = 9 \text{ mm}$$

$$I_f = 12.4 \text{ mm}^4$$

$$c_y = 2.22 \text{ cm}$$

$$I_{xx} = 2960 \text{ cm}^4$$

Step: 3 calculating spacing for toe to toe connection



$$I_{yy} \geq I_{xx'}$$

$$2 [I_{yy} + A \left(\frac{S}{2} - c_y \right)^2] \geq 2 [I_{xx} + A r^2]$$

$$\text{or, } 2 [219 \times 10^4 + 3939 \left(\frac{S}{2} - 2.22 \right)^2] \geq 2 [2960 \times 10^4]$$

$$\text{or, } 3900 \left(\frac{S}{2} - 2.22 \right)^2 \geq 2741 \times 10^4$$

$$\text{or, } \left(\frac{S}{2} - 2.22 \right)^2 \geq 7028.20$$

$$\text{or, } \frac{S}{2} \geq (83.83 + 2.22)$$

$$\therefore S \geq 2 \times 86.05 \text{ mm}$$

$$\text{take } S = 180 \text{ mm} > 172.06 \text{ mm}$$

$$= 220 \text{ mm}$$

Step 4 calculate slenderness ratio & load carrying capacity

$$\lambda = \frac{KL}{r_{\min}} = \frac{0.65 \times 10000}{87.1}$$

$$= 74.62$$

$$\lambda_{\text{design}} = 1.05 \times \lambda_{\text{actual}}$$

$$= 78.358$$

for built up section buckling class = C
 $\alpha = 0.49$

from table 9C

70	152
80	136

for $\lambda = 78.358$

$$f_{cd} = 138.627 \text{ N/mm}^2$$

so, load carrying capacity = $f_{cd} \times A$

$$= 138.627 \times 39 \times 10^2$$

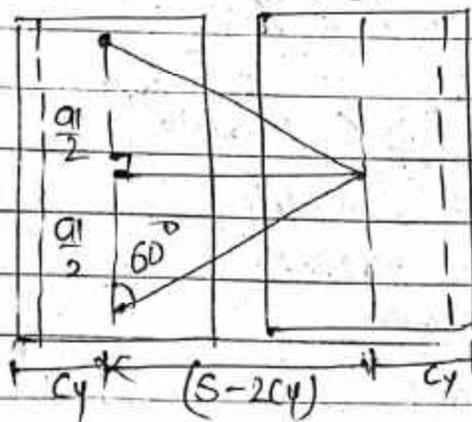
$$= 540.645 \text{ kN}$$

Total load carrying capacity = 2×540.645

$$= 1081.30 \text{ kN} > 1000 \text{ kN (OK!)}$$

Step 5: let, angle of inclination be $\theta = 60^\circ$

Step 6 calculate length & spacing of lacing



$$a_1 = \frac{2(S - 2c_y)}{\tan \theta} = 202.72 \text{ mm}$$

$$l = \frac{(S - 2c_y)}{\sin \theta} = 202.72 \text{ mm}$$

Check: $\frac{a_1}{r} = \frac{202.72}{23.7} = 8.55 \leq 50$

$$\leq 0.7 \times \lambda_d$$

Step: 7 width & thickness of lacing bar:

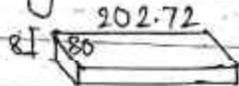
adopt M20 bolt of prci 4.6

or, we can adopt any width of lacing bar

$$\text{width of lacing bar} \geq 3d = 3 \times 20 = 60 \text{ mm} \\ \approx 80 \text{ mm}$$

$$\text{thickness } (t) = \frac{l}{40} \times l = \frac{202.72}{40} \\ = 5.068 \\ \approx 8 \text{ mm}$$

adopt lacing bar of 20x8 mm



for double lacing:

$$t = \left(\frac{l}{60}\right)$$

$$\text{lacing length} = l_{\text{eff}} = 0.7 l$$

$$F = \frac{V}{4 \sin \theta}$$

for single lacing $l = l_{\text{eff}} = 202.72 \text{ mm}$

$$r_{\text{min}} = \frac{t}{\sqrt{12}} = \frac{8}{\sqrt{12}} = 2.31 \text{ mm}$$

$$\lambda = \frac{KL}{r_{\text{min}}} = \frac{1 \times 202.72}{2.31}$$

Step: 8

$$= 87.75 < 145 \text{ OK!}$$

so, f_{cd} for $\lambda = 87.75$ can be calculated such that

for solid section buckling class C

\therefore table 9C gives

$$f_{cd} = 124.375 \text{ N/mm}^2$$

136

121

Step: 9

$$V = 2.5\% \text{ of axial load} = \frac{2.5}{100} \times 1000 \\ = 25 \text{ kN}$$

$$F = \frac{V}{2 \sin \theta} = 14.43 \text{ kN}$$

$$\text{load carrying capacity of lacing bar} = 124.375 \times 80 \times 8 = 79.6 \text{ kN} \\ > 14.43 \text{ kN}$$

Front to front - connection → for stress distⁿ

Step 10: Tensile strength:

Yielding strength $T_d = \frac{A_g f_y}{1.10} = \frac{80 \times 8 \times 250}{1.10}$
 $= 145.25 > 19.43 \text{ kN OK!}$

Step 11: for M20 bolt prcl. 4.6

$$V_{dsb} = \frac{400 \times 0.787 \times 20^2}{\sqrt{3} \times 1.25 \times 9}$$

$$= 45.27 \text{ kN}$$

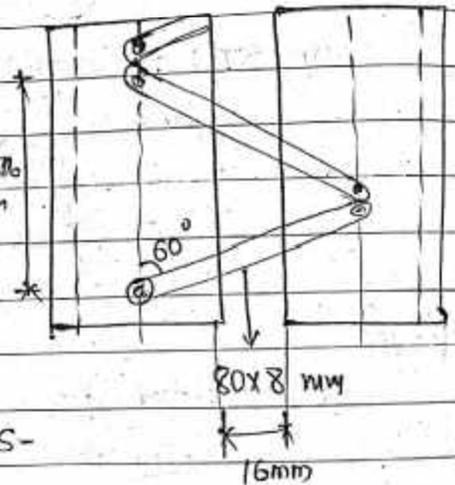
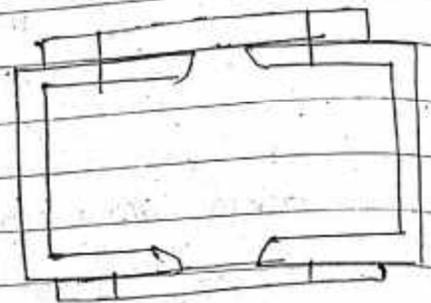
Step 12: assume $k_b = 0.5$

$$V_{dpb} = \frac{2.5 \times 0.5 \times 20 \times 8 \times 400}{1.25}$$

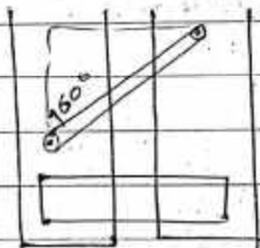
$$= 64 \text{ kN}$$

So Bolt Value = 45.27 kN

$$\text{no of bolt} = \frac{19.43}{45.27} = 0.318 \approx 1 \text{ bolt}$$



Design of tie plate:



width of tie plate $\geq s$

180-2122

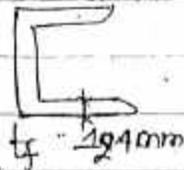
180

164

for weld:

Step 11: welding

size of weld:



$$S_{max} = t_{min} - 1.5 \\ = 8 - 1.5 = 6.5 \text{ mm}$$

lacing thickness = 8 mm

$$S_{min} = 5 \text{ mm}$$

so, adopt, $S = 6 \text{ mm}$

and

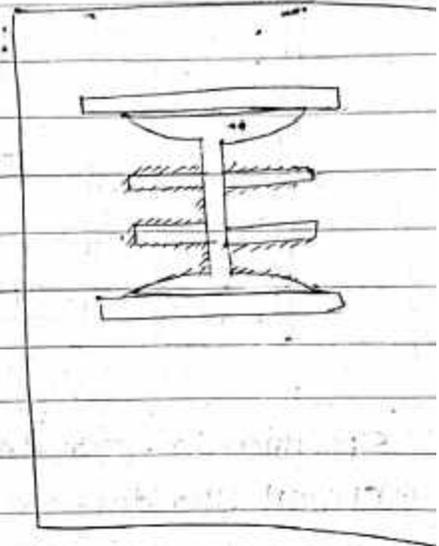
$$t_e = 0.7 S$$

$$= 4.2 \text{ mm}$$

Then,

$$f_{wd} = \frac{f_u}{\sqrt{3} \times 1.25}$$

$$= \frac{480}{\sqrt{3} \times 1.25} = 189.37 \text{ MPa}$$

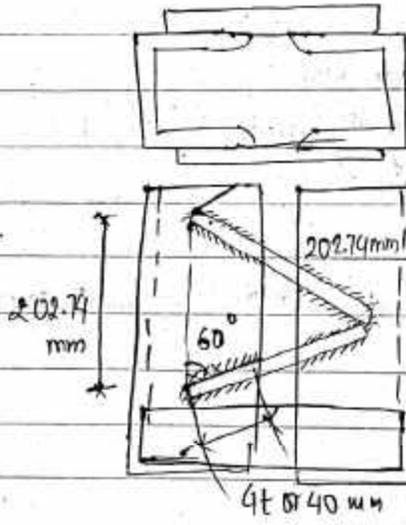


P. load carrying capacity) = $f_{wd} \times l_e \times t_e$

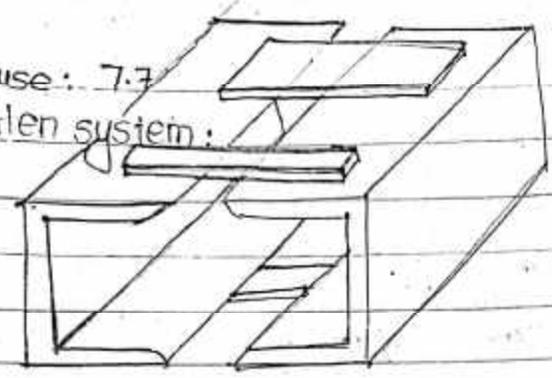
$$14.43 \times 10^3 = 189.37 \times l_e \times 4.2$$

$$\therefore l_e = 18.19 \text{ mm}$$

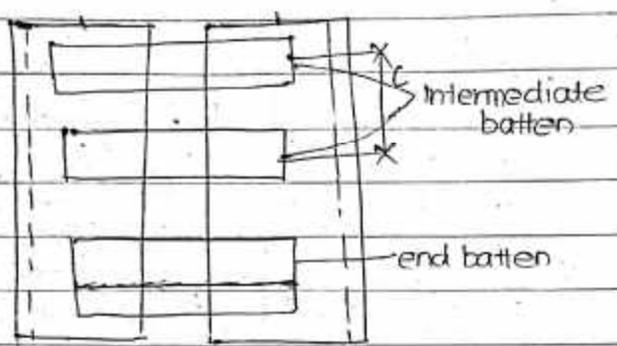
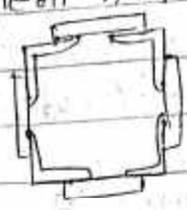
so provide l_e as per required,



clause: 7.7
Batten system:



angle $n=4$



Specification for design

① Critical slenderness ratio is multiplied by 1.1 to obtain design slenderness ratio to consider shear deformation

② Spacing of batten should be such that c should be less than $0.7 \times$ critical slenderness ratio. and ≤ 50

③ Size of batten is determined by shear force and Bending moment acting on batten and given by-

$$V_b = \frac{V_t c}{NS}$$

V_t - transverse shear force
 c - c-c distance betⁿ batten

$$M = \frac{V_t c}{2N}$$

$$S = (S' \pm 2c_y) = (S' \pm 2c_y)$$

S' - spacing

④ width of batten should not be less than c-c distance betⁿ connection on batten:

$$\text{width} \geq (S' - 2c_y)$$

$$\text{thickness} \geq \frac{1}{50} (S' - 2c_y)$$

Width of intermediate batten $= (3/4)^{1/3}$ of end batten.

Step: 4 same same:

Design a builtup column of span of 9m length with both hinged and carrying an axial load of 900kN. Builtup column should consists 2 channel section connected front-to-front using batten system:

Soln:

Step 1: Calculate the area required

$$\begin{aligned} \text{Area} &= \frac{\text{factored load}}{0.6 f_{yp}} \\ &= \frac{1.5 \times 900 \times 1000}{0.6 \times 250} \\ &= 9000 \text{ mm}^2 \end{aligned}$$

Step 2 Selection of channel section such that

$$\begin{aligned} A &\geq \frac{\text{Area}}{2} \\ &\geq \frac{9000}{2} \\ &\geq 4500 \text{ mm}^2 \\ &\geq 45 \text{ cm}^2 \end{aligned}$$

take MC300 @ 46.2 kg/m

$$A = 58.8 \text{ cm}^2$$

$$D = 300 \text{ mm}$$

$$t_{fb} = 13.6 \text{ mm}$$

$$t_w = 12 \text{ mm}$$

$$B = 94 \text{ mm}$$

$$r_x = 11.2 \text{ cm}$$

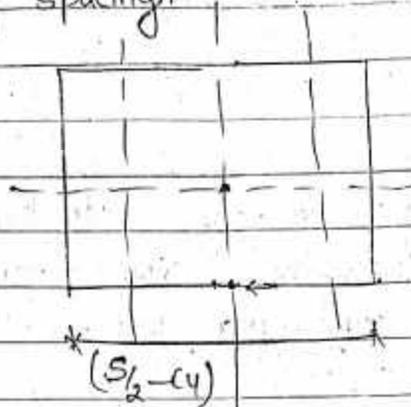
$$r_y = 2.52 \text{ cm}$$

$$I_{xx} = 7350 \text{ cm}^4$$

$$I_{yy} = 375 \text{ cm}^4$$

$$L_y = 2.22 \text{ cm}$$

step: 3 finding spacing:



$$I_{yy'} \geq I_{xx'}$$

$$2 [I_{yy} + A x (S/2 - cy)^2] \geq 2 [I_{xx} + D]$$

$$\text{or, } 375 \times 10^4 + 58.8 \times 100 (S/2 - 22.2)^2 \geq 7350 \times 10^4$$

$$\text{or } (S/2 - 22.2)^2 \geq 11862.25$$

$$\text{or } S/2 - 22.2 \geq 108.91$$

$$\text{or, } S \geq 262.22$$

$$\therefore S = 270 \text{ mm}$$

[required Area 0.6 of JGJ

step: 4 calculate slenderness ratio

Area available at JGJ

max area

$$\begin{aligned} \lambda_{\text{actual}} &= \frac{KL}{r_{\text{min}}} = \frac{KL}{r_x} \\ &= \frac{L \times 9000}{112} \\ &= 80.357 \end{aligned}$$

136

121

$$\begin{aligned} \lambda_{\text{design}} &= 1.1 \times \lambda_{\text{actual}} \\ &= 88.393 \end{aligned}$$

for $\lambda = 88.393$ & builtup section buckling class = C
table 9c

$$f_{cd} = 123.41 \text{ MPa}$$

$$\begin{aligned}\therefore \text{load carrying capacity} &= f_c \times A \\ &= 123.41 \times 58.8 \times 10^2 \\ &= 725.65 \text{ kN}\end{aligned}$$

$$\begin{aligned}\text{Total load carrying capacity} &= 2 \times 725.65 \\ &= 1451.3 \text{ kN} > 900 \text{ kN} \quad (\text{OK!})\end{aligned}$$

Batten system:

Spacing of batten can be calculated as

$$\frac{c}{r_y} \leq 0.7 \times \text{slenderness ratio}$$

$$\frac{c}{2.52} \leq 0.7 \times 88.392$$

$$\therefore \frac{c}{2.52} \leq 50$$

$$\therefore c \leq 1260 \text{ mm}$$

adopt $c = 1000 \text{ mm}$

Now,

shear force on batten (V) = 2.5% of Axial load

$$= \frac{2.5}{100} \times 1350$$

$$V = 33.75 \text{ kN}$$

$n = 2$ (no. of shear plane)

$$\therefore S = s' - 2cy$$

$$= 270 - 2 \times 22.2$$

$$= 225.6 \text{ mm}$$

$$\text{So, shear force on batten} = \frac{VC}{nS} = \frac{33.75 \times 1000}{2 \times 225.6}$$

$$= 74.8 \text{ kN}$$

$$\text{Moment on batten} = \frac{VC}{2n} = \frac{33.75 \times 1000}{2 \times 2}$$

$$= 8437.5 \text{ kNm}$$

Size of end batten:

Depth of end batten $\geq S$

$$\geq 225.6$$

$$\approx 230 \text{ mm}$$

length of batten = 250 (Just less than s')

$$\text{thickness} \geq \frac{1}{50} \times S = \frac{1}{50} \times 225.6$$

$$= 4.512 \text{ mm}$$

$$\approx 8 \text{ mm}$$

adopt 250x230x8 mm of batten.

for intermediate batten:

$$\text{depth of intermediate batten} = \frac{3}{4} \times \text{depth of Batten.}$$

$$= \frac{3}{4} \times 230$$

$$= 172.5 \text{ mm}$$

$$\approx 180 \text{ mm}$$

adopt: 250x180x8 mm intermediate batten.

check size of batten

pag. 59, 8.4; Shear:

$$\text{Shear stress on batten} = \frac{V}{180 \times 8} = \frac{74.8 \times 10^3}{180 \times 8} \leq \frac{f_y}{\sqrt{3} \gamma_{m0}}$$

$$= 51.94 \text{ N/mm}^2 \leq \frac{250}{\sqrt{3} \times 1.10}$$

$$= 51.94 \text{ N/mm}^2 \leq 131.2 \text{ N/mm}^2 \quad (\text{OK!})$$

Page: 53. 8.2.1.2

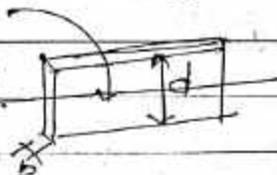
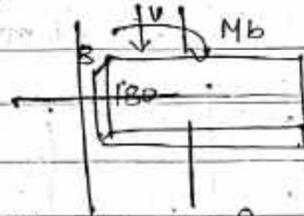
$$\text{designed bending stress} - \frac{M}{Z} \leq \frac{f_y}{\gamma_{m0}}$$

$$= \frac{8437.52}{\left(\frac{8 \times 180^2}{6}\right)} \leq \frac{250}{1.10} \quad z = \frac{bd^2}{6} = \frac{8 \times 180^2}{6}$$

$$= 195.3 \leq 227.27$$

MPa

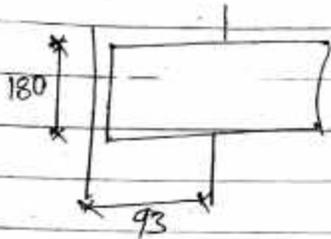
OK!



(+)

Bolted connection:

adopt M20 bolt of pr. ci 4.6 with single line of bolt



$$\text{no. of bolt} = \sqrt{\frac{6Pe}{m p V d_{sb}}}$$

for M20 bolt, pr. ci =

$$V d_{sb} = 48.977 \text{ kN}$$

$$m = 1$$

$$p = 60 \text{ mm} > 2.5 \times 20 = 50 \text{ mm}, e = 1.7 d_0$$

$$\therefore n = \sqrt{\frac{6 \times 8437.5 \times 10^3}{1 \times 60 \times 48.977 \times 10^3}} = 1.7 \times 22 = 33 \times 40 \text{ mm}$$

$$= 4.32$$

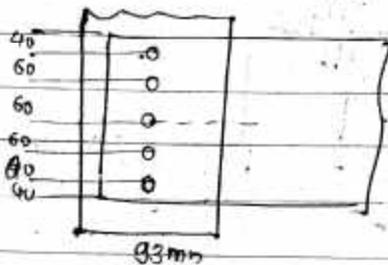
$$\approx 5$$

Since, 5 bolts can't accommodate on depth of 180 mm of batten so increase the size of batten as;

$$\text{depth} = 60 \times 4 + 40 \times 2$$

$$= 240 + 80$$

$$= 320 \text{ mm}$$



Then,

$$\sum n_i^2 = 60^2 \times 2 + 120^2 \times 2 = 36000$$

$$r_{\text{max}} = 120 \text{ mm}$$

$$(\sigma_{\text{max}}^v) = \frac{V_b}{N} = \frac{174.8}{5} = 14.96 \text{ kN}$$

$$\begin{aligned} \text{Torsional force} &= \frac{M \cdot r_{\text{max}}}{\sum n_i^2} \\ &= \frac{8457.5 \times 10^3 \times 120}{36000} \\ &= 28.125 \text{ kN} \end{aligned}$$

$$\therefore R = \sqrt{14.96^2 + 28.125^2} \leq \text{Bolt value} = 31.85 \text{ kN}$$

$$\text{Bearing capacity (vdpb)} = \frac{2.5 k_b d t (f_u / f_u b)}{\gamma_{mb}}$$

$$= \frac{2.5 \times 0.606 \times 20 \times 8 \times 400}{1.25} = 97.568 \text{ kN}$$

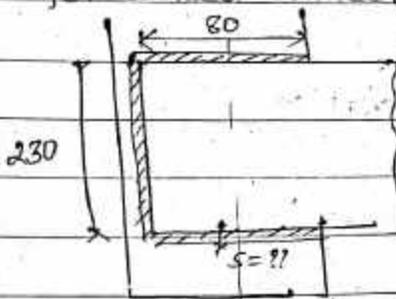
$$k_b \rightarrow \frac{P}{3d_0} = \frac{P}{3d_0} = 0.25, \downarrow, \frac{400}{410}$$

$$0.606, \downarrow, 0.973$$

$$\therefore \text{Bolt value} = 45.27 \text{ kN}$$

$$\text{So, } R = 31.85 \text{ kN} \leq 45.27 \text{ kN OK!}$$

for welded connection: (H.W)

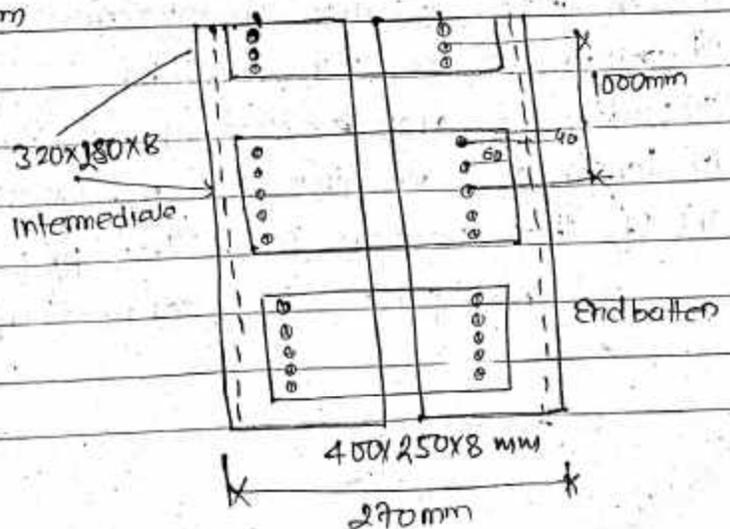
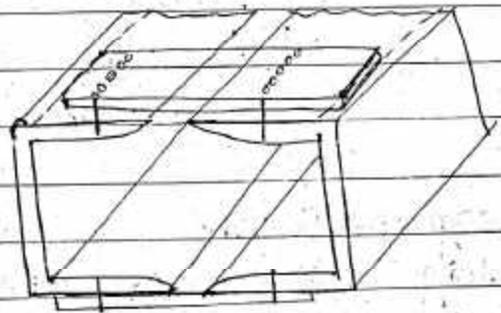


End batten

$$\text{depth of end batten} = \frac{4}{3} \times 320$$

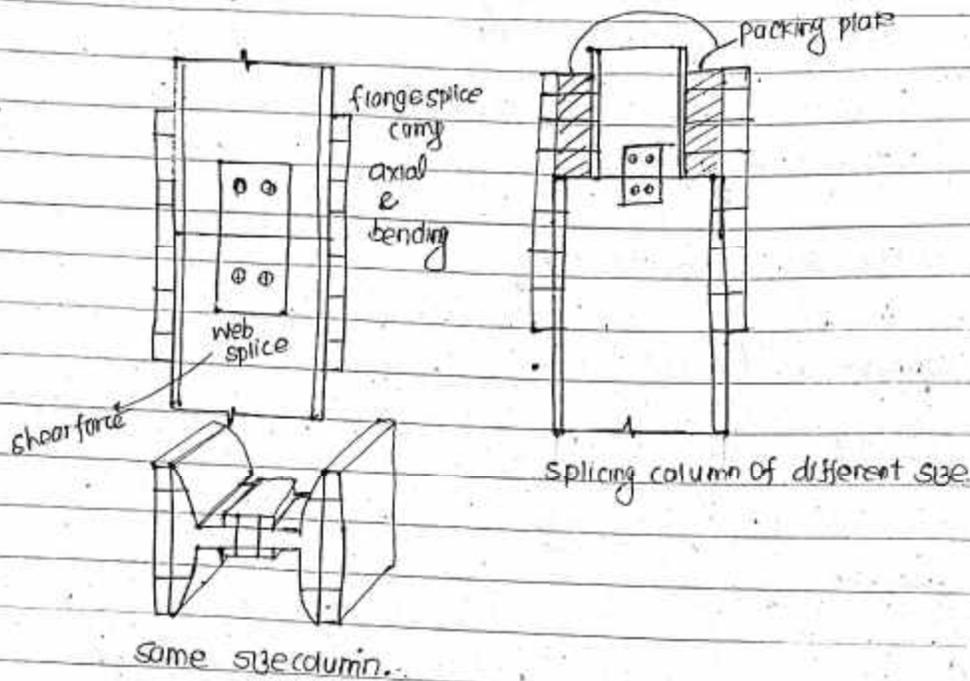
$$= 426.67 \text{ mm}$$

$$\approx 450 \text{ mm}$$



Column splice :-

In case of tall building when two section of column are to be connected or in case of change in size column should be properly connected to facilitate the smooth transfer of load from upper to lower section. Such arrangement is column splice:



Design specification:

- (i) flange splice carries axial force and bending moment carried by column.
- (ii) web splice carries shear force carried by column.
- (iii) splice acts as a short column of '0' slenderness ratio.
- (iv) width of flange splice should be equal to width of flange of column.
- (v) length of splice is determined by no. of bolts required.
- (vi) if the section is milled (properly) only 50% of load is to be transferred by splice & its connection.

Design splice (column) to connect two ~~col~~ SC 220 carrying axial load of 500 kN (factored load) and Bending moment of 40 kN-m along with shear force of 50 kN.

Solⁿ: Assuming properly milled section so only 50% of axial load is to be transferred by splice and its connection.

a) flang splice.

$$\begin{aligned} \text{load on each flange splice} &= \frac{(50\% \text{ of } 500)}{2} \\ &= \frac{250}{2} \\ &= 125 \text{ kN/splice} \end{aligned}$$

Section property for SC 220

$$A = 89.8 \text{ cm}^2$$

$$D = 220 \text{ mm}$$

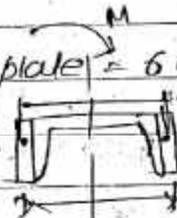
$$B = 220 \text{ mm}$$

$$b_w = 9.5 \text{ mm}$$

$$t_f = 16 \text{ mm}$$

assume the thickness of flange plate = 6 mm

So, axial load on splice due to Bending moment = M



$$\begin{aligned} \text{Lever arm} &= \frac{40 \times 10^3}{\left(220 + \frac{6}{2} + \frac{6}{2}\right)} \\ &= \frac{40 \times 10^3}{226} \\ &= 176.99 \text{ kN} \end{aligned}$$

$$\begin{aligned} \text{Total load on each flange splice} &= 125 + 177 \\ &= 302 \text{ kN} \end{aligned}$$

for short column:-

$$f_{cd} = \frac{f_y}{\gamma_{mo}} = \frac{250}{1.10} = 227.27 \text{ Mpa}$$

$$\begin{aligned} \text{Now, load coming by flange splice} &= f_{cd} \times \text{Area} \\ &= 227.27 \times 220 \times t \\ &= 499.99 t \times 10^3 \end{aligned}$$

$$\text{so } 220 \times t \times 227.27 > \text{total load}$$

$$t > \frac{301.99}{220 \times 227.27}$$

$$t > 6.04$$

$$t > 6.04$$

take, $t \approx 8 \text{ mm}$

adopt M20 bolt of pr.ci. 4.6

$$V_{dsb} = 45.27 \text{ kN}$$

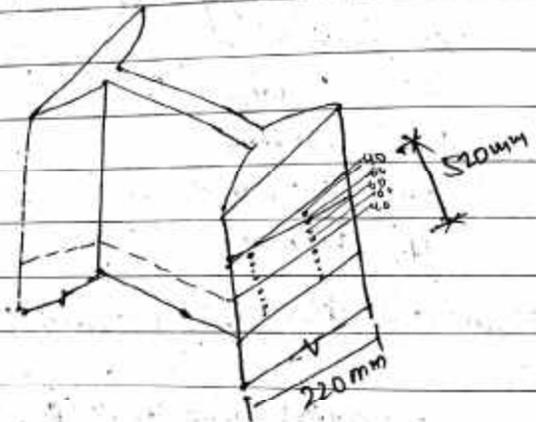
$$b = 60 \text{ mm}$$

$$e = 40 \text{ mm}$$

$$\begin{aligned} \text{No. of bolts} &= \frac{\text{total load}}{\text{bolt value}} \\ &= \frac{302}{45.27} \end{aligned}$$

$$= 6.67 \text{ nos}$$

≈ 8 bolts.



$$\text{total length of flange plate} = 2(2 \times 40 + 3 \times 60)$$

$$= 2[80 + 180]$$

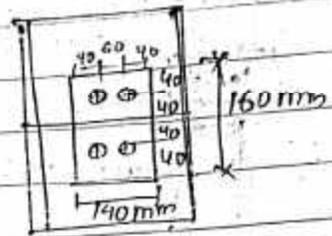
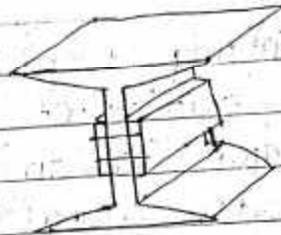
$$= 520 \text{ mm}$$

so, provide a plate of $520 \times 220 \times 8 \text{ mm}$
(flange splice)

Web splice :

Shear force = 50 kN

for M20 bolt of pr. cl. 4.6



Shear capacity of bolt (V_{dsb}) = 2×45.23 if $n_s = 2$
 = 90.54 kN

no of bolt = $\frac{50}{90.54} = 0.55$
 ≈ 2 bolts / column

length of web splice = $4 \times 40 = 160$ mm

width of " " = $2 \times 40 + 1 \times 60$
 = 140 mm

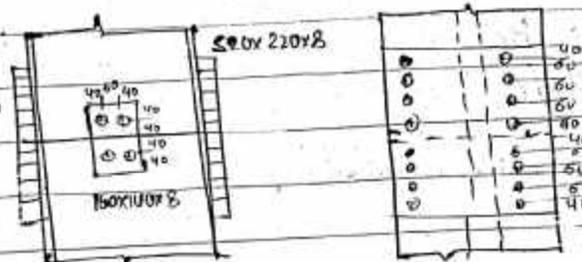
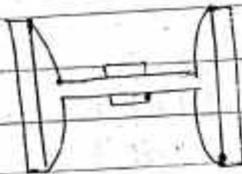
for thickness

$V = \frac{f_y A_v}{\sqrt{3} \times \gamma_{m0}}$

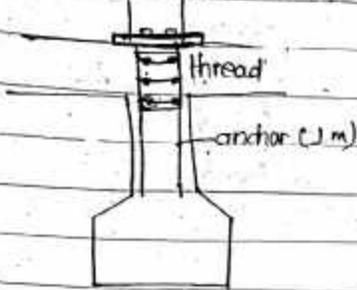
$50 \times 10^3 = \frac{250 \times 140 \times t}{\sqrt{3} \times 1.1}$

$\therefore t = 2.72$ mm
 ≈ 6 mm

So adopt a web splice of 160x140x6 mm



Column base:



Stability of structure is determined by strength & stability of column base.

Major function of column base is to transfer load to footing (footing pedestal) and distribute load in column such that it doesn't exceed bearing capacity of structure underneath.

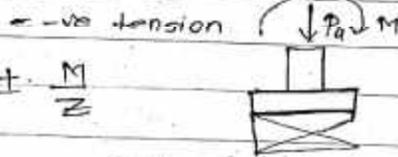
Depending upon load on column, there are two types of column bases:

- Slab base
- Gusseted plate base

a) slab base: if the load in column is moderate or small axial load along with very small bending moment, in such case slab base is suitable. In such case column base is entirely under compression.

compression = +ve

$$\sigma = \frac{P}{A} \pm \frac{M}{Z}$$



Design steps:

1. calculate bearing capacity of concrete.

$$\text{Bearing capacity} = 0.45 f_{ck} \quad [\text{LSM}]$$
$$= 0.25 f_{ck} \quad (\text{WSM})$$

2. Calculate area required;

$$\text{Area} = \frac{P_u}{0.45 f_{ck}}$$

3. Calculate length & breadth of column bases

$$l = B = \sqrt{A}$$

4: Calculate pressure underneath column base

$$w = \frac{P}{\text{Area}} \pm \frac{M}{Z}$$

5. calculate thickness of slab base 'd_s'

$$t_s = \sqrt{\frac{0.5W(a^2 - 0.3b^2)}{f_y}} > t_f$$

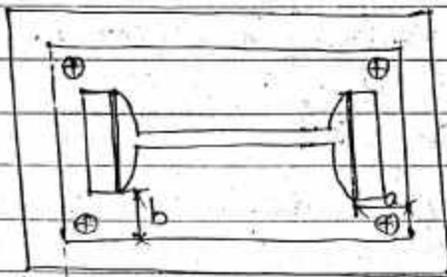
Page:- 7.4.3 (slab base)

Page: 46

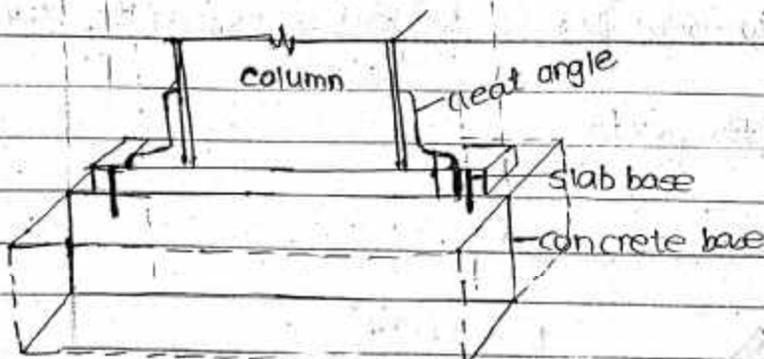
6: connection design:- जॉइंट प्लेट

एक Moment और Tension developed प्लेट को design करें

- Provide four M20 bolts (anchored) of min. anchored length 300mm
- Provide cleat angle of 65x65x6 mm or 150x110x16 mm



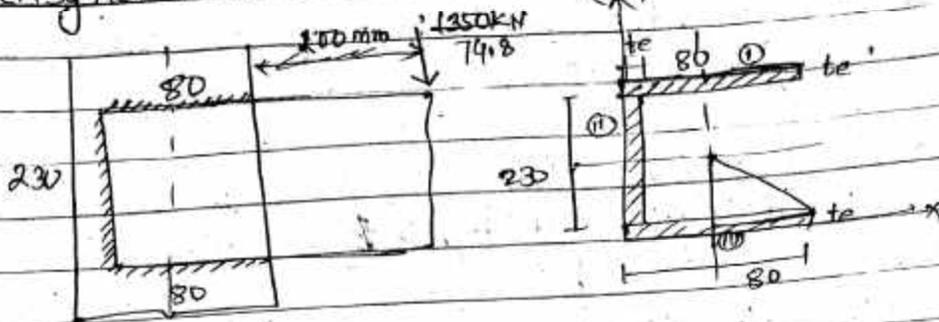
large projection:- a
Small " " :- b



Contd.

Remaining part:

Batten system: welded connection: (parallel to flange) $t_e = 0.75$



Now,

	A_i	x_i	y_i		
1	$80t_e$	40	$230 + 1.5t_e$	$\therefore \bar{x} = \frac{80 \times 40 t_e \times 2 + 230 t_e \times \frac{t_e}{2}}{390 t_e}$	
2	$230t_e$	$\frac{t_e}{2}$	$(115 + t_e)$		$= \frac{66400 t_e + 115 t_e^2}{390 t_e}$
3	$80t_e$	40	$\frac{t_e}{2}$		$= 16.41 + 0.30 t_e$
	$390 t_e$			$\approx 16.41 \text{ mm}$	

$$\bar{y} = 115 + t_e \approx 115 \text{ mm}$$

Then,

$$I_{xx} = \frac{80t_e^3}{12} + 80t_e(230 + 1.5t_e - 115)^2 + \frac{t_e 230^3}{12} + 230t_e(115 + t_e - 115)^2$$

$$+ \frac{80 \times t_e^3}{12} + 80t_e(t_e/2 - 115)^2$$

$$= 1058000t_e + 1013916.6t_e + 0 + 1058000t_e$$

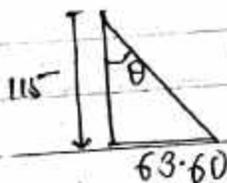
$$= 3129916.67t_e$$

$$I_{yy} = \left[\frac{80^3 t_e}{12} + 80t_e(40 - 16.41)^2 \right] \times 2 + \frac{t_e^3 230}{12} + 230t_e(t_e/2 - 16.41)^2$$

$$= 174371.42t_e + 61936.26 \times t_e$$

$$= 236307.68 t_e$$

$$\therefore I_p = 3366224.3 t_e$$



$$\therefore \theta = 28.94^\circ$$

$$r_{max} = \sqrt{115^2 + 63.60^2}$$

$$= 131.41 \text{ mm}$$

$$= 131.41 \text{ mm}$$

Since, Axial load = 1350 kN + 74.8 kN

$$\therefore e = 250 + 80 - 16.41$$
$$= 263.60 \text{ mm} \quad 112.8 \text{ mm}$$

$$lw = 230 + 80 \times 2$$
$$= 390 \text{ mm}$$

Now,

$$\text{vertical shear stress } (q_v) = \frac{P}{lw \times t_e} = \frac{1350}{390 \times t_e} = \frac{3.46}{t_e} \quad 0.192$$

$$\text{Torsional } q_T = \frac{\text{Permis}}{I_p}$$
$$= \frac{1350 \times 8437.5}{3366224.3 t_e} = \frac{0.7697}{t_e}$$
$$= \frac{13.89}{t_e} \quad 0.3294$$

$$\sigma_x = q_T \cos \theta$$
$$= \frac{12.15}{t_e} = \frac{0.6736}{t_e} \quad 0.288$$

$$\sigma_y = \frac{3461}{t_e} + \frac{6.72}{t_e} = \frac{10.181}{t_e} = \frac{0.939}{t_e}$$

$$\therefore \text{Resultant } R = \sqrt{\sigma_x^2 + \sigma_y^2}$$
$$= \frac{15.851}{t_e} = \frac{0.438}{t_e} \quad \text{fwd.}$$

for safe design.

$$R \leq \text{fwd}$$

$$\frac{0.838 \times 10^3 \times 15.851}{t_e} \leq 189.37$$

$$\therefore t_e \leq 83.70 \text{ mm} - 4.64 \text{ mm}$$

$$t_e = 0.75$$

$$\therefore S = 6629 \text{ mm} = 7 \text{ mm}$$

$$\approx 8 \text{ mm}$$

$$\frac{0.438 \times 10^3}{t_e} \leq 189.37$$

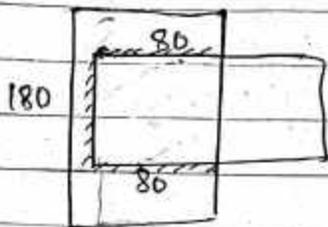
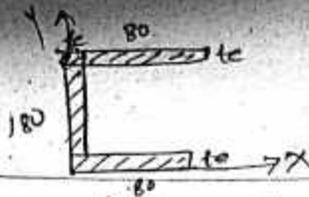
$$\therefore t_e = 2.32 \text{ mm}$$

$$\text{So, } t_e = 0.75$$

$$\therefore S = 3.31 \text{ mm}$$

$$\approx 4 \text{ mm}$$

Batten system: Welding



	A_i	x_i	y_i
1	$80te$	40	$180 + 1.5te$
2	$180te$	$te/2$	$90 + te$
3	$80te$	40	$te/2$
	<u>$340te$</u>		

$$\text{So, } \bar{x} = \frac{80 \times 40 \times 2 + 180 \times te/2}{340}$$

$$= 18.82$$

$$I_{xx} = 2 \left[\frac{80te^3}{12} + 80te \left(180 + 1.5te - 90 \right)^2 + \frac{te \times 180^3}{12} + 180te \left(90 + te - 90 \right)^2 \right]$$

$$+ 80te \left(0.5te - 90 \right)^2$$

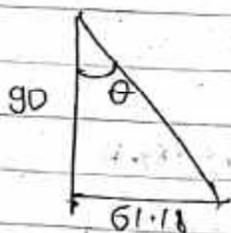
$$= 648000te + 486000te + 10 + \dots$$

$$= 1782000te$$

$$I_{yy} = 2 \left[\frac{80^3te}{12} + 80te \left(40 - 18.82 \right)^2 \right] + 180te \left(0.5te - 18.82 \right)^2$$

$$= 218115.12$$

$$I_p = 2000115.17te$$



$$\theta = \tan^{-1} \left(\frac{61.18}{90} \right) = 34.21^\circ$$

$$r_{max} = 108.82$$

$$P = 74.8 \text{ kN}$$

$$M = 84375 \text{ kN}\cdot\text{m}$$

$$lw = 340 \text{ mm}$$

$$q = \frac{P}{t_w t_e} = \frac{0.22}{t_e}$$

$$q_T = \frac{M_{R_{max}}}{I_p} \\ = \frac{8437.5 \times 10^8 \cdot 82}{2020115 \cdot 27} \\ = \frac{0.459}{t_e}$$

$$\therefore \sigma_x = q_T \cos \theta = \frac{0.379}{t_e}$$

$$\sigma_y = \frac{0.22}{t_e} + \frac{0.213}{t_e} = \frac{0.433}{t_e}$$

$$\therefore R = \sqrt{\sigma_x^2 + \sigma_y^2} \\ = \frac{0.575}{t_e}$$

Since

$$R \leq f_{wd}$$

$$\frac{0.575 \times 10^3}{t_e} \leq 189.37$$

$$\therefore t_e \geq 3.03 \text{ mm}$$

$$\approx 4 \text{ mm}$$

$$s_0, s = \frac{t_e}{0.7} = 5.71 \text{ mm}$$

$$\approx 6 \text{ mm}$$

Numerical:

Design slab base for SC 250 carrying an axial load of 500kN and grade of concrete used in pedestal is M20 (M20)

soln:-

1: Bearing capacity of concrete = $0.45 \times f_{ck}$
= 0.45×20
= 9 N/mm^2

2: Area required = $\frac{P}{0.45 f_{ck}} = \frac{500 \times 1.5}{0.45 \times 20}$
= 83333.33 mm^2

3: length & Breadth, $l = B = \sqrt{A} = \sqrt{83333.33}$
= 288.675 mm

for SC 250

$D = 250 \text{ mm}$

$B = 250 \text{ mm}$

$t_f = 17 \text{ mm}$

4. Adopt a slab base of size; ~~350 x 350 mm~~ 400 x 400

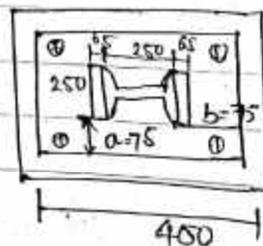
4. step 4: Pressure under column base =

$$\begin{aligned} W &= \frac{P}{A} \pm \frac{M}{Z} \\ &= \frac{500 \times 1.5 \times 10^3}{400 \times 400} \\ &= 4.88 \text{ N/mm}^2 < 9 \text{ N/mm}^2 \text{ OK!} \end{aligned}$$

5: Projection along x and y axis:

projection along x-axis := $b = 75$

" " " y-axis = $a = 75$



S0,

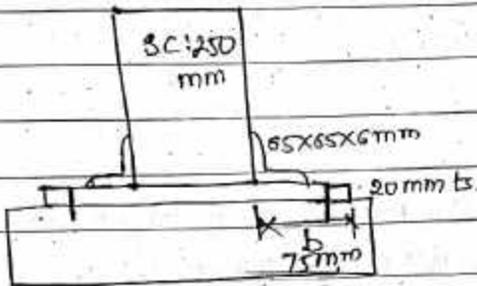
$$t_s = \sqrt{\frac{2.5 \times 4.6875^2 - 0.3 \times 75^2}{2.50}} \times 1.10$$

$$= 14.24 \text{ mm} \geq 17 \text{ mm}$$

take,

$$t_s = 20 \text{ mm}$$

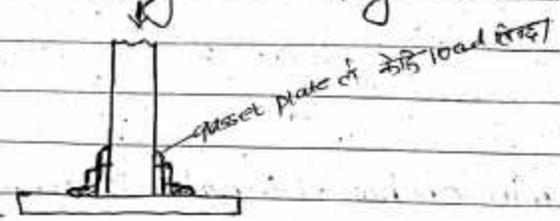
6: provide 4 anchor bolts of M20 of min anchored length 300mm
provide cleat angle of 65x65x6 mm



Column base

Gusseted plate:-

In case of large axial load or axial load with large BM depth of slab base is larger to overcome this limitation column are provided with gusset plates so that load is transferred to the base through bearing as well as through gusset plate



Design steps:

- a) Bearing capacity of concrete = $0.45f_{ck}$
- b) Calculate area of baseplate = $\frac{P_u}{0.45f_{ck}}$

c) length of base plate is calculated such that there is min. projection beyond gusset angle and width of base plate is calculated as

$$B = \frac{A}{l}$$

- d) Calculate the pressure underneath base plate.

$$w = \frac{P_u}{A} \pm \frac{M}{Z}$$

e) calculate thickness of base plate for Bending moment at most critical section

f) connection design:-

Use gusset plate of 16mm thickness

Use gusset angle of 150x115x16mm (ISA)

(Vertical bolts
H3. 1 bolts)

Design gusseted base for a column ISHB 300 @ 58.5 kg/m carrying factored axial load of 1800 kN, use M25 concrete for pedestal and M20 bolt of pr. cl 9.6

Soln:-

for ISHB @ 58.5 kg/m

$D = 300 \text{ mm}$

$B = 250 \text{ mm}$

$t_f = 10.6 \text{ mm}$

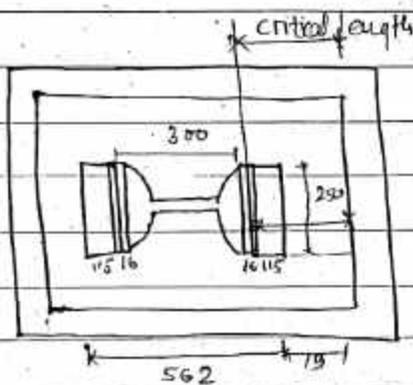
$t_w = 7.6 \text{ mm}$

$A = 74.8 \text{ cm}^2$

adopt gusset plate of 16 mm thickness & gusset angle of 150x115x16 mm (ISA)

a) Bearing capacity of concrete = $0.45 f_{ck}$
 $= 0.45 \times 25$
 $= 11.25 \text{ N/mm}^2$

$= 11.25 \text{ N/mm}^2$



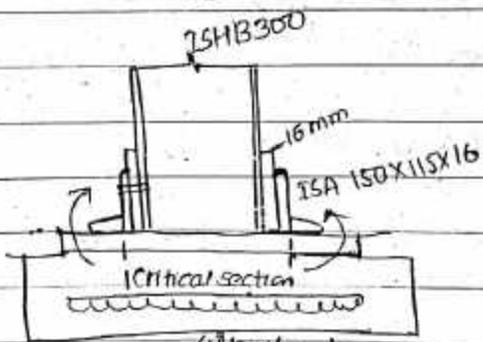
b) Area required (A) = $\frac{P_u}{B.C} = \frac{1800 \times 10^3}{11.25}$

$= 160000 \text{ mm}^2$

$= 1600 \text{ cm}^2$

c) length of gusset plate = $300 + 115 \times 2 + 16 \times 2$
 $= 562 \text{ mm}$

$\approx 600 \text{ mm}$



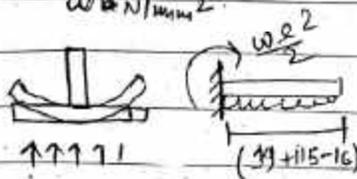
d) Width (B) = $\frac{A}{L} = \frac{160000}{600}$

$= 266.67 \text{ mm}$

≈ 300

e) $w = \frac{P_u}{A} + \frac{M}{Z} = \frac{1800 \times 10^3}{300 \times 600}$

$= 10 \text{ N/mm}^2 < 11.25 \text{ N/mm}^2$



length of critical section = 118 mm

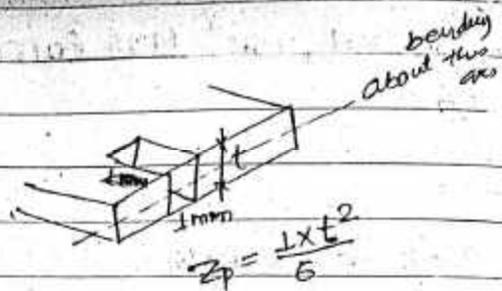
$$C = 118 \text{ mm} \quad (\text{critical length})$$

$$\text{B.M at critical section} = \frac{w \times l \times c \times c}{2}$$

$$= \frac{w c^2}{2}$$

$$= \frac{(10 \times 1) \times 118^2}{2}$$

$$= 69620 \text{ N.mm/mm} \quad \text{--- (i)}$$



$$\text{Bending capacity} = \frac{Z_p f_y}{\gamma_{mo}}$$

$$= \frac{1 \times t^2}{6} \times \frac{250}{1.10}$$

$$= \text{--- (ii)}$$

from (i) & (ii)

$$69620 = \frac{t^2 \times 250}{6 \times 1.10}$$

$$\therefore t = 42.87 \text{ mm}$$

$$\approx 50 \text{ mm}$$

f) 50% of load is transferred by bearing, only 50% load is to be transferred by connection for gusset plate.

$$\therefore \text{load for connection} = 50\% \text{ of factored load}$$

$$= 50 \times 1800$$

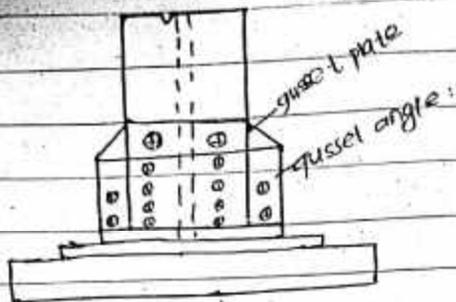
$$= 900 \text{ kN}$$

for M20 both of prcl: 4.6

$$V_{dsb} = \frac{f_{ub}}{\sqrt{3} \times 1.25} \times 1.787 \times \frac{20^2}{4} = 103314 \text{ kN}$$

$$\text{No of bolts} = \frac{900}{103314} = 8.71$$

$$\approx 10$$



Eccentrically loaded column base:-

$$\omega = \frac{P}{l \times B} \pm \frac{P \times e}{\frac{B \times l^2}{6}}$$

$$= \frac{P}{lB} \left[\frac{1}{6} \pm \frac{6e}{l} \right]$$

for tension in this section:-

$$\omega = 0$$

$$\frac{P}{lB} \left(1 \pm \frac{6e}{l} \right) = 0$$

$$\therefore 1 = \frac{6e}{l}$$

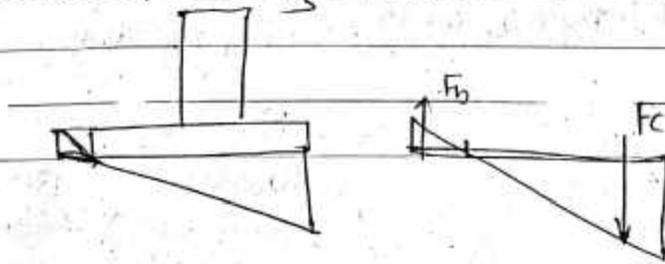
$$\boxed{\frac{l}{6} = e}$$

case ① if $e \leq \frac{l}{6}$ section column base is entirely under compression

$$\boxed{\left(\frac{P}{A} + \frac{M}{Z} \right) \leq 0.45 f_{ck}}$$

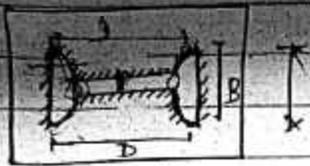
case ② if $e \geq \frac{l}{6}$ and $e \leq \frac{l}{3}$ although column base is under tension it is negligible hence designed similar to case ①.

case ③ if $e > \frac{l}{3}$, tension in column base is significant



$$\text{no. anchor bolt} = \frac{T_{du}}{f_b} = \frac{F_b}{T_{du}}$$

Welded connection



$$l_w = 2 \times B + 2(B - t) + 2(D - t)$$

Now, ISHB 300

$$D = 300 \text{ mm}$$

$$B = 250 \text{ "}$$

$$t_f = 10.6 \text{ "}$$

$$t_{flange} = 7.6 \text{ "}$$

$$A = 74.8 \text{ cm}^2$$

factored load = 1800 kN

Now,

$$\text{length of weld} = 2 \times 250 + 2(300 - 2 \times 10.6) + 2(250 - 9.4)$$

$$= 1539 \text{ mm}$$

load from column be transferred by weld connection

for, size of weld

$$\text{let, } s = 8 \text{ mm}$$

$$\text{and, } l_e = l_w - (\text{end turn}) \times 2s$$

$$= 1539 - 12 \times 2 \times 8$$

$$= 1347 \text{ mm}$$

$$\text{throat thickness } (t_e) = 0.7s$$

$$= 0.7 \times 8$$

$$= 5.6 \text{ mm}$$

$$\text{Strength of weld} = \frac{f_u}{\sqrt{3} \gamma_{mw}} \times A_{we}$$

$$= \frac{410}{\sqrt{3} \times 1.25} \times 5.6 \times l$$

$$= 1060.48 \text{ N/mm} \quad (\text{for shop weld})$$

$$\therefore \text{Required length of weld} = \frac{\text{axial load}}{\text{Strength/mm}}$$

$$= \frac{1800 \times 10^3}{1060.48}$$

$$= \frac{1800 \times 10^3}{1060.48} = 1697 \text{ mm} > 1539 \text{ mm}$$

not ok!

again increased the size of weld as $f = 12 \text{ mm}$

$$\begin{aligned} \text{SO, } l_e &= l_w - 12 \times 25 \\ &= 1539 - 12 \times 2 \times 12 \\ &= 1251 \text{ mm} \end{aligned}$$

$$\begin{aligned} \text{throat thickness } = t_e &= 0.7s \\ &= 0.7 \times 12 \\ &= 8.4 \text{ mm} \end{aligned}$$

$$\begin{aligned} \text{Strength of weld/mm} &= \frac{8.4 \times 1 \times 410}{\sqrt{3} \times 125} \\ &= 1590 \text{ N/mm (Shop weld)} \end{aligned}$$

$$\begin{aligned} \text{Required length of weld} &= \frac{\text{Axial load}}{\text{Strength/mm}} \\ &= \frac{1800 \times 10^3}{1590} \\ &= 1132 \text{ mm} < 1251 \text{ mm OK} \end{aligned}$$

Hence, provide the size of weld = 12 mm

Required length of weld = 1132 mm

CH: 5 Tension Members:

→ Members are the action of axial tension or member under tension due to BM are tension members.

failure in tension member

6.2.2.

① Yielding of section

$$T_{dy} = \frac{A_g f_y}{\gamma_{mo}}$$

② Rupture on tearing of section:-

$$T_{dn} = \frac{0.9 A_n f_u}{\gamma_{m1}}$$

$$\text{where, } A_n = \left[\left\{ (b - nd_0) + \frac{\sum p_i^2}{4g} \right\} t \right]$$

③ Block shear failure: [cl. 6.4]

$$T_{db} = \left[A_g f_y / (\sqrt{3} \gamma_{mo}) + 0.9 A_n f_u / \gamma_{m1} \right]$$

or

$$= \left[0.9 A_n f_u / (\sqrt{3} \gamma_{m1}) + A_g f_y / \gamma_{mo} \right]$$

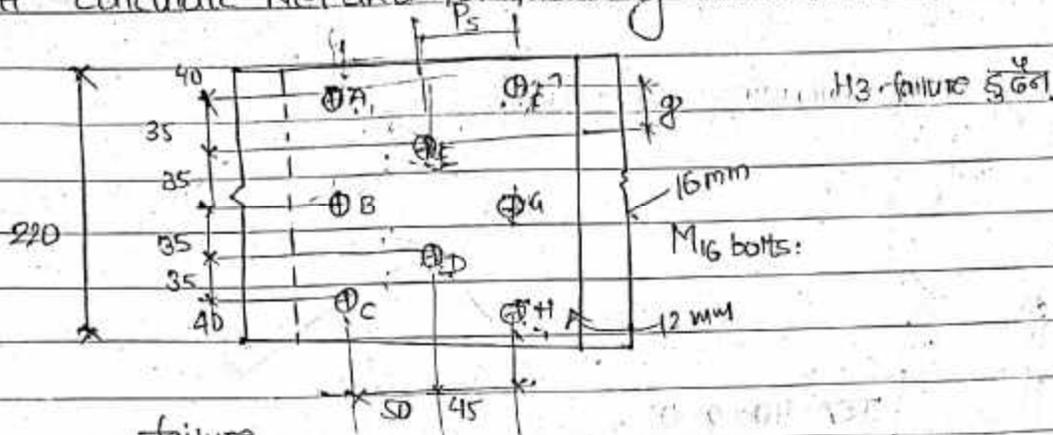
Net area:

$$A_n = \left[\left\{ b - nd_0 \right\} + \frac{\sum p_i^2}{4g} \right] \times t$$

also,

$$T_{dn} = 0.9 A_n f_u / \gamma_{m1}$$

Calculate Net area for following connection:



failure
 (i) Along ABC

$$A_n = [(B - n d_o) + \frac{\sum p_i^2}{4g}] \times t$$

$$= [(220 - 3 \times 18)] \times 12$$

$$= 1992 \text{ mm}^2$$

(v) along AEDC

$$A_n = 2204.57$$

(vi) along A-F-G-H, A-B-C

$$A_n = 1992$$

(ii) along A-E-B-C

$$A_n = [(B - n d_o) + \frac{\sum p_i^2}{4g}] \times t$$

$$= [(220 - 4 \times 18) + \frac{50^2}{4 \times 35}] \times 12$$

$$= 1990.28 \text{ } 2204.57$$

2 - due to two inclination

(vii) along AEGH $A_n = 2163.85$

(viii) along FEGDH

$$A_n = 2254.28 \text{ mm}^2$$

(ix) along F-E-D

$$A_n = 2165.57 \text{ mm}^2$$

(iii) along A-F-B-D-C

$$A_n = [(220 - 5 \times 18) + \frac{4 \times 50^2}{4 \times 35}] \times 12$$

$$= 2417.14$$

along F-E-GH

$$A_n = 1940.57 \text{ } 2123.14 \text{ mm}^2$$

(iv) along A-E-D

$$A_n = 2206.28$$

for failure

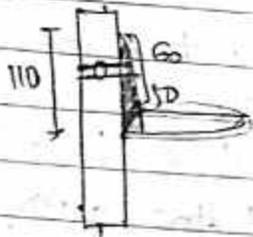
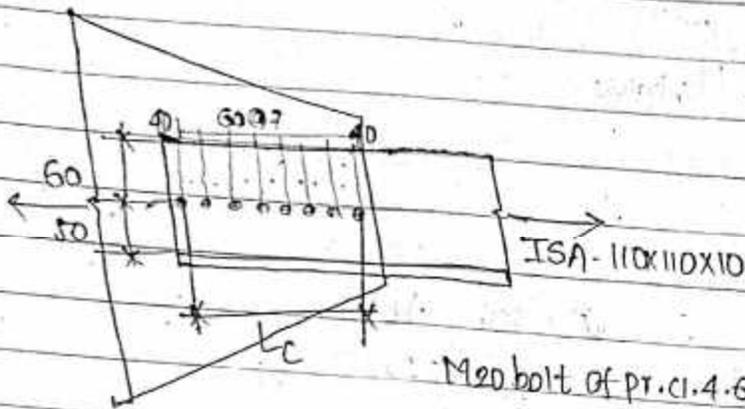
no of bolt है

प्रथम भेदी inclination दिर की arrangement लिते

[Tension word
Tensile capacity]

SD, $A_n = 1992 \text{ mm}^2$

Calculate Tensile capacity of the following connection:



Now, design shear strength $V_{dsb} = \frac{f_{ub} (A_n n_s + A_s n_t)}{\sqrt{3} \gamma_m}$

$$= \frac{400 \cdot 0.7871 \times 20^2}{\sqrt{3} \times 1.25}$$

$$= 45.272 \text{ kN}$$

$$\text{Total design shear strength} = 45.272 \times 8$$

$$= 362.18 \text{ kN} \quad \text{--- (1)}$$

$$b = 60$$

$$e = 40$$

$$\therefore \frac{e}{3d_0} + \frac{p}{3d_0} = 0.25$$

$$0.60, 0.659$$

$$\text{Bearing capacity} = \frac{2.5 k b d t (f_u / f_{ub})}{1.25}$$

$$(V_{dpb}) = \frac{2.5 \times 0.60 \times 20 \times 10 \times 400}{1.25}$$

$$= 9600 \text{ kN}$$

$$\therefore \text{Total } V_{dpb} = 9600$$

$$= 768 \text{ kN} \quad 775.68 \text{ kN} \quad \text{--- (2)}$$

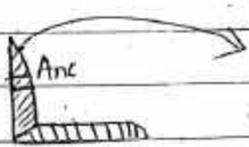
$$\textcircled{iii} \text{ Yielding capacity of plate (Tdg)} = \frac{A_g f_y}{\gamma_{m0}}$$

$$= \frac{210 \times 250}{1.10}$$

$$= 478.54 \text{ kN}$$

\textcircled{iv} Rupture on tearing of section;

$$T_{dn} = \frac{0.9 A_{nc} f_y}{\gamma_{m1}} + \beta \frac{A_{go} f_y}{\gamma_{m0}}$$



connected leg area

$$A_{nc} = (500 - 8 \times 72) \times 10$$

$$= 3240 \text{ mm}^2$$

$$A_{nc} = [(110 - 10) - 22] \times 10 + \frac{1}{2} \times 10 \times 10$$

$$= 830 \text{ mm}^2$$

$$A_{go} = 100 \times 10 + 50 = (110 - 10) \times 10 + \frac{1}{2} \times 10 \times 10$$

$$= 1050 \text{ mm}^2$$

$$\text{So, } \beta = 1.4 - 0.076 \left(\frac{w/t}{t} \right)^{1/4} \left(\frac{b_s}{L_c} \right) \leq f_u \gamma_{m0} / f_y \gamma_{m1}$$

$$\geq 0.7$$

$$= 1.4 - 0.076 \left(\frac{110}{10} \right) \left(\frac{100}{420} \right)^{1/4} \leq \frac{410 \times 1.10}{250 \times 1.25}$$

$$= 1.20 \leq 1.44$$

$$\geq 0.7$$

$$b_s = W + w_L - t \geq 0.70$$

$$= 110 + 50 - 10$$

$$= 150$$

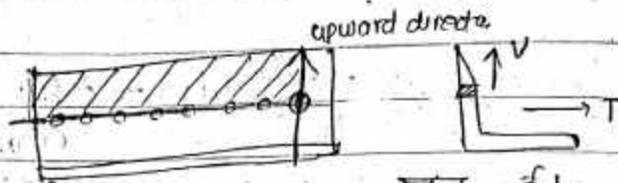
$$L_c = 60 \times 7 = 420$$

$$\therefore \beta = 1.20$$

$$\text{So, } T_{dn} = \frac{0.9 \times 830 \times 410}{1.25} + \frac{1.20 \times 1050 \times 250}{1.10}$$

$$= 535.6 \text{ kN}$$

Q. Block shear failure:



7.5 bolt dia $u \leq l$

shear area $\left[\begin{array}{l} A_{gv} = (40 + 7 \times 60) \times 10 = 4600 \text{ mm}^2 \end{array} \right.$

$\left[\begin{array}{l} A_{vn} = [(40 + 7 \times 60) - 7.5 \times 22] \times 10 = 2950 \text{ mm}^2 \end{array} \right.$

tension area $\left[\begin{array}{l} A_{tg} = 60 \times 10 = 600 \text{ mm}^2 \end{array} \right.$

$\left[\begin{array}{l} A_{tn} = (60 - 0.5 \times 22) \times 10 = 490 \text{ mm}^2 \end{array} \right.$

$$T_{db} = \frac{A_{gv} f_y}{\sqrt{3} \gamma_{mo}} + 0.9 \frac{A_{tn} f_u}{\gamma_{mi}} = 748.24 \text{ kN}$$

$$= \frac{0.9 A_{vn} f_u}{\sqrt{3} \gamma_{mi}} + \frac{A_{tg} f_y}{\gamma_{mo}} = 639.143 \text{ kN}$$

so, $T_{db} = 639.143 \text{ kN}$

so, Tensile capacity of angle = 362.16 kN

Design unequal angle to carry a factored tensile load of 250 kN
 soln:- use M20 bolt of prcl 4.6

from yielding criteria:

$$T_{dg} = \frac{f_y A_g}{\gamma_{mo}}$$

$$250 \times 10^3 = \frac{250 \times A_g}{1.10}$$

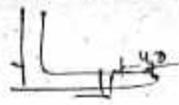
$$\therefore A_g = 1100 \text{ mm}^2 = 11 \text{ cm}^2$$

also:

$$T_{dn} = \frac{\alpha A_n f_u}{\gamma_{mi}}$$

$$250 \times 10^3 = \frac{0.8 \times A_n \times 400}{1.25}$$

$$A_n = 9.52 \text{ cm}^2$$



Selection of ^{unequal} angle having area $> 11 \text{ cm}^2$

take ISA $90 \times 60 \times 10$ $A = 14 \text{ cm}^2$

$$V_{dsb} = \frac{f_{ub}}{\sqrt{3} \gamma_{mb}} \left(1 \times 0.78 \times 71 \times \frac{20^2}{4} \right)$$

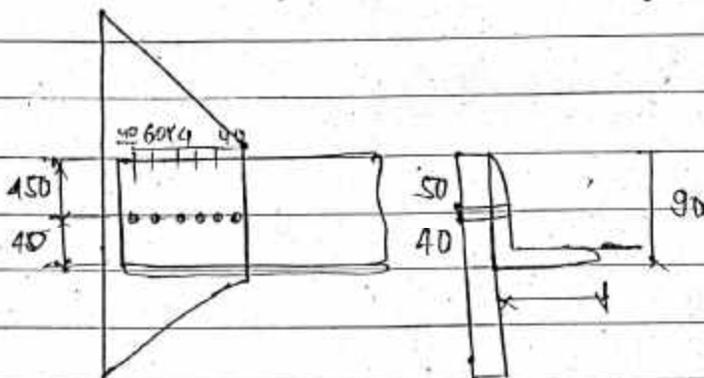
$$= 45.27 \text{ kN}$$

$$\therefore \text{no of bolts} = \frac{\text{load}}{V_{dsb}} = \frac{250}{45} = 5.5$$

take $n = 6$

$$\text{pitch } p \geq 2.5d = 50 \approx 60 \text{ mm}$$

$$e \geq 1.5d_0 = 1.5 \times 22 \geq 33 \text{ mm} \approx 40 \text{ mm}$$



$$V_{dpb} = \frac{2.5 k_b d_t (f_u / t_{ub})}{1.25}$$

$$= \frac{2.5 \times 0.606 \times 20 \times 10 \times 400}{1.25}$$

$$= 96.96 \text{ kN}$$

$$\text{Total} = 96.96 \times 6$$

$$= 581.76 > 250 \text{ kN OK!}$$

Tdn 2 block check gerd:

$$A_{g0} = (90 - 10) \times 10 + \frac{10 \times 10}{2}$$
$$= 805 \text{ mm}^2$$

$$w = 90$$

$$b_s = w + w_1 - t$$

$$= 90 + 40 - 10$$

$$= 120 \text{ mm}$$

$$L_c = 5 \times 60 = 300 \text{ mm}$$

$$\beta = 1.4 - 0.076 \times (w/t) \times \left(\frac{t_1}{t_2}\right) \times \left(\frac{b_s}{L_c}\right)$$
$$= 1.233 \leq 1.44$$

$$T_{dn} = \frac{0.9 \times 585 \times 410}{1.25} + \frac{1.233 \times 805 \times 250}{1.10}$$
$$= 398.27 > 250$$

$$A_{vg} = (40 + 5 \times 60) \times 10$$
$$= 3400$$

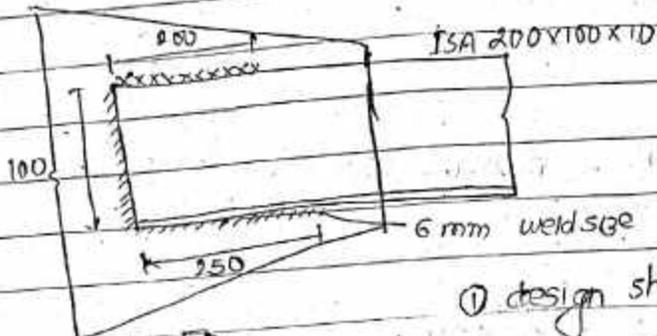
$$A_{vn} = 24100 \text{ mm}^2$$

$$A_{tg} = 50 \times 10 = 500 \text{ mm}^2$$

$$A_{tn} = (50 - 0.5 \times 22) \times 10 = 370 \text{ mm}^2$$

$$T_{db} = \frac{3400 \times 250}{\sqrt{3} \times 1.10} + \frac{0.9 \times 370 \times 410}{1.25}$$
$$= 561.28 > 250 \text{ KN}$$

Calculate tensile load carrying capacity of following angle section.



① design shear capacity of weld (fwd) = $\frac{f_u}{\sqrt{3} \times 1.25}$
 $= \frac{410}{\sqrt{3} \times 1.25}$
 $= 189.37 \text{ kN}$

$l_c = \frac{250 + 200}{2} = 225 \text{ mm}$
 $b_s = w = 100$

total load carried by weld = $f_w \times t \times l_e$
 $= 189.37 \times 0.7 \times 550$
 $= 189.37 \times 0.7 \times 6 \times 550$
 $= 437.4 \text{ kN}$

$l_w = 200 + 100 + 250$
 $= 550$

for ISA 100x100x10
 $A = 19 \text{ cm}^2$

② Yielding capacity of angle = $\frac{f_y A_g}{1.10}$
 $= \frac{250 \times 19 \times 10}{1.10}$
 $= 431.8 \text{ kN}$

$A_{nc} = (100 - \frac{10}{2}) \times 10$
 $= 950 \text{ mm}^2 = A_{70}$
 $\beta = 1.4 - 0.076 \times \frac{100 \times 250 \times 10}{10 \times 410 \times 225}$
 $= 1.19 \geq 0.7$

$\leq \frac{410 \times 1.1}{250 \times 1.25} = 1.44$

③ Rupture or Tearing,

$f_{dn} = \frac{0.9 A_{nc} f_u}{\gamma_{m1}} + \frac{\beta A_{70} f_y}{\gamma_{m0}}$
 $= \frac{0.9 \times 950 \times 410}{1.25} + \frac{1.19 \times 950 \times 250}{1.10}$
 $= 537.31 \text{ kN}$

① Block shear failure:-

$$A_{vg} = A_{tn} = (200 + 250) \times 10 = 4500 \text{ mm}^2$$

$$A_{tn} = A_{tg} = 100 \times 10 = 1000 \text{ mm}^2$$

$$T_{db} = \frac{4500 \times 250}{\sqrt{3} \times 1.10} + \frac{0.9 \times 1000 \times 410}{1.25} = 885.67 \text{ kN}$$

$$\text{or, } \frac{0.9 \times 1000 \times 410}{\sqrt{3} \times 1.25} + \frac{1000 \times 250}{1.10} = 994.224 \text{ kN}$$

So, Tensile load carrying capacity:- 431.8 kN

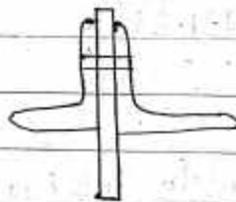
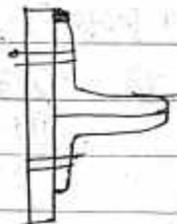
calculate load carrying capacity of 2 ISA 100x100x10 connected to a gusset plate 16 mm in

① same side of gusset plate

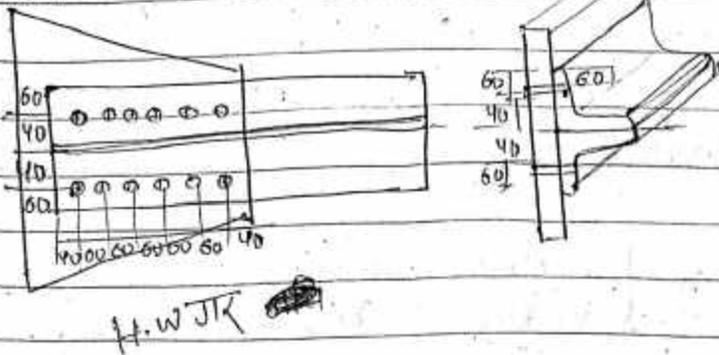
② opposite " " " "

इसके value single बार निकालें और multiply करें।

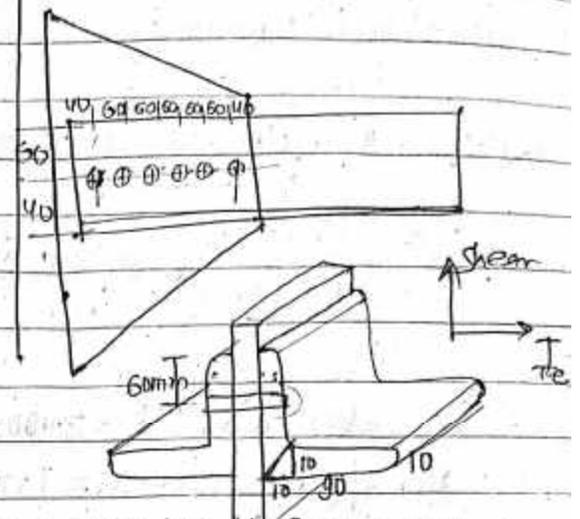
Same side.



① Same side:



opposite side:



assume M20 bolt of prcl. 4.6
plate thickness = 16 mm
angle:

2 ISA 150x150x10

Yielding capacity of angle (T_{dy})

$$= \frac{A_g f_y}{\gamma_{m0}}$$

$$= \frac{1500 \times 250}{1.10}$$

$$= 431.82 \text{ kN}$$

Total yielding = $2 \times 431.82 = 863.636 \text{ kN}$ — (ii)

Rupture strength $T_{dn} = \frac{0.9 A_{nc} f_u}{\gamma_{m1}} + \frac{\beta A_{g0} f_y}{\gamma_{m0}}$

$$= \frac{0.9 \times 410 A_{nc}}{1.25} + \frac{\beta \times A_{g0} \times 250}{1.10}$$

$$A_{nc} = [(100 - 10) - 22] \times 10 + \frac{10 \times 10}{2} = 730 \text{ mm}^2$$

$$A_{g0} = (100 + 10) \times 10 + 50 = 950 \text{ mm}^2$$

$$L_c = 60 \times 5 = 300, \quad b_g = w + w_1 - t = 130$$

$$\beta = 1.4 - 0.076 \times \left(\frac{100}{10}\right) \times \frac{250}{400} \times \frac{130}{300}$$

$$= 1.2 > 0.7$$

$$\leq 1.4$$

$$\therefore T_{dn} = 474.586 \text{ kN}$$

$$\text{Total } T_{dn} = 2 \times 474.586$$

$$= 949.172 \text{ kN} \text{ — (iv)}$$

① design shear strength of bolt

$$V_{dsb} = \frac{f_{ub} (1.787 d^2)}{\sqrt{3} \times 1.25 \times 4}$$

$$= \frac{400 \times 1.787 \times \pi \times 20^2}{\sqrt{3} \times 1.25 \times 4}$$

$$= 103.31 \text{ kN}$$

Total $V_{dsb} = 103.31 \times 6 = 619.884$

$$V_{dph} = \frac{2.5 k_b d t f_u / f_{ub}}{1.25}$$

$$= \frac{2.5 \times 0.606 \times 20 \times 16 \times 400}{1.25}$$

$$= 155.136 \text{ kN}$$

Total $V_{dph} = 6 \times 155.136$

$$= 930.816 \text{ kN}$$

— (iii)

Lag angle if the length of connection is restricted An extra angle section is provide

Design strength due to block shear:

$$T_{db} = \left[\frac{A_{vg} f_y}{\sqrt{3} \gamma_{m0}} + \frac{0.9 A_{tn} f_u}{\gamma_{m1}} \right] \text{ or } \left[\frac{0.9 A_{vn} f_u}{\sqrt{3} \gamma_{m1}} + \frac{A_{tg} f_y}{\gamma_{m0}} \right]$$

$$A_{vg} = (40 + 60 \times 5) \times 10 = 3400 \text{ mm}^2$$

$$A_{vn} = [(40 + 60 \times 5) - 5.5 \times 22] \times 10 = 3504 \text{ mm}^2 \quad 2190 \text{ mm}^2$$

$$A_{tg} = 60 \times 10 = 600 \text{ mm}^2$$

$$A_{tn} = (60 - 0.5 \times 22) \times 10 = 490 \text{ mm}^2$$

$$\text{So, } T_{db} = \left(\frac{3400 \times 250}{\sqrt{3} \times 1.10} + \frac{0.9 \times 490 \times 410}{1.25} \right) \text{ or } \left[\frac{0.9 \times 2190 \times 410}{\sqrt{3} \times 1.25} + \frac{600 \times 250}{1.10} \right]$$

$$= 590.78 \text{ or } 509.613 \text{ kN}$$

$$\text{So, Total } T_{db} = 2 \times 509.613$$

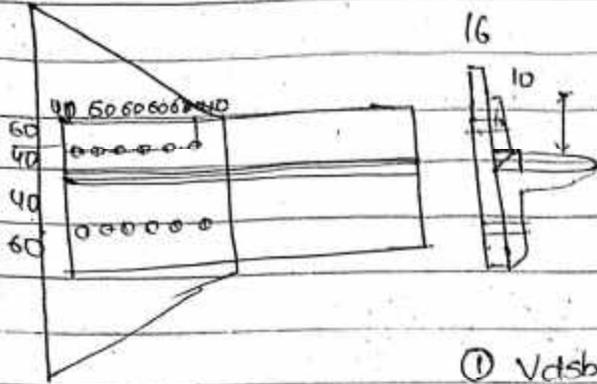
$$= 1019.227 \text{ kN} \quad \text{--- (v)}$$

Hence, load carrying capacity = 619.884 kN



Soln:-

On same side:



Given M20 bolt

$$d = 20 \text{ mm}$$

$$d_o = 22 \text{ mm}$$

$$p = 16 \text{ mm}$$

$$\text{ISA} = 100 \times 100 \times 10 \text{ mm}$$

$$\textcircled{1} V_{dsb} = \frac{f_{ub}}{\sqrt{3} \times 1.25} \left(0.787 \pi \frac{d^2}{4} \right)$$

$$= \frac{400 \times 0.787 \times \pi \times 20^2}{\sqrt{3} \times 1.25 \times 4}$$

$$= 45.272 \text{ kN}$$

$$\text{Total } V_{dsb} = 45.272 \times 6 \times 2 = 271.632 \text{ kN} \times 2 = 543.264 \text{ kN}$$

$$\textcircled{11} \text{ Bearing capacity} = \frac{2.5 k_b d t (f_u / f_{ub})}{1.25}$$

$$= \frac{2.5 \times 0.606 \times 20 \times 10 \times 400}{1.25} = 96.96 \text{ kN}$$

$$\text{Total } V_{dpb} = 96.96 \times 6 \times 2 = 581.76 \text{ kN} \times 2 = 1163.52 \text{ kN}$$

$$\textcircled{12} \text{ Yielding strength of angle} = T_{dg} = \frac{A_g f_y}{1.10} = \frac{1900 \times 250}{1.10} = 431.818 \text{ kN}$$

$$\text{Total } T_{dg} = 2 \times 431.818 = 863.636 \text{ kN}$$

\textcircled{13} Design strength due to rupture.

$$T_{dn} = \frac{0.9 A_{nc} f_u}{1.25} + \frac{\beta A_{gd} f_y}{1.10}$$

$$\beta = 1.4 - 0.076 \times \frac{100}{10} \times \frac{200}{410} \times \frac{130}{300}$$

$$= 1.19 \geq 0.7$$

$$\leq 0.94$$

$$\therefore T_{dn} = 472.427$$

$$\therefore \text{Total } T_{dn} = 944.855 \text{ kN}$$

$$A_{nc} = (100 - 10 - 22) \times 10 + \frac{1}{2} \times 100 \times 10 = 730 \text{ mm}^2$$

$$A_{gd} = (100 - 10) \times 10 + 50 = 950 \text{ mm}^2$$

$$W = 100$$

$$W_t = 40 \quad b_s = 140 - 10 = 130$$

$$L = 10 \quad L_c = 60 \times 5 = 300$$

Block shear:

$$A_{vg} = (40 + 60 \times 5) \times 10 = 3400 \text{ mm}^2$$

$$A_{vn} = (40 + 60 \times 5 - 4.5 \times 22) \times 10 = 2190 \text{ mm}^2$$

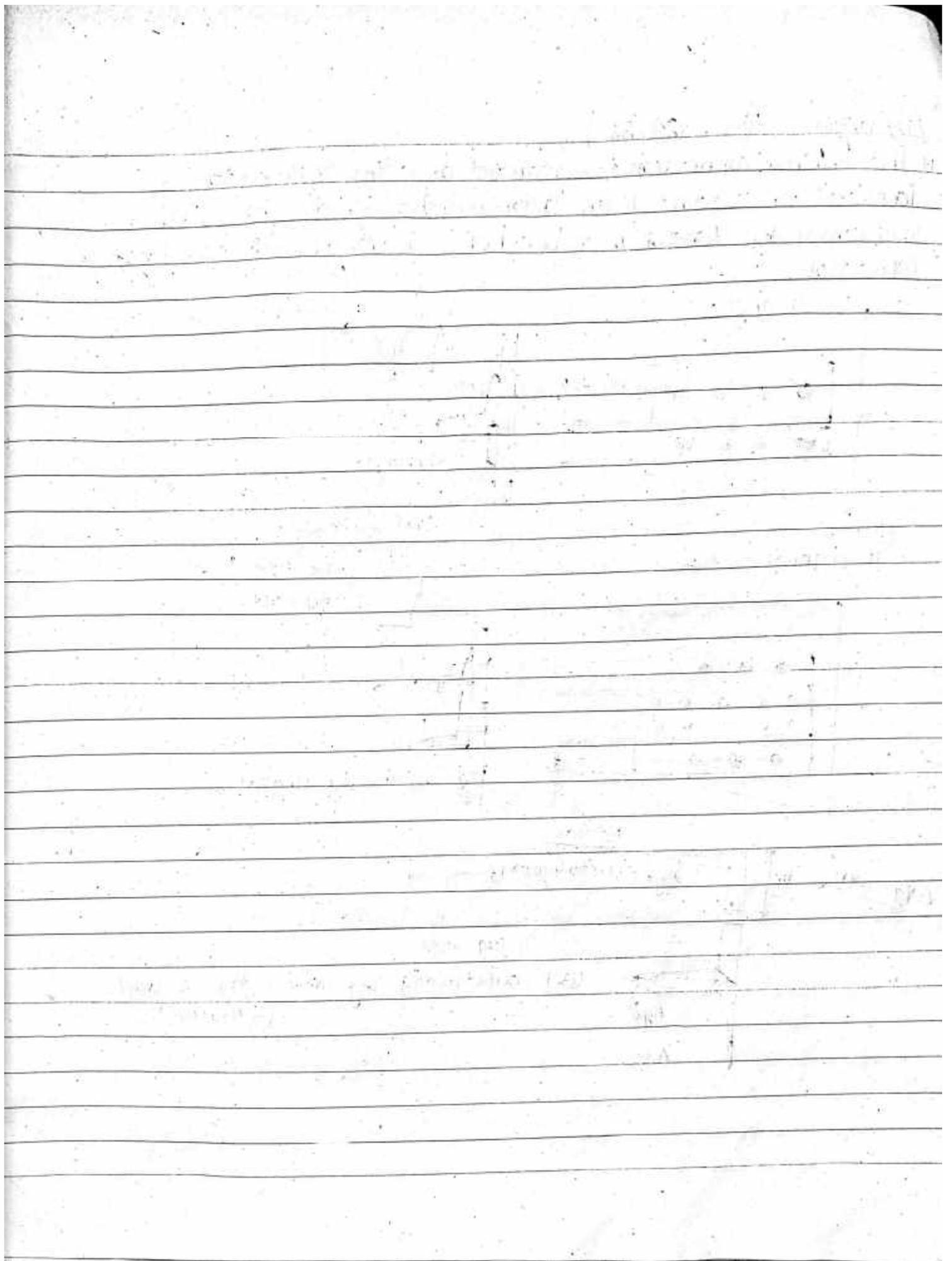
$$A_{tg} = 60 \times 10 = 600 \text{ mm}^2$$

$$A_{tn} = (60 - 0.5 \times 22) \times 10 = 490 \text{ mm}^2$$

$$\begin{aligned} \therefore T_{db} &= \left(\frac{A_{vg} f_y}{\sqrt{3} \times 1.10} + \frac{0.9 A_{tn} f_u}{1.25} \right) \text{ or } \left[\frac{0.9 A_{vn} f_u}{\sqrt{3} \times 1.25} + \frac{A_{tg} f_y}{1.10} \right] \\ &= \left(\frac{3400 \times 250}{\sqrt{3} \times 1.10} + \frac{0.9 \times 490 \times 410}{1.25} \right) \text{ or } \left(\frac{0.9 \times 2190 \times 410}{\sqrt{3} \times 1.25} + \frac{600 \times 250}{1.10} \right) \\ &= 790.782 \text{ kN or } 509.615 \end{aligned}$$

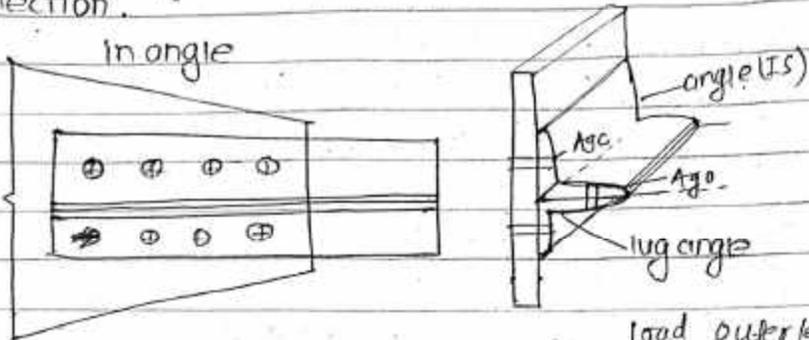
$$\text{So, Total } T_{db} = \underline{1019.227 \text{ kN}}$$

$$\text{Hence, Tensile Capacity} = 271.632 \text{ kN} \times 2 = 543.64 \text{ kN}$$



Lug angle: 10.12 (83/84)

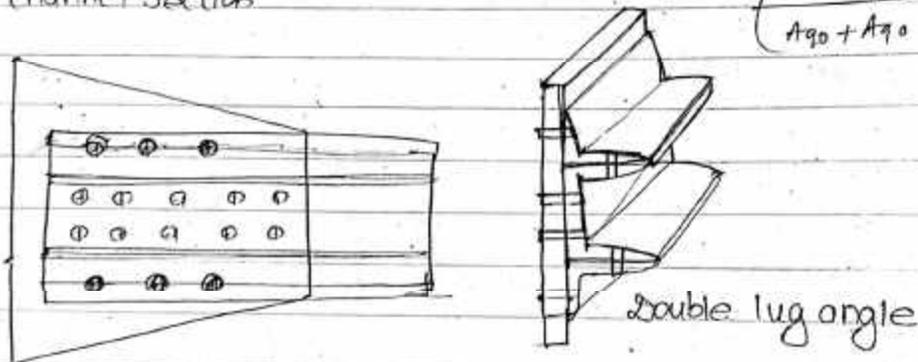
if the length of connection is restricted an extra angle section is provided to support main tension member which share (load) load carried by tension member hence reducing no of bolts & length of connection.



load by outer leg:

$$\left(\frac{100 A_{gl}}{A_{gl} + A_{gc}} \right)$$

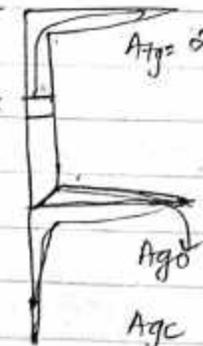
in channel section



MC 400

$$A_{lg} = A_{vd}$$

v_1



$$A_{lg} = 200 \times t_w + 100 \times t_f - t_f - t_w$$

lug angle

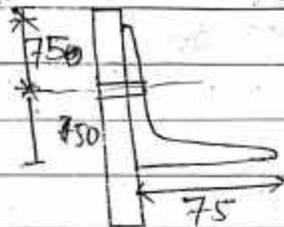
outstanding leg load = $\frac{A_{gl}}{2 A_{gl} + A_{gc}}$ x load

Design criteria 10.12.2

load carried by lug angle & its connection to gusset plate is 20% in excess of load carried by outstanding leg whereas load carried by connection betⁿ lug angle & main member is 40% in excess of load carried by outstanding leg in case of single lug angle.

Design a single ^(unequal) angle to carry a factored tensile load of 400 kN using M16 bolts of pr CI 4.6. Design with & without lug angle:

a) without lug angle:-



$$W = 75$$

$$W_t = 50 \quad t = 10 \quad \therefore b_s = 75 + 50 - 10$$

$$\textcircled{1} \text{ Area required} = \frac{T \times 8 m_0}{f_y} = \frac{400 \times 10^3 \times 1.10}{250} = 1760 \text{ mm}^2 = 17.60 \text{ cm}^2$$

Select ISA 125x75x10 mm having $A = 18.0 \text{ cm}^2$

connection g design:-

$$\textcircled{1} V_{dsb} = \frac{f_{ub}}{\sqrt{3}} \times 0.787 \times \frac{b^2}{4} = 28.974 \text{ kN}$$

$$\textcircled{2} V_{dpb} = \frac{2.5 \times 0.556 \times 16 \times 10 \times 400}{1.25} = 71.168 \text{ kN}$$

$$\therefore \text{no of bolts} = \frac{400}{28.974} = 13.8 \approx 14 \text{ nos}$$

$$\text{Total bearing capacity} = 14 \times 71.168$$

$$= 996.352 \text{ kN} > 400 \text{ kN}$$

$$\text{Pitch } p \geq 2.5d_0 = 2.5 \times 18 = 40 \approx 50$$

$$\text{edge } e \geq 1.5d_0 = 1.5 \times 18 \approx 30 \text{ mm}$$

$$k_b = 0.556$$

Tensile capacity of angle:
connected longer leg to gusset:

$$b_s = 115$$

$$t = 10$$

$$W = 75$$

$$L_c = 13 \times 50 = 650 \text{ mm}$$

$$\beta = 1.4 - 0.076 \times \left(\frac{75}{10}\right) \times \frac{250}{410} \times \frac{115}{650}$$

$$= 1.34 > 0.7$$

$$A_{g0} = (115 - 18) \times 10 = 970 \text{ mm}^2 + 50$$

$$+ 50 = 1020 \text{ mm}^2$$

$$A_{g0} = (75 - 10) \times 10 + \frac{13 \times 10}{2} = 700 \text{ mm}^2$$

$$\therefore T_{dn} = \frac{0.9 \times 1020 \times 410}{1.25} + \frac{1.34 \times 700 \times 250}{1.10}$$

$$= 514.285 \text{ kN} > 400 \text{ kN}$$

For Block shear strength

$$A_{vg} = (90 + 50 \times 13) \times 10 = 6800 \text{ mm}^2$$

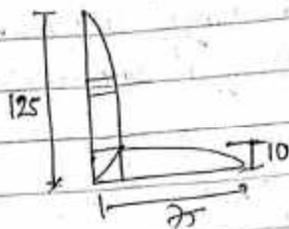
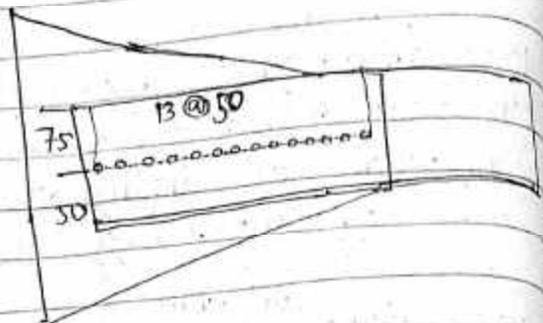
$$A_{vn} = (30 + 50 \times 13 - 13.5 \times 18) \times 10 = 4370 \text{ mm}^2$$

$$A_{tg} = 75 \times 10 = 750 \text{ mm}^2$$

$$A_{tn} = (75 - 0.5 \times 18) \times 10 = 660 \text{ mm}^2$$

$$T_{db} = \left(\frac{6800 \times 250}{\sqrt{3} \times 1.10} + \frac{0.9 \times 660 \times 410}{1.25} \right) \text{ or } [170.43 \times A_{vn} + 227.27 \times A_{tg}]$$

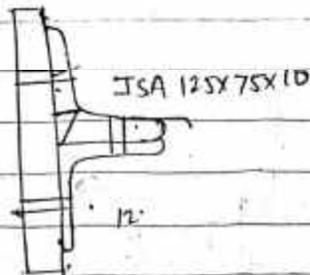
$$= 1089.20 \text{ kN} \text{ or } 915.23 \text{ kN} > 400 \text{ kN}$$



With Lug angle

$$A_{go} = (75 - \frac{10}{2}) \times 10 \\ = 700 \text{ mm}^2$$

$$A_{gc} = (125 - \frac{10}{2}) \times 10 \\ = 1200 \text{ mm}^2$$



$$\text{load carried by connected leg} = \frac{1200}{(1200 + 700)} \times 400 \text{ kN} \\ = 252.6 \text{ kN}$$

$$\text{load carried by outstanding leg} = \frac{700}{(1200 + 700)} \times 400 \text{ kN} \\ = 147.368 \text{ kN}$$

Now, for M16 bolt of PTC 4.6

$$V_{dsb} = 28.97 \text{ kN}$$

$$\text{so no of bolts by connected leg} = \frac{252.6}{28.97} \\ = 8.71 \approx 9 \text{ nos}$$

Design of lug angle - ^{strength} 1.2×147.368
 $= 176.8 \text{ kN}$

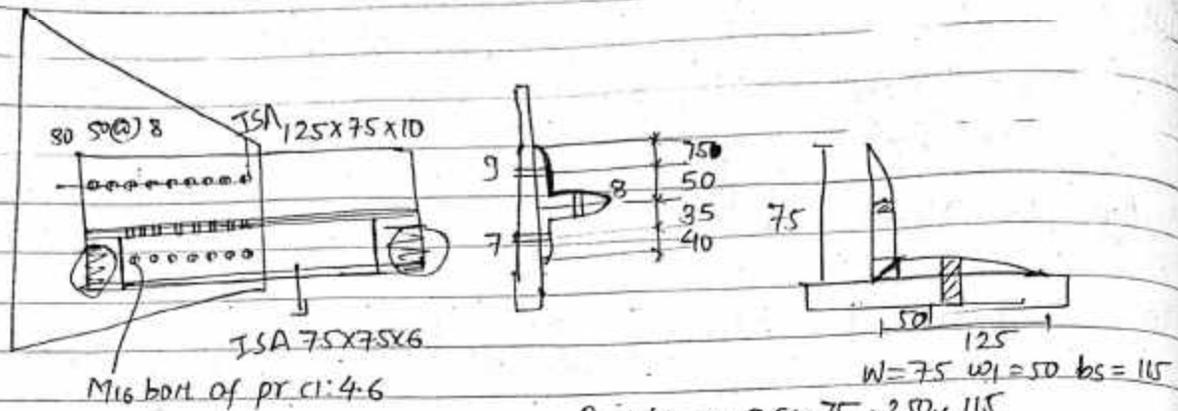
$$\text{area required for lug angle} = \frac{176.8 \times 10^3 \times 1.1}{250} \\ = 7.78 \text{ cm}^2$$

Select, lug angle: 75x75x6 mm of area 8.6 cm²

$$\text{no. of bolt, required for connect lug angle to gusset plate} \\ = \frac{176.8}{28.97} = 6.10 \approx 7 \text{ nos.}$$

$$\text{load, to be carried by connection both lug angle and main angle section} = 1.4 \times 147.368 \\ = 206.36 \text{ kN}$$

$$\therefore \text{no of bolts} = \frac{206.36}{28.97} = 7.14 \approx 8 \text{ nos.}$$



$$\beta = 1.40 - 0.076 \times \frac{75}{10} \times \frac{250}{410} \times \frac{115}{960}$$

$$= 1.30 (> 0.7) (< 1.44)$$

So $\beta = 1.30$

T_{dn} & T_{db} for main angle :-

For T_{dn}: $T_{dn} = \frac{0.9 A_{nc} f_u}{\gamma_{m1}} + \frac{\beta A_{g0} f_y}{\gamma_{m0}}$

$$= \frac{0.9 \times 2020 \times 410}{1.25} + \frac{1.30 \times 520 \times 250}{1.10}$$

$$= 454.74 > 400 \text{ kN OK!}$$

$$A_{nc} = (125 - 10 - 18) \times 10 = 930 \text{ mm}^2$$

$$+ \frac{1}{2} \times 30 \times 10 = 1020 \text{ mm}^2$$

$$A_{g0} = (75 - 10 - 18) \times 10 + 50 = 520 \text{ mm}^2$$

For T_{db}: $A_{vg} = (30 + 30 \times 8) \times 10 = 4300 \text{ mm}^2$

$$A_{vn} = (30 + 30 \times 8 - 7.5 \times 18) \times 10 = 2950 \text{ mm}^2$$

$$A_{tg} = 75 \times 10 = 750 \text{ mm}^2$$

$$A_{tn} = (75 - 0.5 \times 18) \times 10 = 660 \text{ mm}^2$$

So,

$$T_{db} = (131.21 A_{vg} + 295.2 A_{tn}) \text{ or } (17043 A_{vn} + 227.27 A_{tg})$$

$$= 759.035 \text{ or } 673.221$$

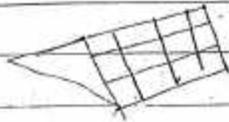
$$\therefore T_{db} = 673.221 > 400 \text{ kN (OK!)}$$

CH:7 Flexure member (14-16)

- Member under Bending moment as well as shear force as a major action
- it is generally a horizontal member

→ Types of flexure Member

1. Beam
2. Stringer
3. Lintel
4. Purlin
5. Rafter etc.



Section used in flexure member

- (i) Rolled - I-section
- (ii) wide flange beam
- (iii) Angle section
- (iv) channel "
- (v) tubular "
- (vi) Plate girder -
- (vii) BOX girder etc.



Types of section of flexure member: according to local buckling

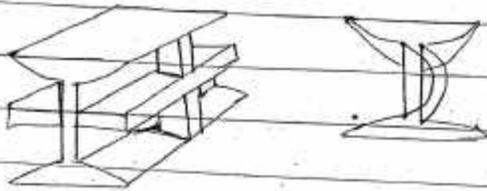
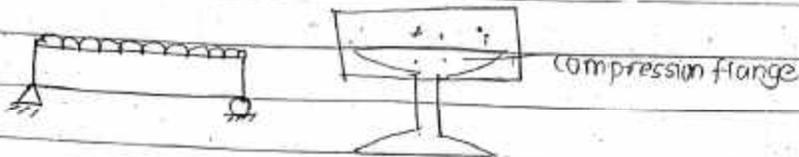
- (i) Plastic section Class - 1
- (ii) Compact " " - 2
- (iii) Semi-compact " " - 3
- (iv) Slender " " - 4

Elements of flexure member

- (i) outstanding
- (ii) Internal
- (iii) Tapered

Types of beam as per lateral support provided to compression flange

1. laterally supported
2. laterally unsupported.



laterally supported beam:-

Design steps

1) calculate effective length of beam: 8.1.1 page: 52

2) calculate total load

3) calculate max BM & Shear force

4) calculate plastic section modulus $Z_p = \frac{M_{max} \cdot \gamma_{mb}}{f_y}$

5. Select section such that $Z_p > Z_{required}$

Table 46 Page 138

6. ~~se~~ classify the section (tab. 2, page 18)

7. check for shear force (8.4.1 page 59)

8. " " B.M (8.2.1.2 page 53)

9. " " deflection (table: 5, page 31)

10. " " web buckling [8.4.2 page 59

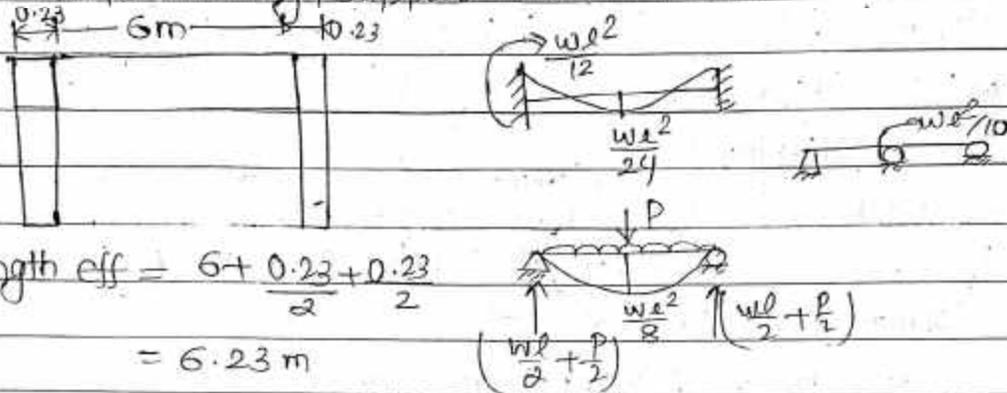
(8.7.3 page: 67)

11: check for web crippling clause 8.7.4 page: 67

Design a beam section having 6m clear span carrying a UDL of 46 kN/m. Compression flange is laterally supported throughout the section. use Fe 410

Soln:-

① Step 1: Adopt bearing / support width 230 mm



2. Step: 2 load calculation:

① UDL = 46 kN/m

② self wt = 1 kN/m (assume) always

∴ Total wt = 47 kN/m

factored UDL = 47×1.5
 $= 70.5 \text{ kN/m}$

Step: 3 B.M = $\frac{wL^2}{8} + \frac{PL}{4}$ (no center load)
 $= \frac{70.5 \times 6.23^2}{8}$
 $= 342.038 \text{ kNm}$

Step: 4 $V_{max} = \frac{wL}{2} + \frac{P}{2}$
 $= \frac{70.5 \times 6.23}{2}$
 $= 219.606 \text{ kN}$

Step: 5 $Z_p(\text{req}) = \frac{M_{max} \cdot \gamma_{m0}}{f_{yz}}$ $= \frac{342.038 \times 10^6}{250}$
 $= 1.504 \times 10^6 \text{ mm}^3$
 $= 1504 \text{ cm}^3$

Step: 6: select, ISMB 450 $Z_p = 1533.86 \text{ cm}^3 > Z_p \text{ required.}$

Then,

$$I_{xx} = 30400 \text{ cm}^4$$

$$I_{yy} = 839 \text{ cm}^4$$

$$t_f = 17.4 \text{ mm}$$

$$t_w = 9.4 \text{ mm}$$

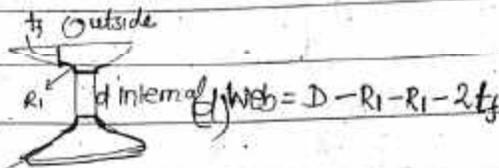
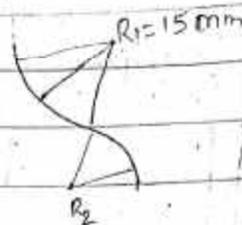
$$h = D = 450 \text{ mm} = 450 \text{ mm}$$

$$B = 150 \text{ mm} = 150 \text{ mm}$$

$$Z_{cx} = 1350 \text{ cm}^3$$

$$r_x = 182 \text{ mm}$$

$$r_y = 301 \text{ mm}$$



For outstanding element of compression flange
for rolled section

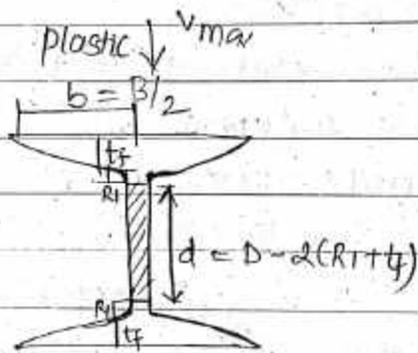
$$\frac{b}{t_f} = \frac{75}{17.4} = 4.33 \leq 9.4 \epsilon$$

$$b = \frac{B}{2} = \frac{150}{2} = 75$$

$$d = D - 2(R_1 + t_f)$$

$$= 450 - 2(15 + 17.4)$$

$$= 385.2 \text{ mm}$$



$$\frac{d}{t_w} = \frac{385.2}{9.4} = 40.98 \leq 84 \epsilon \text{ (plastic) (Neutral axis at mid depth)}$$

Hence, the section is plastic.

Step: 7: 8.4.1

$$V_d = \frac{A_v f_y}{\sqrt{3} \gamma_{m0}} = \frac{h t_w \times f_y}{\sqrt{3} \times 1.10} = \frac{450 \times 9.4 \times 250}{\sqrt{3} \times 1.10}$$

$$= 555.34 \text{ kN} > 219.6 \text{ kN (OK)}$$

$$V_d^l = 0.6 V_d$$

$$= 0.6 \times 555.34$$

$$= 333.206 \text{ kN} > 219.6 \text{ so, it is low shear case}$$

< 219.6 High shear case

Page: 53

Step: 8 :

$$M_d = \frac{\beta_b Z_p f_y}{\gamma_{mo}}$$

$$= \frac{1.0 \times 1533.36 \times 10^3 \times 250}{1.10} \leq \frac{1.2 Z_{ex} f_y}{\gamma_{mo}}$$

$$\leq \frac{1.2 \times 1350 \times 16^3 \times 250}{1.10}$$

$$= 3485 \text{ kN-m} \leq 368.18 \text{ kN-m}$$

$$\therefore M_d = 348.5 \text{ kN-m} \geq 342.03 \text{ kN-m}$$

Step: 9: $\delta = \frac{5 \text{ WL}^4}{384 EI_x} + \frac{D L^3}{48 EI_x}$ ^{not factored load}

$$= \frac{5 \times 700^4}{384 \times 2 \times 10^5 \times 30460 \times 10^2}$$

$$= 22.74 \text{ mm}$$

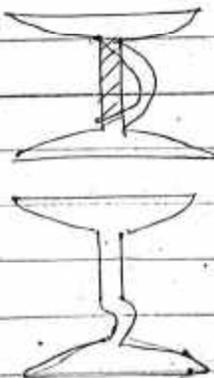
$$= 15.163 \text{ mm}$$

Step: 10: $\delta_{per} = \frac{\text{Span}}{360}$ for brittle

$$= \frac{6230}{300}$$

$$= 20.76 \text{ mm} >> 15.163 \text{ mm (OK!)}$$

Step: 10:



$$d = 40.98 \leq 67 E$$

tw

no need of web buckling check,

(page 59) 8.4.2

otherwise we have to check

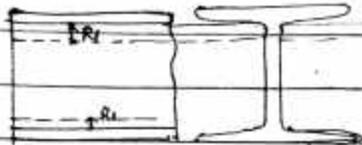
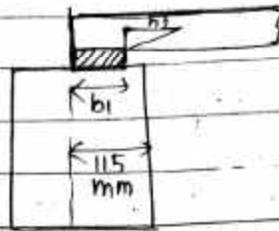
$$\text{if } \frac{d}{tw} > 67 E$$

Step: II web crippling

stiff bearing length (b_1)
= 100 mm

$$n_2 = 2.5(t_f + R_1)$$

$$= 2.5(17.4 + 15) = 81 \text{ mm}$$



$$\therefore F_w = \frac{(b_1 + h_2) t_w \times f_y}{\gamma_{m0}}$$

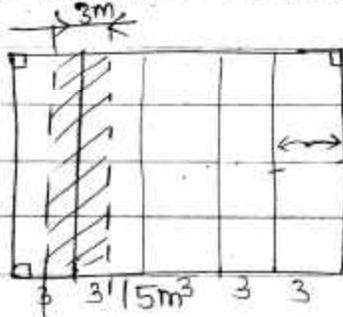
$$= \frac{(100 + 81) \times 9.4 \times 250}{1.10}$$

$$= 386.681 \text{ kN} \geq V_{max}$$

$$= 386.681 \text{ kN} \geq V_{max}$$

Design a steel beam of 6m span supporting a slab of 150 mm (RCC) which is provided with floor finish (punning) of 25mm, it also supports a live load of 6 kN/m^2 . The beam is provided at 3m c-c spacing in a hall of $6 \times 15 \text{ m}$. The beam is laterally supported throughout the span.

Soln:-



$$\gamma_{RCC} = 25 \text{ kN/m}^3, \gamma_{PCC} = 24 \text{ kN/m}^3$$

end beam \uparrow half load

intermediate, full load

critical \uparrow \downarrow

Step 1:- Assume support width = 230 mm

$$l_{eff} = 6 + 0.23$$

$$= 6.23 \text{ m}$$

$$= 6230 \text{ mm}$$

Step 2: load calculation

$$\text{(i) Slab load} = \gamma_{RCC} \times V = 25 \times 3 \times 0.15 \times \frac{6.23}{6.23} = 11.25 \text{ kN/m}$$

$$\text{(ii) floor finish} = 24 \times 3 \times 0.025 \times \frac{6.23}{6.23} = 1.8 \text{ kN/m}$$

$$\text{(iii) live load} = 6 \times 3 \times \frac{6.23}{6.23} = 18 \text{ kN/m}$$

$$\text{self load} = 1 \text{ kN/m}$$

$$\text{Total load} = 32.05 \text{ kN/m}$$

$$\therefore \text{factored load} = 48.075 \text{ kN/m}$$

$$\text{Step: 3 } BM = \frac{wL^2}{8} + \frac{P \cdot L}{4}$$

$$= 233.241 \text{ kN-m}$$

$$\text{Step 4: } V_{\text{max}} = \frac{wL}{2} + \frac{P}{2}$$

$$= \frac{48.075 \times 6.23}{2}$$

$$= 152.965 \text{ kN}$$

$$= 149.753 \text{ kN}$$

Step: 5

$$Z_p(\text{req}) = \frac{M_{\text{max}} \cdot \gamma_{m0}}{f_y}$$

$$= \frac{233.241 \times 1.10}{250}$$

$$= 1026.2 \text{ cm}^3$$

Step: 6 select: ISMB 400 $Z_p = 1176.18 \text{ cm}^3 > Z_{p \text{ required}}$

Then

$$I_{xx} = 20500 \text{ cm}^4$$

$$I_{yy} = 622 \text{ cm}^4$$

$$t_f = 16 \text{ mm}$$

$$t_w = 8.9 \text{ mm}$$

$$h = D = 400 \text{ mm}$$

$$B = 140 \text{ mm}$$

$$Z_{xx} = 1020 \text{ cm}^3$$

$$r_x = 162 \text{ mm}$$

$$r_y = 28.2 \text{ mm}$$

$$t_1 = 14 \text{ mm}$$

for outstanding element of compression flange
for rolled section

$$\frac{b}{t_f} = \frac{B}{2t_f} = \frac{140}{2 \times 16} = \frac{70}{16} = 4.3 \leq 9.4 \epsilon \quad (\text{plastic})$$

$$d = D - 2(t_f + r_1) = 400 - 2(16 + 14) \\ = 400 - 60 \\ = 340 \text{ mm}$$

$$\frac{d}{t_w} = \frac{340}{2.9} = 38.20 \leq 84 \epsilon \quad (\text{plastic})$$

Hence, section is plastic.

Step: 7.

$$V_d = \frac{A_g f_y}{\sqrt{3} r_{mo}} = \frac{h t_w f_y}{\sqrt{3} \times 1.10} = \frac{400 \times 8.9 \times 250}{\sqrt{3} \times 1.10} \\ = 467.128 \text{ kN} > V_{max}$$

$$V_d^1 = 0.6 V_d = 280.277 \text{ kN} > V_{max} \quad \checkmark \quad \text{low shear case}$$

$$\text{Step: 8} \quad M_d = \frac{P_b \times Z_p f_y}{\gamma_{mo}} = \frac{1 \times 1176.18 \times 250}{1.10} \leq \frac{1.2 \times 1020 \times 250}{1.10} \\ = 267.295 \leq 278.181$$

$$\therefore M_d = 267.295 \text{ kN-m} \geq 233.241 (\text{OK!})$$

Step: 9:

$$f = \frac{5 w l^4}{348 E I_x} + \frac{p l^3}{48 E I_x} \\ = \frac{5}{348} \times \frac{32.05 \times 6230^4}{2 \times 10^5 \times 20500}$$

alternatively:

assume, $V = 300 \text{ kN} < 467.128 \text{ kN OK!}$

$$V' = 0.6Vd = 280.216 < 300 \text{ (High shear case)}$$

8.2.1.3 for High shear case
step: 8

$$M_{dv} = M_d - \beta(M_d - M_{fd}) \leq \frac{1.2 Z_{ex} f_y}{\gamma_{m0}}$$

$$M_d = \frac{F_0 Z_p f_y}{\gamma_{m0}} = 267.314 \text{ kN}$$

$$\beta = \left(\frac{2V}{Vd} - 1 \right)^2 = \left(\frac{2 \times 300}{467.128} - 1 \right)^2$$
$$= 0.0809$$

$$M_{fd} = \frac{Z_{fd} \times f_y}{\gamma_{m0}}$$

$$Z_{fd} = Z_p - 2 \left[\frac{D}{2} \times t_w \times \frac{D}{4} \right] \times 10^3$$

=

$$= 820.18 \text{ cm}^3$$

$$\therefore M_{fd} = \frac{820.18 \times 250}{1.10} = 186.405 \text{ kN-m}$$

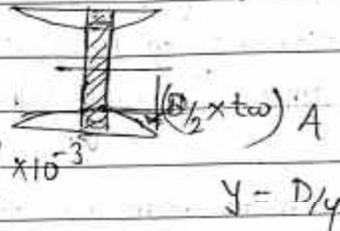
$$\therefore M_{dv} = 267.314 - 0.0809 (267.314 - 186.405)$$

$$= 260.77$$

$$\leq \frac{1.2 \times 1020 \times 250}{1.10}$$

$$\leq 278.181 \text{ kN}$$

$$\therefore M_{dv} = 260.77 \geq M_{max}$$



Design a steel beam of span 7m ^(less) carrying a total UDL of 30 kN/m including self wt. depth of beam is restricted to 300mm & laterally supported throughout.

soln:-

Step 1: $l_{eff} = 7m$

Step 2: load calculation

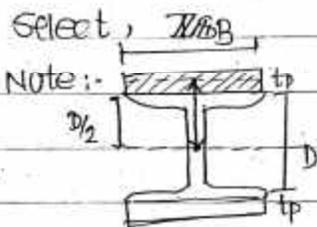
$$\text{Total UDL} = 30 \text{ kN/m}$$

$$\text{factored " } = 30 \times 1.5 \\ = 45 \text{ kN/m}$$

Step 3: $V_{max} = \frac{Wl}{2} = \frac{45 \times 7}{2} = 157.5 \text{ kN}$

$$M_{max} = \frac{Wl^2}{8} = \frac{45 \times 7^2}{8} = 277.625 \text{ kNm}$$

Step 4: $Z_p(\text{required}) = \frac{M_{max} \cdot \gamma_{m0}}{f_y} = \frac{277.625 \times 1.10}{250} \\ = 122.75 \text{ cm}^3$



if $Z_{p \text{ req}} > Z_p$

$$Z_{\text{plate}} = Z_{p \text{ req}} - Z_p$$

$$Z_{\text{plate}} = 2 \times (B \times t_p) \times \left(D/2 + \frac{t_p}{2} \right)$$

$$= 2 A X y$$

$$\therefore t_p = \frac{Z_{\text{plate}}}{B \cdot D}$$

$$\text{thickness of extra plate} = \frac{Z_{\text{plate}}}{B \cdot D}$$

for ISMB 250

$$Z_p = 465.71 \text{ cm}^3 \quad Z_{ex} = 410 \text{ cm}^3$$

$$I_{xx} = 530 \text{ cm}^4 \quad D = 250 \text{ mm}$$

$$I_{yy} = 335 \text{ cm}^4 \quad B = 125 \text{ mm}$$

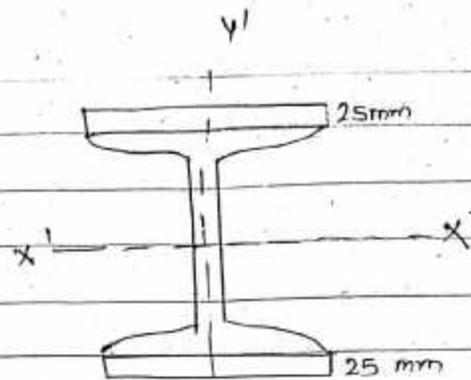
$$r_1 = 13 \text{ mm} \quad t_f = 12.5 \text{ mm}$$

$$t_w = 6.9 \text{ mm}$$

$$\begin{aligned}
 Z_{\text{plate}} &= Z_{\text{req}} - Z_p \\
 &= 1212.75 - 465.71 \\
 &= 747.04
 \end{aligned}$$

$$\begin{aligned}
 \therefore t_p &= \frac{Z_{\text{plate}}}{B.D} = \frac{747.04}{250 \times 125} \\
 &= 2.39 \text{ cm}
 \end{aligned}$$

∴ 2.5 cm



$$I_{xx'} = [I_{xx} + Ah^2]_{MB} + [I_{xx} + Ah^2]_{\text{plate} \times 2}$$

$$\begin{aligned}
 &= (5130 + 0) + \left[\frac{12.5 \times 2.5^3}{12} + 12.5 \times 2.5 \times \left(\frac{2.5}{2} + \frac{2.5}{2} \right)^2 \right] \times 2 \\
 &= 16978.96 \text{ cm}^4
 \end{aligned}$$

$$\begin{aligned}
 Z_{xx'} &= \frac{I_{xx'}}{y_{max}} = \frac{16978.96}{15} \\
 &= 1131.93 \text{ cm}^3
 \end{aligned}$$

$$Z_p' = (Z_p)_{MB} + (Z_p)_{\text{plate}}$$

$$\begin{aligned}
 &= 465.71 + 2 \times 12.5 \times 2.5 \times \left(12.5 + \frac{2.5}{2} \right) \\
 &= 1325.086 \text{ cm}^3 > 1212.75 \text{ cm}^3 \text{ OK!}
 \end{aligned}$$

अब जहाँ Value use जहाँ

Shear area - web की area मात्र

no need to check high / low shear.

$$\eta_2 = 2.5 (f_f + R_1 + t_p)$$

Flexure Member:

laterally unsupported beam:

→ Torsional Buckling, hence flexural capacity in calculate considering the effect

Bending capacity is calculated as 8.2.2

Design laterally unsupported beam of span 3.5m carrying UDL of 20 kN/m including self wt.

Step 1: assume 230 mm support beam

$$l_{eff} = 3.5 + 0.23 \\ = 3.73 \text{ m}$$

Step 2: load calculation: UDL = 20 kN/m

$$\text{Factored UDL} = 20 \times 1.5$$

$$= 30 \text{ kN/m}$$

$$\text{Step 3: } V_{max} = \frac{wL}{2} = \frac{30 \times 3.73}{2} = 52.5 \text{ kN}$$

$$M_{max} = \frac{wL^2}{8} = \frac{30 \times 3.73^2}{8} = 52.17 \text{ kN-m}$$

$$\text{Step 4: } Z_{p(req)} = \frac{M_{max} \gamma_{mo}}{f_y} \\ = \frac{52.17 \times 1.10 \times 10^6}{250} \\ = 229.548 \text{ cm}^3$$

Step 5: select section such that,

$$Z_p \geq 1.5 Z_{p(req)}$$

Page 138.

$$\text{ZSMB 250 } \cdot Z_p = 465.71 \text{ cm}^3$$

$$I_{xx} = 5130 \text{ cm}^4$$

$$B = b_f = 125$$

$$I_{yy} = 335 \text{ cm}^4$$

$$t_f = 12.5$$

$$r_x = 104 \text{ mm}$$

$$f_w = 6.9$$

$$r_y = 26.5 \text{ mm}$$

$$Z_{ex} = 10.8$$

$$B = h = 250 \text{ mm}$$

$$R_1 = 13 \text{ mm}$$

Step: 6

$$b = \frac{B}{2} = \frac{125}{2} = 62.5 \text{ mm}$$

$$d = 250 - 2(12.5 + 13) \\ = 199 \text{ mm}$$

$$\frac{b}{t_f} = \frac{62.5}{12.5} = 5 \leq 9.4 \epsilon \quad \text{plastic}$$

$$\frac{d}{t_w} = \frac{199}{6.9} = 28.8 \leq 84 \epsilon \quad \text{plastic}$$

Section is plastic:

Step: 7:

$$V_d = \frac{A_v f_y}{\sqrt{3} s_{mo}} = \frac{250 \times 600 \times 250}{\sqrt{3} \times 110} = 226.347 \geq 55.95 \text{ KN. OK!}$$

Step: 8 Page 54. 8.2.2

$$G = \frac{E}{2(1+\mu)} \quad [\mu = 0.3]$$

$$G = \frac{2 \times 10^5}{2 \times 1.3} = 76923.07 \text{ N/mm}^2$$

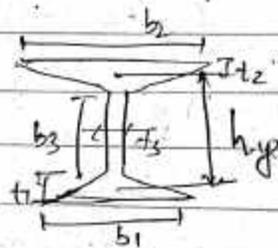
$$I_w = (1 - \beta_f) \beta_f I_y \cdot h_y^2$$

$$\beta_f = \frac{I_{fc}}{I_{fc} + I_{ft}} = \frac{1}{2}$$

$$h_y = 250 - t_f = 250 - 12.5 = 237.8 \text{ mm}$$

$$I_w = (1 - 0.5) \times 0.5 \times 335 \times \left(\frac{237.8}{10}\right)^2 \\ = 47240.234 \text{ cm}^4$$

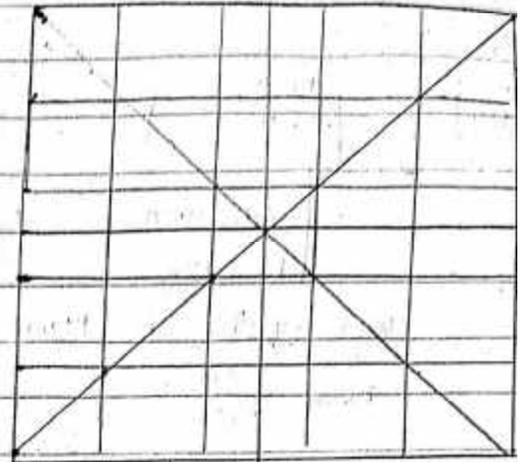
$$I_t = \frac{\sum b_i t_i^3}{3} = \frac{2 \times 12.5 \times 125^3}{3} + \frac{225 \times 6.9^3}{3} \\ = 187398.592 \text{ mm}^4$$



Page: 58

$$\begin{aligned}L_{LT} &= 0.7 \times L \\ &= 0.7 \times 3.73 \\ &= 2.611 \text{ m}\end{aligned}$$

$$\begin{aligned}M_{cr} &= \sqrt{\left\{ \frac{\pi^2 EI_y}{(L_{LT})^2} \left[GJ_t + \frac{\pi^2 EI_w}{L_{LT}^2} \right] \right\}} \\ &= 1.65 \times 10^8\end{aligned}$$



$$\lambda_{LT} = 0.84 \leq 0.86 \quad \lambda_{LT} = 0.84$$

$$\alpha_{LT} = 0.21$$

$$\phi_{LT} = 0.92$$

$$\chi_{LT} = 0.7721$$

$$f_{bd} = \frac{\chi_{LT} \cdot f_y}{\gamma_{m0}} = 175.468 \text{ N/mm}^2$$

$$\begin{aligned}M_d &= B_d Z_p f_{bd} = 1 \times 465.71 \times 175.468 \times 10 \\ &= 81.7 \geq 52.17\end{aligned}$$

$$\text{Step: 9} \quad \delta_{max} = \frac{5 \cdot w \cdot l^4}{384 \cdot EI}$$

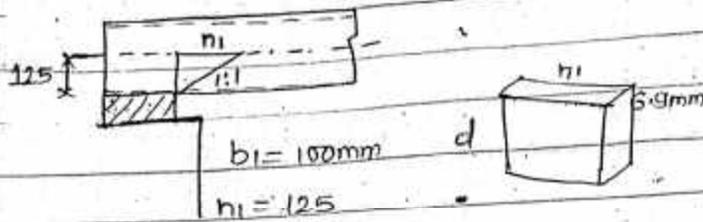
$$= 4.91 \text{ mm}$$

$$\delta_{per} = \frac{3.73 \times 10^3}{300}$$

$$= 12.433 \text{ mm} > 4.91 \text{ OK!}$$

$$\text{Step: 10: } \frac{d}{t_w} = 28.84 \leq 67 \text{ E}$$

no need to check web buckling



$$\text{web length} = d = 199 \text{ mm}$$

$$r_{\min} = \frac{t_w}{\sqrt{12}} = \frac{6.9}{\sqrt{12}} = 1.99 \text{ mm}$$

$$\lambda = \frac{0.7d}{r_{\min}} = \frac{0.7 \times 199}{1.99} = 70$$

Buckling class C

$$f_{cd} = 152 \text{ N/mm}^2$$

Ans 8.7.3 ली गिवा

$$\begin{aligned} \therefore \text{load carrying capacity} &= f_{cd} \times A \\ &= 152 \times (b_1 + h_1) \times t_w \\ &= 152 (225) \times 6.9 \\ &= 235.98 \text{ kN} \end{aligned}$$

Step: II stiff bearing length = $b_1 = 100$

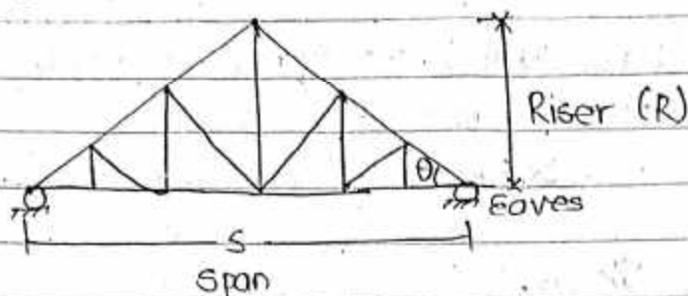
$$\begin{aligned} \text{load dist}^n \text{ along } H_3: n_2 &= 20(t_f + r_1) \\ &= 20(12.5 + 13) \\ &= 63.75 \text{ mm} \end{aligned}$$

$$\begin{aligned} \text{vertically} &= 1 \times (r_1 + t_f) \\ &= 1(13 + 12.5) \\ &= 25.5 \text{ mm} \end{aligned}$$

$$\begin{aligned} t_w &= \frac{(b_1 + n_2) \times t_w \times f_{yw}}{r_{m0}} = \frac{(100 + 63.75) \times 6.9 \times 250}{1.10} \\ &= 196.806 \geq V_{\max} \text{ ok} \end{aligned}$$

CH-8 Roof truss:

If we need a large space without column, then it is provided with truss. They are under action of wind load.



Pitch (p): it is a ratio of riser to span. Generally taken as $(\frac{1}{6})$
economical spacing is when, $t = p + r$

t = cost of truss

p = cost of purlin

r = cost of roofing material

Dead load: Dead load of truss & roofing materials [IS-875] part 1

① Generally taken as $(20 + 6.6L) \text{ N/m}^2$

When $LL \leq 2 \text{ kN/m}^2$

② it is multiplied by $(\frac{LL}{2})$ if $LL > 2 \text{ kN/m}^2$

live load = (LL) (IS-875) part: 2

live load on roof

Inaccessible = 0.75 kN/m^2 for 10° slope (θ), it is decrease by 0.02 kN/m^2

Accessible = 1.5 kN/m^2

[for every degree rise in θ]

3) Wind load (IS 875) Part 3 [NBC-104]

Basic wind speed (Annex A)

① NBC gives the ^{two} basic distinct basic wind velocity in case of Nepal.

47 m/s - ht from MSL \leq 3000m

55 m/s - " " " \geq 3000m

② Design wind speed (V_d) = $V_b k_1 k_2 k_3$

$$V_d = k_1 k_2 k_3 V_b$$

(Risk factor) k_1 = table 1 - life expectancy & V_b

k_2 = Terrain factor Tab. 2

k_3 = Topographic " [Annex-c]

③ Pressure calculation: at roof (P) = $0.6 V_d^2 \cdot N/m^2$

iv) Design pressure (P_d) = $(C_{pe} - C_{pi}) P_d$

\therefore force = $P_d \times A$

[6.2.3] C_{pe} = external pressure coeff] table (4+1) = 5
page 27 C_{pi} = internal " "]
= ± 0.2 [permeability $\leq 5\%$] normal permeability
= ± 0.5 [5 to 20%]
= ± 0.7 [permeability $> 20\%$]

Wind p_i

calculate wind pressure on a roof truss having height to eaves 12m located in central km and designed life expectancy of 50 yr & having total Ht of truss from ground of 15m, span of truss 20m. Max dimension of building is 40m

Soln:-

1) basic wind speed, $V_b = 47 \text{ m/s}$ [MSL ^{Ht above} < 3000]

2) designed wind speed $V_d = k_1 k_2 k_3 V_b$

$$k_1 = 1$$

terrain category = 3

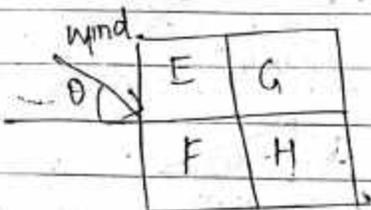
Eaves Height = 12m, class: B

Height	k_2
10	0.88
15	0.94
12	0.904

$$\therefore k_2 = 0.904$$

$$k_3 = 1$$

$$\therefore V_d = 1 \times 0.904 \times 1 \times 47 = 42.488 \text{ m/s}$$



3) wind pressure (P) = $0.6 V_d^2$
 $= 1083.13 \text{ N/m}^2$

$$\therefore P_d = (C_{pi} - C_{pe}) P$$

$C_{pi} = \pm 0.2$ [for normal permeability]

$C_{pe} \Rightarrow$

$$\frac{h}{w} = \frac{12}{20} = 0.6 > 0.5$$

Case (i)

$$\theta = \tan^{-1} \left(\frac{3}{10} \right) = 16.69^\circ$$

	EF	GH	GG	FH
C_{pe}	-0.8324	-0.5331	-0.8	-0.60
C_{pi}	+2	+2	+2	+2

P_d

$$C_{pi} = +0.2$$

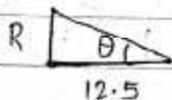
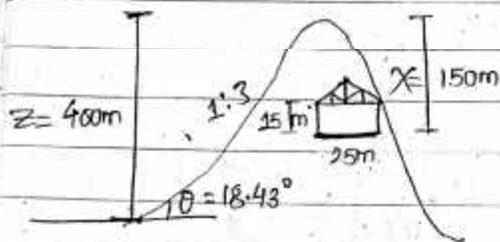
$P_d (EF) = -1118.88$ Mpa
$P_d (GH) = -793.94$ "
$P_d (EG) = -1083.138$ "
$P_d (FH) = -866.51$ "

$$C_{pi} = -0.2$$

$P_d (EF) = -684.543$ Mpa
$P_d (GH) = -360.682$ "
$P_d (EG) = -649.882$ "
$P_d (FH) = -433.255$ "

So, $P_d = 1118.88$ Mpa

Calculate wind pressure on a roof of a building located at chandragiri having ht to top from bottom of hill is 400m and avg slope of 1:3, building is located at 150m downward from the crest, permeability of building is normal & having life expectancy of 100 yrs. Ht of building is 15m to the eaves & pitch of $\frac{1}{4}$ with span of truss 25m



$$\frac{R}{12.5} = \frac{1}{4}$$

$$\therefore R = \frac{12.5}{4} = 3.125m$$

soln:-

$$(i) V_b = 47 \text{ m/s}$$

$$(ii) V_d = k_1 k_2 k_3 V_b$$

$$k_1 = 1.07$$

$$k_2 = 0.97 \text{ for Terrain category 2}$$

Building class C

$$k_3 = 1 + CS$$

$$\theta > 17^\circ \text{ so } C = 0.36$$

$$z = 400m$$

$$H = 15m$$

$$X = 150m$$

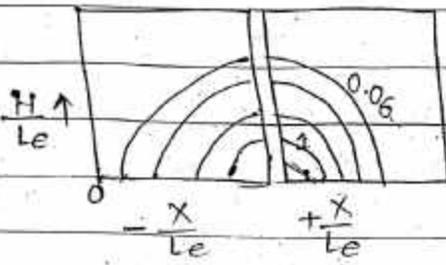
$$le = \frac{z}{0.3} \text{ for } \theta > 17^\circ$$

$$= \frac{400}{0.3}$$

$$= 1333.33m$$

$$\frac{x}{L_e} = \frac{150}{1333.33} = 0.1125$$

$$\frac{H}{L_e} = \frac{15}{1333.33} = 0.01125$$



$$\therefore S = 1$$

$$\therefore k_3 = 1 + 0.36 \times 1$$
$$= 1.36$$

$$\therefore v_d = 1.07 \times 0.97 \times 1.36 \times 47$$
$$=$$

Design of purlin

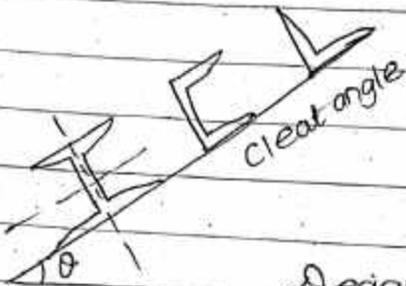
It is a inclined section placed horizontally on the roof of truss

There are 3 section particularly used in purlins.

I-section

Channel section

Angle section.



Design both direction MA moment आउरुं
combined action check सिर्

Design of I section & channel section purlin

- i) calculate effective length
- ii) calculate total load
- iii) calculate max. BM and SF
- iv) calculate Plastic section modulus required,

$$Z_{p, req} = \frac{M_z \delta_{m0}}{f_y} + 2.5 \left(\frac{d}{b}\right) \times \frac{M_y \delta_{m0}}{f_y}$$

$$\text{take, } \left(\frac{d}{b}\right) = 2$$

v) select section such that $Z_p > Z_{p, req}$.

vi) Section classification

vii) check for shear force

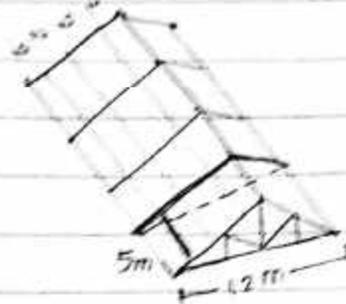
viii) check for BM

ix) check for deflection

x) check for combined bending. $\left(\frac{M_z}{M_{dz}} + \frac{M_y}{M_{dy}}\right) \leq 1.0$

Design I section purlin for following data:

- ① span of truss = 12m
- ② spacing of truss = 5m
- slope of roof = 30°
- wind load = 1.5 kN/m^2
- Dead load = 200 N/m^2
- live load = 0.75 kN/m^2



Step: 1. Effective length of purlin = 5m

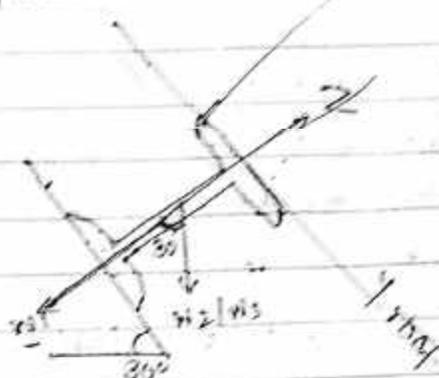
Step: 2: load calculation

$$w_1 = 1.5 \times 2 \text{ kN/m}$$

$$= 3 \text{ kN/m}$$

$$w_2 = 0.2 \times 2 = 0.4 \text{ kN/m}$$

$$w_3 = 0.75 \times 2 = 1.5 \text{ kN/m}$$



$$\text{factored load along Z axis} = [w_1 + (w_2 + w_3) \cos 30^\circ] \times 1.5$$

$$= 6.97 \text{ kN/m}$$

$$\text{factored load along Y axis} = (w_2 + w_3) \sin 30^\circ \times 1.5 = 1.428 \text{ kN/m}$$

$$\text{step: 3. } M_z = \frac{w_z l^2}{10}$$

$$= \frac{6.97 \times 5^2}{10}$$

$$= 17.425 \text{ kN-m}$$

$$M_y = \frac{w_y l^2}{10}$$

$$= \frac{1.428 \times 5^2}{10} = 3.563 \text{ kN-m}$$

$$\text{step: 4. } Z_{p \text{ req}} = \frac{M_z \gamma_{mo}}{f_y} = \frac{17.425 \times 10^6 \times 1.10}{250} + \frac{5 \times 3.563 \times 10^6 \times 1.10}{250}$$

$$= 155.5 \text{ cm}^3$$

take ISMB 200 having $Z_p = 253.86 \text{ cm}^3$

$$h = 200 \text{ mm}$$

$$b_f = 100 \text{ mm}$$

$$t_w = 6.7 \text{ mm}$$

$$t_f = 10.0 \text{ mm}$$

$$I_{xx} = 2120 \text{ cm}^4$$

$$R_1 = 11 \text{ mm}$$

$$Z_z = Z_{ex} = 212.4 \text{ cm}^3$$

$$Z_{cy} = 27.4 \text{ cm}^3$$

Step: 6: $b = \frac{100}{2} = 50 \text{ mm}$

$$d = 200 - 2(t_f + R_1)$$

$$= 200 - 2(10 + 11)$$

$$= 158$$

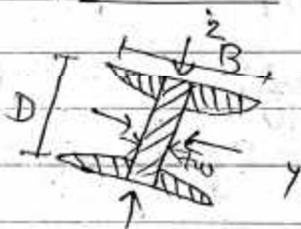
$$\frac{b}{t_f} = \frac{50}{10} = 5 \leq 9.4 \epsilon \quad (\text{plastic})$$

$$\frac{d}{t_w} = \frac{158}{6.7} \leq 27.7 \leq 84 \epsilon \quad (\text{plastic})$$

Step: 7:

$$V_z = \frac{W_z L}{2} = \frac{6.97 \times 5}{2} = 17.42 \text{ kN}$$

$$V_y = \frac{W_y L}{2} = \frac{1.42 \times 5}{2} = 3.55 \text{ kN}$$



$$V_{dz} = \frac{A_v f_y}{\sqrt{3} \times 110} = \frac{D \times t_w \times 250}{\sqrt{3} \times 110}$$

$$= 49.5 > 17.42 \text{ kN} \quad \text{OK!}$$

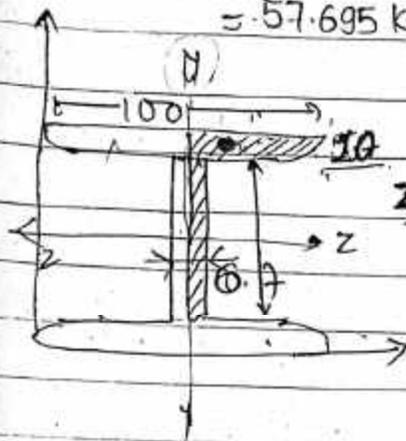
$$V_{dy} = 2 \frac{A_v f_y}{\sqrt{3} \times 110} = \frac{B \times t_f \times 250 \times 2}{\sqrt{3} \times 110}$$

$$= 209.91 = 262.431 \text{ kN} > 3.55 \text{ kN} \quad \text{OK!}$$

(1 x 9)

$$M_{dz} = \frac{B_b \times Z_{pz} \times 10^3 \times 250}{1.1}$$

$$= 57.695 \text{ kN-m} > 17.42 \text{ kN-m } Z_{py}$$



$$Z_{py} = Z_{py} = 4 \left(\frac{B \cdot t_f}{2} \cdot \frac{B}{4} \right) + 2 \times \left[(D - 2t_f) \cdot \frac{t_w}{2} \times \frac{t_w}{4} \right]$$

$$= 4 \times \left(\frac{100}{2} \times 10 \times \frac{100}{4} \right) + 2 \times \left[(200 - 2 \times 10) \times \frac{6.7}{2} \times \frac{6.7}{4} \right]$$

$$= 51462.05 \text{ mm}^3$$

$$= 51.462 \text{ cm}^3$$

$$\therefore M_{dy} = \frac{51.46 \times 10^3 \times 250}{1.10}$$

$$= 11.681 \text{ kN-m}$$

Step: 9: $\delta = \frac{5}{384} \times \frac{W L^4}{EI}$

$$= 13.37 \text{ mm}$$

$$\delta_{per} = \frac{l}{180} = \frac{5000}{180} = 27.77 \text{ mm} > \delta \text{ (OK!)} \quad \begin{matrix} \text{Ten} \\ (21) \end{matrix}$$

Step: 10:

$$\left(\frac{M_z}{M_{dz}} + \frac{M_y}{M_{dy}} \right) \leq 1.0$$

$$\left(\frac{17.42}{57.69} + \frac{3.563}{11.681} \right) \leq 1.10$$

$$\therefore 0.61 \leq 1.10 \text{ OK!}$$

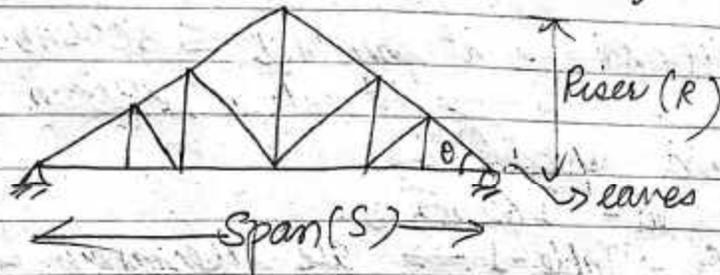
Same quest but use channel section:-

समस्या :- Z_p हैन। Z_x साँ compare जौँ

Z_{pz} } calculate जौँ
 Z_{py} }

Roof truss Chapter - 8

→ If we need a large space without column then it is provided with steel truss. Truss under the action of wind load



→ pitch (p) :- It is a ratio of riser to span. Generally taken as $\left(\frac{1}{6}\right)$

→ Economical spacing is when $t = p + \gamma$

$t =$ cost of truss

$p =$ " " purlin

$\gamma =$ " " roofing material

* Dead load (IS 875 part-1)

Dead load of truss and roofing material

Generally taken as $(20 + 6.6L) \text{ N/m}^2$, where live load (LL) $\leq 2 \text{ kN/m}^2$

It is multiplied by $\left(\frac{LL}{2}\right)$ if $LL > 2 \text{ kN/m}^2$

→ live load (LL) (IS-875 part 2)

live load on roof

(i) Inaccessible $= 0.75 \text{ kN/m}^2$

(ii) Accessible $= 1.5 \text{ kN/m}^2$

for 10° slope (θ), it decreases by 0.02 kN/m^2 for every degree rise in θ .

$L = S$

Wind load (IS-875 part 3) (NBC-104)
→ Basic wind speed (Annex A) (V_b).
NBC gives two distinct basic wind velocity in case of Nepal.

47m/sec → ht. from MSL ≤ 3000 m.

55m/s → ht. from MSL > 3000 m

Design wind speed (V_d)

$$V_d = K_1 K_2 K_3 V_b$$

Risk coefficient $K_1 =$ Table-1 → life expectancy & V_b .

$K_2 =$ Terrain factor (Table-2)

$K_3 =$ topographic factor (Annex-C)

→ Pressure on roof (P) = $0.6 V_d^2$ Pascal or N/m^2

→ Design pressure on roof (P_d) = $(C_{pe} - C_{pi}) P_0$

force = $P_d \times A$

where C_{pe} → external pressure coefficient

(6.2.6) C_{pi} → internal " Table 5

(6.2.3.1)

(6.2.8.2) $C_{pi} = \pm 0.2$ (permeability = 5%)

↳ Normal Permeability

= ± 0.5 (Permeability 5% to 20%)

= ± 0.7 (" " (>20%))

Q) Calculate wind pressure on a roof truss having height to eaves; 12m located in central Kathmandu and designed life expectancy of 50 years and having total height of truss from ground of 15 meters. Span of truss is 20m. Maximum dimension of building = 40m.

Solⁿ :- Basic wind speed (V_b) = 47 m/sec

(Table 2), Pg. 8 \rightarrow (eave height) $K_1 = 1$. (Table 1.)
 Terrain category 3. K_2
 Page 11. \rightarrow class B \rightarrow dimension (20m to 50m)

Height	10	0.91	0.88
	15	0.97	0.94

$$\frac{10-15}{0.88-0.94} = \frac{12-15}{x-0.94}$$

$$x = 0.904$$

$K_3 = 1 \rightarrow$ generally 1.

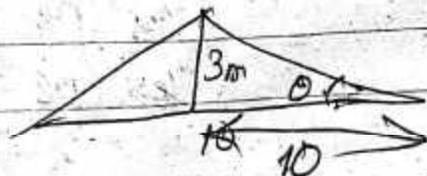
$$\begin{aligned} \text{Design wind pressure (} V_d \text{)} &= K_1 \times K_2 \times K_3 \times V_b \\ \text{velocity} &= 1 \times 0.904 \times 1 \times 47 \\ &= 42.488 \text{ m/s} \end{aligned}$$

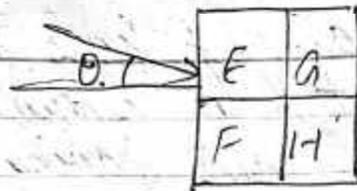
$$\begin{aligned} \text{Wind pressure (} P \text{)} &= 0.6 \times V_d^2 \\ &= 0.6 \times 42.488^2 \\ &= 1083.138 \text{ N/m}^2 \end{aligned}$$

$C_{pi} = +0.2$ (normal permeability)

$$\frac{h}{w} = \frac{12.6}{20} = 0.6 \quad 0.5 < 0.6 < 1.5$$

$$\theta = \tan^{-1} \frac{3}{10} = 16.69^\circ$$





	EF	GH
10	-1.1	-0.6
20	-0.7	-0.5
$\frac{10-20}{-1.1+0.7}$	$= \frac{10-16.69}{-1.1+x}$	

$$\therefore x =$$

$$\frac{(C_{pe})_{EF}}{10-20} = \frac{(C_{pe})_{EF}}{10-16.69} = -0.832$$

$$\frac{-0.5+0.5}{-0.6+x}$$

$$(C_{pe})_{GH} = -0.533$$

$$\frac{10-20}{-0.8+0.8} = \frac{10-16.69}{-0.8+x}$$

$$\therefore x = -0.8$$

$$(C_{pe})_{EG} = -0.8$$

$$(C_{pe})_{FH} = -0.6$$

$$\text{for } C_{pi} = +0.2$$

$$P_d = (C_{pe} - C_{pi}) P$$

$$-1117.8 \text{ N/m}^2$$

$$\text{for } (C_{pe})_{EF} = -0.832, P_d = -884.54 \text{ N/m}^2$$

$$\text{for } C_{pe} = -0.533, P_d = -793.99 \text{ N/m}^2$$

$$\text{for } C_{pe} = -0.8, P_d = -1083.13 \text{ N/m}^2$$

$$\text{for } C_{pe} = -0.6, P_d = -866.5 \text{ N/m}^2$$

for $C_{pi} = -0.2$

$$P_d = (C_{pe} - C_{pi}) P$$

for $C_{pe} = -0.832$, $P_d = -684.5 \text{ N/m}^2$

for $C_{pe} = -0.533$, $P_d = -360.68 \text{ N/m}^2$

for $C_{pe} = -0.8$, $P_d = -649.88 \text{ N/m}^2$

for $C_{pe} = -0.6$, $P_d = -433.25 \text{ N/m}^2$

Maximum design pressure = 1174.8 N/m^2
 $= 1.117 \text{ kN/m}^2$

Q) Calculate wind pressure on a roof of a building located at Chandragiri Hill having height to top from bottom of hill of 400m and average slope of 1:3. The building is located at 150m downwards from crest. The permeability of building is normal and having life expectancy of 100 yrs. The height of building is 15m to the eaves and peak pitch of $\frac{1}{3}$ with span of eaves 25m. The building is $25 \times 60 \text{ m}^2$ in dimension.

Ans $V_b = 47 \text{ m/sec}$

$K_1 = 1.07$

Terrain category - 2

Building class is 'c'

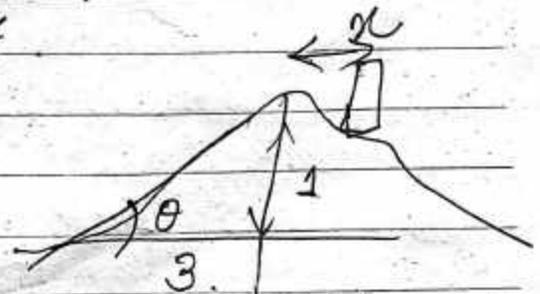
$K_2 = 0.97$

For K_3 :-

$K_3 = 1 + C_s$

$\theta = \tan^{-1}\left(\frac{1}{3}\right) = 18.43^\circ$

$C_s = 0.36$



if $3 < \theta < 1.2 \left(\frac{z}{L}\right)$ (divide)
 17°

$Z = 400 \text{ m}$, $H = 15 \text{ m}$

$x = 150 \text{ m}$ (downwards so +ve)

Pg. no. 55 $\frac{z}{L} = \frac{z}{0.3} = \frac{400}{0.3} = 1333.33 \text{ m}$

$$\frac{X}{L_e} = 0.1125$$

L_e

$$\frac{H}{L_e} = \frac{15}{1333.33} = 0.01125$$

(Cliff and encarpment.)
From fig 14: $S = 1$

$$\begin{aligned} K_3 &= 1 + C \times S \\ &= 1 + 0.36 \times 1 = 1.36 \end{aligned}$$

* ~~Part 10.~~

Purlin :-

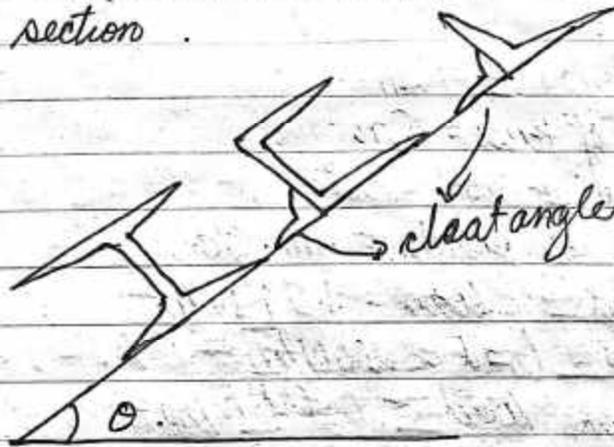
Design of Purlin:

→ It is an inclined section placed horizontally on the roof of truss.

→ There are three section particularly used in purlins.

a) I-section b) channel section.

c) Angle section.



Design steps of I-section or channel section purlin

- 1) Calculate effective length.
- 2) Calculate total load.
- 3) Calculate maximum BM & shear force.
- 4) Calculate plastic section modulus required.

$$Z_{p, req} = \frac{M_z t_{mo}}{f_y} + 2.5 \left(\frac{d}{b} \right) \frac{M_y t_{mo}}{f_y}$$

Generally $\frac{d}{b} = 2$

- 5) Select section such that $Z_p > Z_{p, req}$.
- 6) Classify the section.
- 7) Check for shear force, \neq
- 8) Check for bending moment
- 9) Check for deflection
- 10) Check for combined bending

10) Check for combined bending

$$\left(\frac{M_{xz}}{M_{z}} \right) + \left(\frac{M_{xy}}{M_{y}} \right) \leq 1$$

Q) Design I section for following data:-

span of truss = 12m

spacing of truss = 5m

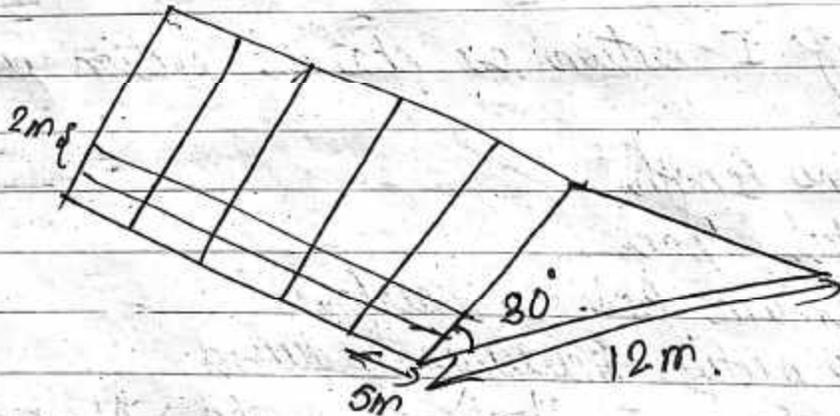
slope of roof = 30°

spacing of purlin = 2m c/c.

Wind load = 1.5 kN/m²

Dead load = 200 N/m²

live load = 0.75 kN/m²



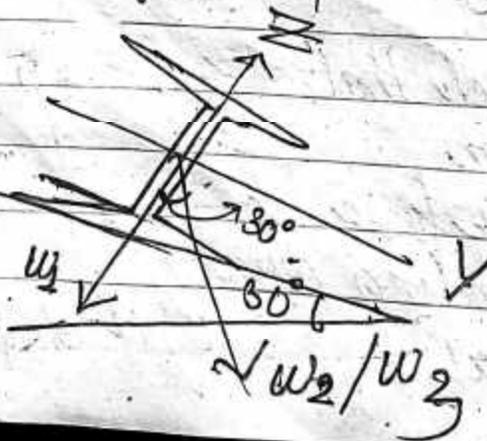
Step 1 :- Effective length of purlin = 5m

Step 2.

$$W_1 = 1.5 \times 2 = 3 \text{ kN/m}$$

$$W_2 = 0.2 \times 2 = 0.4 \text{ kN/m}$$

$$W_3 = 0.75 \times 2 = 1.5 \text{ kN/m}$$



$$\text{Factored Load along } \bar{x}\text{-axis} = \{w_1 + (w_2 + w_3) \cos \theta\} \times 1.5$$

$$= \{3 + (0.4 + 1.5) \cos 30^\circ\} \times 1.5$$

$$\text{Factored load along } y\text{-axis} = \{(w_2 + w_3) \sin \theta\} \times 1.5$$

$$= 1.42 \text{ kN/m}$$

load along z axis effects y -axis.

Step 3: - for continuous purlin section

$$M_z = \frac{w l^2}{10} = \frac{6.97 \times 5^2}{10} = 17.425 \text{ kNm}$$

$$M_y = \frac{1.42 \times 5^2}{10} = 3.55 \text{ kNm}$$

$$\text{Step 4: - } Z_{pz} = \frac{M_z t_{mo}}{f_y} + 2.5 \left(\frac{d}{b} \right) \frac{M_y t_{mo}}{f_y}$$

$$= \frac{17.42 \times 10^6 \times 1.1}{250} + \frac{2.5 \times 2 \times 3.56 \times 10^6 \times 1.1}{250}$$

$$= 199056 \text{ mm}^3 = 199.056 \text{ cm}^3$$

$$= 155504.8 \text{ mm}^3$$

$$= 155.505 \text{ cm}^3$$

See Z_p only from
38 other
all from IS 808.

Step 5: ISMB 200

$$Z_p = 258.86 \text{ cm}^3$$

$$D = h = 200 \text{ mm} \quad B = B_f = 100 \text{ mm}$$

$$T = t_f = 6.7 \text{ mm} \quad t = t_w = 6.7 \text{ mm}$$

$$I_{xx} = 2120 \text{ cm}^4 \quad I_{yy} = 137 \text{ cm}^4, R_1 = 11 \text{ mm}$$

$$Z_{xy} = Z_{yx} = 228.8 \text{ cm}^3, Z_x = Z_y = 258.86 \text{ cm}^3$$

$$Z_z = Z_x = Z_{rx} = 212.4 \text{ cm}^3$$

$$Z_y = Z_{ry} = 27.4 \text{ cm}^4$$

Step 6: $b = \frac{100}{2} = 50 \text{ mm}$

$$d = 200 - 2(t_f + R_1) = 158 \text{ mm}$$

$$\frac{b}{t_f} = \frac{50}{10} = 5 \leq 9.4 \epsilon \text{ (plastic)}$$

$$\frac{d}{t_w} = \frac{158}{6.7} = 23.7 \leq 84 \epsilon \text{ (plastic)}$$

Hence, section is plastic.

Step 7: $V_z = \frac{W_z l}{2} = \frac{6.97 \times 5}{2} = 17.42 \text{ kN}$

$$V_y = \frac{W_y l}{2} = \frac{1.42 \times 5}{2} = 3.55 \text{ kN}$$

$$V_dz = \frac{A_v f_y}{\sqrt{3} t_{mo}} = \frac{D \times t_w \times 250}{\sqrt{3} \times 1.1}$$

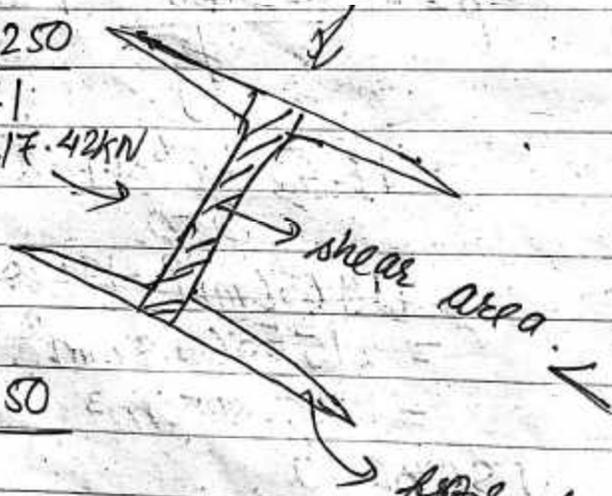
$$= 149.5 \text{ kN} > 17.42 \text{ kN}$$

OK

$$V_{dy} = \frac{A_v f_y}{\sqrt{3} t_{mo}}$$

$$= \frac{2 \times 16 \times t_f \times 250}{\sqrt{3} \times 1.1}$$

$$= 262.43 \text{ kN}$$



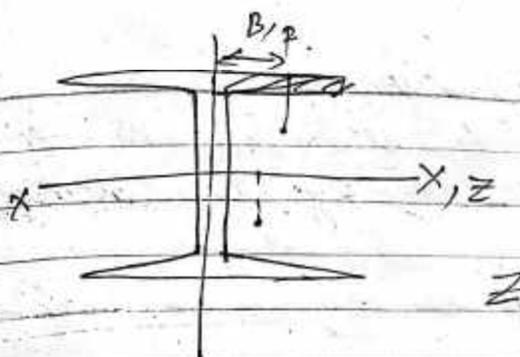
lateral loading

Step 8: $M_dz = \frac{\rho_b \times Z_p z f_y}{t_{mo}}$

$$= \frac{1 \times 253.86 \times 250 \times 10^3}{1.1} = 57695.45$$

$$= 57.69 \text{ kN-m}$$

OK



$$Z_{py} = 4 * \left[\frac{B}{2} * t_f * \frac{B}{4} \right] + 2 * \left[\frac{(D - 2t_f) * t_w * t_w}{2} \right]$$

$$= 51.46 \text{ cm}^3$$

$$M_{dy} = \frac{Z_{py} f_y}{\gamma_{mb}} = \frac{51.46 \times 10^3 \times 250}{1.1} = 11.681 \text{ kN-m} \geq 3.56 \text{ kN-m}$$

OK

Step 9: $\delta = \frac{5 w l^4}{384 EI}$

$$= \frac{5 * 6.95 \times 5000^4}{384 * 2 \times 10^5 * 2120 \times 10^4} = 18.38 \text{ mm} \cdot 8.91 \text{ mm}$$

$$\delta_{per} = \frac{l}{180} = \frac{5000}{180} = 27.78 \text{ mm} > 18.37 \text{ mm OK}$$

Step 10: $\frac{M_z}{M_{dz}} + \frac{M_y}{M_{dy}}$

$$= \left(\frac{17.425}{57.69} \right) + \left(\frac{3.563}{11.681} \right)$$

$$= 0.61 < 1 \text{ OK}$$

NW - Same question for Channel section.

Compare Z_x see IS 808 not Z_p .
 Z_{pz} & Z_{py} also calculate.

Angle Section Section Purlin
Design steps

1. Calculate effective length
2. Calculate total load and assume all the loads perpendicular to surface.
3. Calculate maximum bending moment & shear force.
4. Calculate section modulus required as:-

$$Z_{req} = \frac{M}{f_y}$$

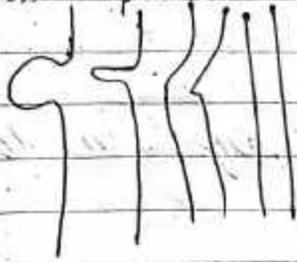
5. Select sections such that $Z_x \geq Z_{req}$ and depth not less than $\frac{\text{span}}{45}$ and width not less than $\frac{\text{span}}{60}$.

6. Check for bending moment capacity.

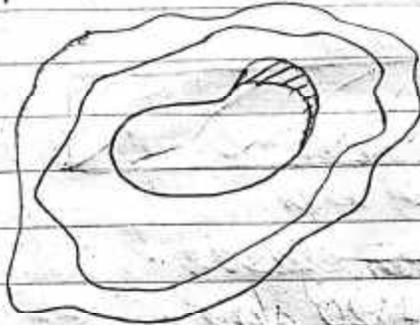
Chapter 9-12

Timber Structure

a) Defects in timber structures - knots



b) shake



c) check



d) warping, etc.



*) Structural timber

A well seasoned timber without any major defect and having better strength to weight ratio is known as structural timber.

Factors affecting strength of timber

- 1) Moisture :- Moisture content should be in between 10-15% but moisture content of 12% is preferred. It should be free of free moisture.

(ii) Density - Higher density represents higher amount of wood which means higher strength.

(iii) Defects :- There should not be major defects in timber.

(iv) Slope and type of grain



less slope \rightarrow not good
more slope \rightarrow good

Types of timber as per grain grade.

1. Select grade \rightarrow 1:20 slope.
2. Grade-I \rightarrow 1:15 - 1:20
3. Grade-II \rightarrow 1:12

IS-883 pg-10-6-8

Except 'E' all values are multiplied by 1.16 and 0.84

* Timber method is calculated by working stress method. if factored load is given then calculate using equivalent

* Grouping of timber (5.1.1 Table 19.2)

* Design of Timber Beam:-

(if not mentioned inside taken)
Working stress \Rightarrow Elastic method.

- (i) Bending
(ii) shear (iii) Bearing (iv) deflection

Design a sal wood timber beam of span 4m carrying UDL of 16 kN/m (8 kN/m dead load + 8 kN/m live load).

Solⁿ

Table-1.

for sal wood Pg. 3.

$$E = 126.7 \times 100 \text{ N/mm}^2$$

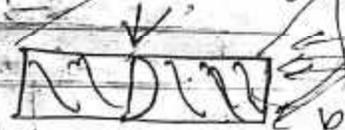
$$\sigma_b = 16.9 \text{ N/mm}^2$$

$$\tau_u = 0.94 \text{ N/mm}^2$$

$$\sigma_{cb} = 4.6 \text{ N/mm}^2$$

$$\rho = 805 \text{ kg/m}^3$$

Shear stress (horizontal)



(i) Bending: (assume 200 x 400 beam)

load calculation

(i) DL = 8 kN/m

(ii) LL = 8 kN/m

(iii) self weight = $8 \times 0.2 \times 0.4 \times l \times g$

$$= 805 \times 0.2 \times 0.4 \times 10$$

$$= 0.644 \text{ kN/m}$$

total load = 16.644 kN/m

$$M_{max} = \frac{wl^2}{8} = \frac{16.644 \times 4.23^2}{8}$$

assume 230 mm support width

$$\text{Effective length} = 4 + \frac{0.23}{2} + \frac{0.23}{2}$$

$$= 4.23$$

since, $M = \sigma \times Z$

$$\text{or, } 37.266 \times 10^6 = 16.9 \times Z$$

$\therefore Z = 2202721.89 \text{ mm}^3$ (Elastic section modulus)

$$Z = \frac{bd^2}{6}$$

Let, ~~b=2d~~ $d = 2b$.

$$\frac{b(2b)^2}{6} = Z$$

$$\therefore b = 148.9 \text{ mm}$$

Let $b = 150 \text{ mm}$; $d = 300 \text{ mm}$

(ii) Top shear: (support to centre of 'd' distance in beam is critical in shear)



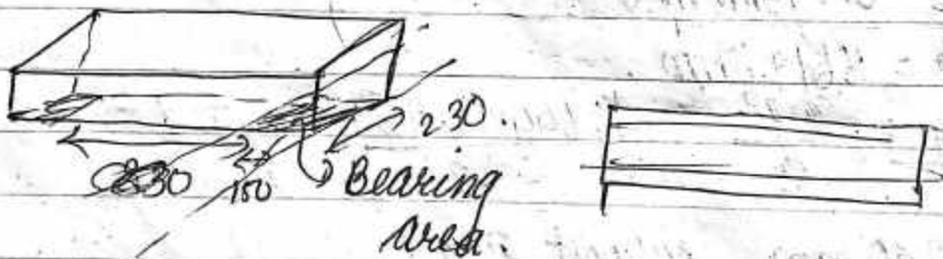
$$\text{Shear stress } (\tau) = \frac{V \times 1.5}{bd}$$

$$= \frac{30.2 \times 10^3 \times 1.5}{150 \times 300}$$

$$= 1.0067 \text{ N/mm}^2 \leq 0.94 \text{ N/mm}^2$$

$$\Rightarrow = 1.0065 \text{ N/mm}^2 \leq 0.94 \text{ N/mm}^2 \quad \text{OK}$$

(iii) Bearing: - Bearing stress = $\frac{wl}{2} = \frac{16.644 \times 4.23}{2} = 35.2 \text{ kN}$



$$\text{Bearing stress} = \frac{35.2 \times 10^3}{230 \times 150}$$

$$= 1.02 \text{ N/mm}^2 \leq 4.60 \text{ N/mm}^2 \quad \text{OK}$$

$\frac{wl}{2}$

(iv) Deflection

Take 200×400

$$v = wl \left(\frac{l^2}{2} - d \right)$$

$$\begin{aligned} \text{Load per deflection} &= 2 \times DL + 0.75 \times LL \\ &= 2 \times (8 + 0.644) + 0.75 \times 8 \\ &= 23.288 \text{ kN/m} \end{aligned}$$

$$\begin{aligned} \delta_{\text{max}} &= \frac{5}{384} \frac{w l^4}{EI} = \frac{5}{384} \times 23.288 \times \frac{4230^4}{126.7 \times 10^2 \times \left[\frac{150 \times 300^3}{12} \right]} \\ &= 22.7 \text{ mm} \end{aligned}$$

$$\delta_{\text{per}} = \frac{\text{Span}}{240} = \frac{4230}{240} = 17.62 \text{ mm} \leq 22.7 \text{ mm} \quad \text{not ok.}$$

Increase size to 200 x 400 mm

$$\delta_{\text{max}} = 7.18 \text{ mm} \leq \delta_{\text{per}} \quad \text{OK}$$

$$\frac{\delta_{\text{max}}}{\delta_{\text{per}}} = \frac{I_{\text{new}}}{I}$$

$$I_{\text{new}} = \frac{\delta_{\text{max}}}{\delta_{\text{per}}} \times I$$

*) adopt 200 x 400 mm sal wood timber beam

Pg. no. 11. 7.5. Flexure of

7.5.7.2.

$$W = w \times l$$

7.5.9. deflection

Design a deodar beam of span 5m

to carry UDL of 20 kN/m if support of 200 mm is provided.
Also note that timber is of select grade and to be used in terrace.

$$\text{Ans } l_{\text{eff}} = l + \frac{0.2}{2} + \frac{0.2}{2}$$
$$= 5.2 \text{ m}$$

For deodar wood.

Terrace \rightarrow outside.

$$s = 557 \text{ Kg/m}^3$$

$$E = 94.8 \times 10^2 \text{ N/mm}^2$$

$$\sigma_b = 8.7 \text{ N/mm}^2 \times 1.16 = 10.092 \text{ N/mm}^2$$

$$\sigma_{cd} = (2.1 \text{ N/mm}^2) \times 1.16 = 2.436 \text{ N/mm}^2$$

$$\tau_v = 0.7 \text{ N/mm}^2 \times 1.16 = 0.812 \text{ N/mm}^2$$

load calculation :- (200 \times 400 mm beam)

(i) UDL = 20 kN/m

(ii) self weight = $557 \times 0.2 \times 0.4 \times 10$
= 0.445 kN/m

total load = 20.445 kN/m

(i) Bending σ

$$M_{\text{max}} = \frac{wl^2}{8}$$

$$= \frac{20.445 \times 5.2^2}{8}$$

$$= 69.106 \text{ kNm}$$

$$M = 2 \times \sigma_b$$

$$\frac{M}{Z} = \sigma_b$$

$$\text{assume } d = 2b$$

We know, $M = \sigma_b \times Z$

$$\text{or, } 69.106 \times 10^6 = 10.09 \times \left[\frac{b \times d (2b)^2}{6} \right] \quad \therefore \text{(assume } b = 2b)$$

$$b = 217.99 \text{ mm}$$

$$\approx 250 \text{ mm}$$

$$d = 500 \text{ mm}$$

Since $d > 300 \text{ mm}$

$$k_3 = 0.81 \times \left[\frac{d^2 + 89400}{d^2 + 55000} \right] \quad \left(\begin{array}{l} 28883 \\ \text{Cl. 7.5.4} \end{array} \right)$$

$$= 0.81 \times 0.901$$

$$\begin{aligned} \text{Moment carrying capacity} &= (k_3 Z) \times \sigma_b \\ &= 0.901 \times \left[\frac{250 \times 500^2}{6} \right] \times 10.09 \\ &= 99.7 \text{ kN-m} > 69.106 \text{ kN-m} \end{aligned}$$

(ii) Shear :- $V_{\max} = W \left(\frac{l}{2} - d \right)$

$$= 20.445 \left(\frac{5.2}{2} - 0.5 \right)$$
$$= 42.93 \text{ kN}$$

$$\begin{aligned} \tau &= 1.5 \frac{V_{\max}}{bd} = 1.5 \times \frac{42.93}{250 \times 500} \\ &= 0.515 \text{ N/mm}^2 \leq 0.81 \text{ N/mm}^2 \quad (\text{OK}) \end{aligned}$$

(iii) Bearing stress.

$$\text{Bearing force} = \frac{Wl}{2}$$

$$= \frac{20.445 \times 5.2}{2} = 52.135 \text{ kN}$$

2

$$\text{Bearing stress} = \frac{52.135 \times 10^3}{250 \times 200}$$

$$= 1.04 \text{ N/mm}^2 \leq 2.436 \text{ N/mm}^2 \text{ (OK)}$$

(iv) Deflection :-

$$\delta_{\text{max}} = \frac{5wL^4}{384 EI}$$

$$= \frac{5}{384} * \frac{20.445 \times 5200^4}{94.8 \times 10^2 * \left[\frac{250 \times 500^3}{12} \right]}$$

$$= 7.88 \text{ mm}$$

$$\delta_{\text{per}} = \frac{\text{span}}{240} \quad (7.5.9)$$

$$= \frac{5200}{240}$$

$$> 21.67 \text{ mm} \geq 7.88 \text{ mm (OK)}$$

Adopt 250 x 500 mm deodar timber beam

Design of Columns :-

Types :

- i) Solid column
- ii) Box/Built-up column
- iii) Spaced column.

Solid columns:

- i) Short column : $\frac{l}{d} \leq 11$.

d = least lateral dimension

$$\sigma'_{cp} = \sigma_{cp}$$

- ii) Intermediate column :- $11 < \frac{l}{d} \leq K_g$.

$$\sigma'_{cp} = \sigma_{cp} \left[1 - \frac{1}{3} \left(\frac{l}{K_g d} \right)^4 \right]$$

- iii) Long column :- $\frac{l}{d} > K_g$

$$\sigma'_{cp} = \frac{0.829 E}{\left(\frac{l}{d} \right)^2}$$

l = length of column

σ_{cp} = Permissible compressive strength parallel to grain.

σ'_{cp} = modified " " " " " "

$$K_g = 0.702 \sqrt{\frac{E}{\sigma_{cp}}}$$

0.584 in K_g & K_{10}

should be replaced

by 0.702 in code.

$f = \sigma$ in code

Rg. 14 $\rightarrow l = s, \sigma = f$

6 Marks

Q) Calculate load carrying capacity of teak wood column of length 5m and having lateral dimension of 300×300 mm. Timber is of grade II.

Ans For teak wood (UP),

$$E = 99.7 \times 100 \text{ N/mm}^2$$

$$\sigma_{cp} \text{ (Compression parallel to grain)} = 9.4 \times 0.89 = 7.896 \text{ N/mm}^2$$

Now,

$$\frac{l}{d} = \frac{5000}{300}$$

$$= 16.67 > 11$$

d = least lateral dimension

$$K_g = 0.702 \sqrt{\frac{E}{\sigma_{cp}}} = 0.702 \sqrt{\frac{99.7 \times 10^2}{7.896}} = 24.945$$

$11 < \frac{l}{d} \leq K_g$, so it is intermediate column.

$$\begin{aligned} \sigma_{cp}' &= \sigma_{cp} \left[1 - \frac{1}{3} \left(\frac{l}{K_g d} \right)^4 \right] \\ &= 7.896 \times \left[1 - \frac{1}{3} \times \left(\frac{5000}{24.945 \times 300} \right)^4 \right] \\ &= \cancel{7.896} \times 7.87 \text{ N/mm}^2 \end{aligned}$$

$$\begin{aligned} \text{Then, load carrying capacity} &= \sigma_{cp}' \times A \\ &= 7.37 \times 300 \times 300 \\ &= 884.4 \text{ kN} \end{aligned}$$

Q) Design sal wood, timber column of 4m length to carry axial load of 300kN.
 Ans: For sal wood.

$$E = 126.7 \times 10^2 \text{ N/mm}^2$$

$$\sigma_{cp} = 10.6 \text{ N/mm}^2$$

$$\text{Then } A_{req} = \frac{P}{\sigma_{cp}} = \frac{300 \times 10^3}{10.6} = 28301.886 \text{ mm}^2$$

Assume, square column.

$$b = d = \sqrt{28301.886} \\ = 168.23 \text{ mm} \\ = 200 \text{ mm}$$

$$\text{Now, } \frac{l}{d} = \frac{4000}{200} = 20 > 11$$

$$K_8 = 0.702 \sqrt{\frac{E}{\sigma_{cp}}} \\ = 0.702 \sqrt{\frac{126.7 \times 10^2}{10.6}} \\ = 24.27$$

$11 < \frac{l}{d} \leq K_8$, so it is intermediate column

$$\sigma'_{cp} = \sigma_{cp} \left[1 - \frac{1}{3} \left(\frac{l}{K_8 d} \right)^4 \right]$$

$$= 10.6 * \left[1 - \frac{1}{3} \left(\frac{4000}{24.27 * 200} \right)^4 \right]$$

$$= 7.69 \text{ N/mm}^2 \quad 8.97 \text{ N/mm}^2$$

$$\text{load carrying capacity} = \sigma'_{cp} * A_{gr} \\ = 7.69 * 200 * 200$$

$$= 307.6 \text{ kN} > 300 \text{ kN}$$

(ii) Box / Built-up column:

a) short column:

$$\frac{l}{\sqrt{d_1^2 + d_2^2}} \leq 8$$

$$\sigma'_{cp} = \sigma_{cp}$$

b) Intermediate column:

$$8 < \frac{l}{\sqrt{d_1^2 + d_2^2}} \leq k_g$$

$$\sigma'_{cp} = \sigma_{cp} \left[1 - \frac{1}{3} \left(\frac{l}{k_g \sqrt{d_1^2 + d_2^2}} \right)^4 \right]$$

(iii) long column:

$$\frac{l}{\sqrt{d_1^2 + d_2^2}} > k_g$$

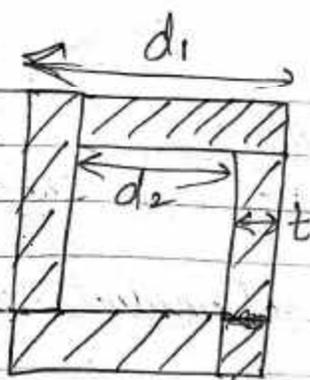
$$\sigma_{cp} = 0.329UE$$

$$\left(\frac{l}{\sqrt{d_1^2 + d_2^2}} \right)^2$$

$d_1 + d_2 =$ least external & internal dimension

$$k_g = \frac{\pi}{2} \sqrt{\frac{UE}{5\sigma_{cp}}}$$

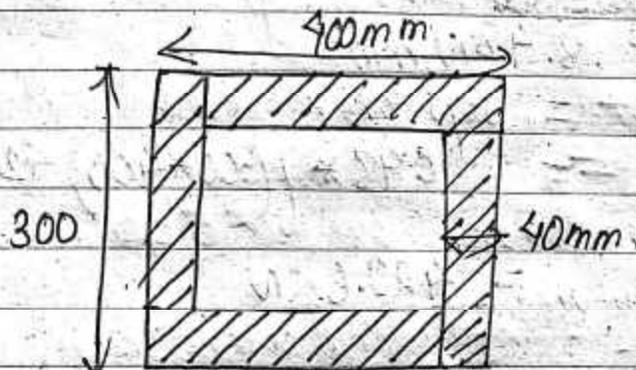
$U =$ modification factor depending upon thickness of plank



200×300

cl. 7.6.2.5

Q) Calculate load carrying capacity of 6m box column made of oak wood having following section:-



→ Solⁿ:- for oak wood (west Bengal) @ 874 kg/m^3

$$E = 126.3 \times 10^2 \text{ N/mm}^2$$

$$f_{cp} = 9.6 \text{ N/mm}^2$$

$$d_1 = 400 \text{ mm}, \quad d_2 = 300 - 2 \times 40 = 220 \text{ mm}$$

$$\text{Then, } \frac{l}{\sqrt{d_1^2 + d_2^2}} = \frac{6000}{\sqrt{400^2 + 220^2}} = 16.128 > 8$$

$$\frac{t}{25}$$

$$25$$

$$50$$

$$0$$

$$0.8$$

$$0.6$$

$$\frac{25 - 0}{0.8 - 0.6} = \frac{25 - 40}{0.8 - x}$$

$$\therefore x = 0.68$$

$$K_g = \frac{\pi}{2} \sqrt{\frac{UE}{5\sigma_{cp}}} = \frac{\pi}{2} \sqrt{\frac{0.68 \times 126.3 \times 10^2}{5 \times 9.6}}$$

Since, $8 < \frac{l}{d} < K_g$, so it is intermediate column.

$$\sigma'_{cp} = \sigma_{cp} \left[1 - \frac{1}{3} \left(\frac{l}{K_g \sqrt{d_1^2 + d_2^2}} \right)^4 \right]$$

$$= 9.6 \left[1 - \frac{1}{3} \left(\frac{8000}{21 \sqrt{300^2 + 220^2}} \right)^4 \right]$$

$$= 7.934 \text{ N/mm}^2 \cdot 8.48 \text{ N/mm}^2$$

$$\text{Load carrying capacity} = \sigma_{cp}' \times A$$

$$= 8.48 \times [(300 \times 400) - (220 \times 320)]$$

Q) Design a box column using 420.6 kN

Design a box column using 60mm thick salwood plank to carry 400kN load in a column of 3.5m length

Ans solⁿ :- for salwood :-

$$E = 126.7 \times 10^2 \text{ N/mm}^2$$

$$\sigma_{cp} = 10.6 \text{ N/mm}^2$$

$$A_{req} = \frac{400 \times 10^3}{10.6}$$

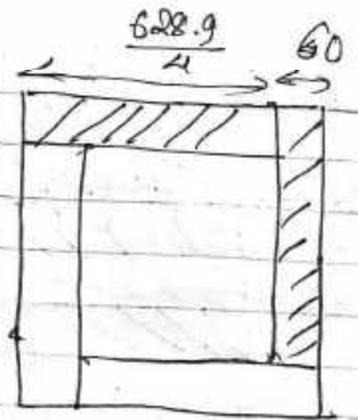
$$= 37735.85 \text{ mm}^2$$

$$\text{length of total plank} = 37735.85$$

$$= \frac{60}{4} = 628.9 \text{ mm}$$

$$\text{Each side of column} = \frac{628.9 + 60}{4} = 217.25 \text{ mm}$$

$$\approx 250 \text{ mm}$$



$$d_1 = 250 - 60 = 190$$

$$d_2 = 250 - 60 = 190$$

$$d_1 = 250$$

$$d_2 = 250 - 2 \times 60 = 130 \text{ mm}$$

$$\frac{l}{\sqrt{250^2 + 130^2}} = 12.42 > 8$$

t	U
25	0.8
50	0.6
25 50	0.8 0.6

$$U = 0.6$$

$$K_g = \frac{\pi}{2} \sqrt{\frac{0.6 \times 126.7 \times 10^2}{5 \times 10^6}}$$

$$= 18.81$$

$$\frac{l}{\sqrt{d_1^2 + d_2^2}} < K_g$$

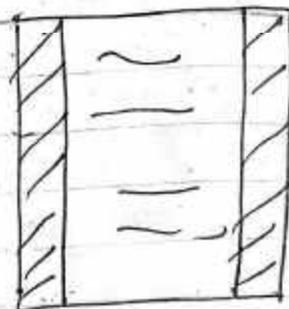
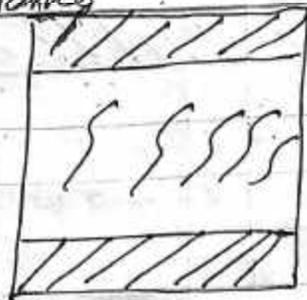
$$\sigma'_{cp} = \sigma_{cp} \left[1 - \frac{1}{3} \left(\frac{l}{K_g \sqrt{d_1^2 + d_2^2}} \right)^4 \right]$$

$$= 9.93 \text{ N/mm}^2$$

$$\text{Load carrying capacity} = 9.93 \times [(250 \times 250) - (130 \times 130)]$$

$$= 452.81 \text{ kN} > 400 \text{ kN ok}$$

✓✓
Moment of resistance



*) Column under Bending & axial combined.

$$\left(\frac{\sigma_{b, cal}}{\sigma_b} \right) + \left(\frac{\sigma_{c, cal}}{\sigma_{cp}} \right) \leq 1.0$$

$\sigma_{cp} \rightarrow$ compressive permissible stress

$$\sigma_{b, cal} = \frac{M}{Z} = \text{calculated Bending stress}$$

if so for σ_{cp} if σ_{cp} in any condition we use σ'_{cp} .

$$\sigma_{c, cal} = \frac{P}{A} = \text{calculated compression stress}$$

Q) Check the safety of a solid column 300mm x 400mm of Sal wood having unsupported length of 4m and acted by axial force of 200kN and bending moment of 25kNm.

Ans Solⁿ :- for salwood.

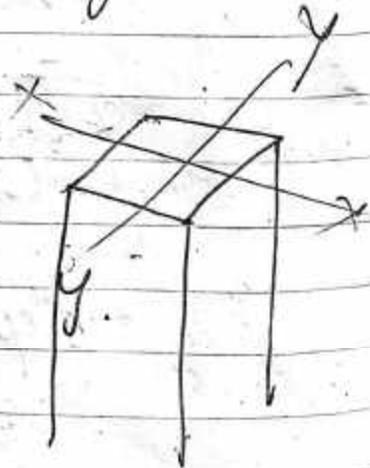
$$E = 126.7 \times 10^2 \text{ N/mm}^2$$

$$\sigma_b = 16.9 \text{ N/mm}^2$$

$$\sigma_{cp} = 10.6 \text{ N/mm}^2$$

Bending :-

$$\sigma_{b, cal} = \frac{M}{Z} = \frac{25 \times 10^6}{400 \times 300^2}$$



Minimum Z'

6.

$$= 4.17 \text{ N/mm}^2 \leq 16.9 \text{ N/mm}^2 \text{ (OK)}$$

Compression: $\sigma_{c, cal} = \frac{P}{A} = \frac{200 \times 10^3}{300 \times 400}$
 $= 1.67 \text{ N/mm}^2$

$$\frac{l}{d} = \frac{4000}{300} = 13.33 > 11$$

$$K_8 = 0.702 \sqrt{\frac{E}{\sigma_{cp}}}$$

$$= 0.702 \sqrt{\frac{126.7 \times 10^2}{10.6}}$$

$$= 0.702 \cdot 24.27$$

Since,

$11 < \frac{l}{d} \leq K_8$, it is intermediate column.

$$\sigma'_{cp} = \sigma_{cp} \left[1 - \frac{1}{3} \left(\frac{l}{K_8 d} \right)^4 \right]$$

$$= 10.28 \text{ N/mm}^2 > 1.68 \text{ N/mm}^2 \text{ (OK)}$$

Finally $\left(\frac{\sigma_{b, cal}}{\sigma_b} \right) + \left(\frac{\sigma_{c, cal}}{\sigma_{cp}} \right)$

$$= \frac{4.17}{16.9} + \frac{1.68}{10.28}$$

$$= 0.41 \leq 1.0 \text{ (OK)}$$

Hence the section is safe.

* Design salwood timber column of 5m to carry an axial load of 250kN and bending moment of 35kNm

Solⁿ: For sal wood.

$$E = 126.7 \times 10^2 \text{ N/mm}^2$$

$$\sigma_b = 16.9 \text{ N/mm}^2$$

$$\sigma_{cp} = 10.6 \text{ N/mm}^2$$

$$A_{req} = \frac{P}{\sigma} = \frac{250 \times 10^3}{10.6} = 23584.9 \text{ mm}^2$$

Assume square column

$$d = b = \sqrt{A_{req}} = 153.57 \text{ mm}$$

Adopt 200 x 200 (double calculated size) column

Chapter (10-12)

Timber structure

Spaced column:

→ All parameters similar to solid column only effective length is to be calculated.

$$l_{eff} = \frac{l}{\sqrt{R.F.}}$$

R.F = reduction factor

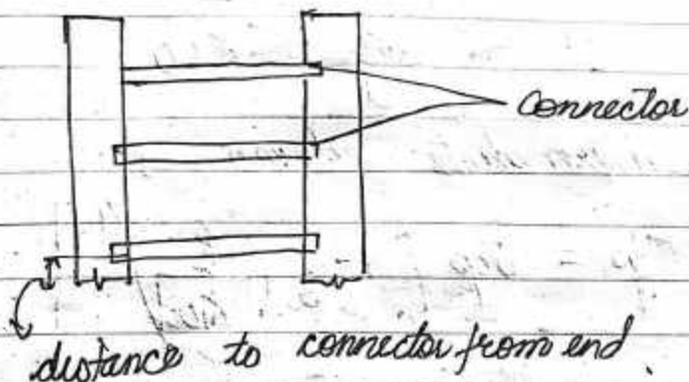
= 2.5 for distance of connector at $\frac{l}{20}$ from

= 3 support " " " " " " at $\frac{l}{10}$ " "

$K_1 = 0$ instead of K_8 .

$$K_{10} = 0.702 \sqrt{\frac{2.5E}{\sigma_{cp}}} \quad \& \quad \text{for load column}$$

$$\sigma'_{cp} = \frac{0.329E \times 2.5}{\left(\frac{l}{d}\right)^2}$$



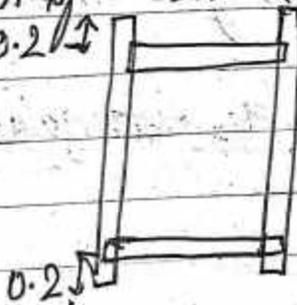
Q) Calculate load carrying capacity of a spaced column consisting of 2 planks 60×300 connected by connectors placed at 200mm from support if the length of the column is 4m. The column is made of sal wood.

Solⁿ :-

Distance of connector = 200mm
which is exactly $\frac{1}{20}$ ($\frac{4000}{20}$) from support

Hence, R.F = 2.5
Pg. no. 14 7.6.3

(l_c) length of end connector to end connected = $4 - 2 \times 0.2 = 3.6m$



$$l_{eff} = \frac{l_c}{\sqrt{2.5}} = 2.27m$$

$$\frac{l_{eff}}{d} = \frac{2.27}{0.06} = 37.94 > 1$$

$$K_{10} = 0.702 \sqrt{\frac{2.5E}{\sigma_{cp}}}$$

For salwood

$$E = 126.7 \times 10^2 \text{ N/mm}^2$$

$$\sigma_{cp} = 10.6 \text{ N/mm}^2$$

$$K_{10} = \cancel{39.89} 38.87$$

Since, $11 < \frac{l_{eff}}{d} \leq K_{10}$

it is intermediate column.

$$\sigma_{cp} = \sigma_{cp} \left[1 - \frac{1}{3} \left(\frac{l_{eff}}{K_{10}d} \right)^4 \right]$$

$$= 10.6 \left[1 - \frac{1}{3} \left(\frac{37.94}{38.87} \right)^4 \right]$$

$$= 7.22 \text{ N/mm}^2$$

$$\begin{aligned} \text{load carrying capacity} &= \sigma_{cp}' \times A \\ &= 7.22 \times (2 \times 60 \times 300) \\ &= 259.92 \text{ kN} \end{aligned}$$

Q) Design a spaced column to be used as a 8m long column carrying 250kN axial load and made of oak

Q) Design a circular salwood column of 8.5m length and having to carry 200kN axial load.

$\left(\frac{l}{d}\right) \rightarrow$ for rectangular / square

Ans $E = 126.7 \times 10^2 \text{ N/mm}^2$

$$\sigma_{cp} = 10.6 \text{ N/mm}^2$$

2

$$\text{Area required} = \frac{200 \times 10^3}{10.6} = 188.67 \text{ mm}^2 \quad 18867 \text{ mm}^2$$

Taking equivalent square section

$$d = \sqrt{18867}$$
$$= 137.35$$
$$\approx 150 \text{ mm}$$

Equivalent circle :-

$$\frac{\pi}{4} \times D^2 = 150^2$$

$$D = \dots$$

(*) Nail connection in two timber

→ Pitch $\geq 5d$ in tension

$\geq 10d$ in compression

end distance $\geq 2.5 \times d$

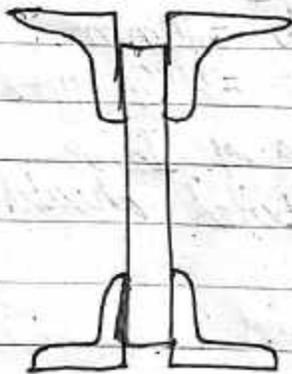
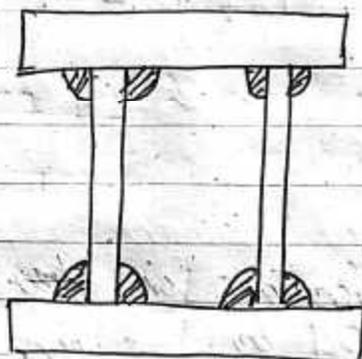
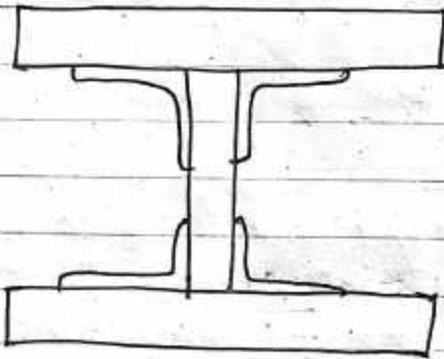
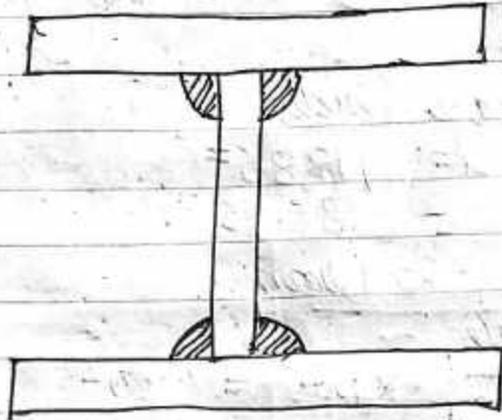
Minimum thickness of plank = 15mm

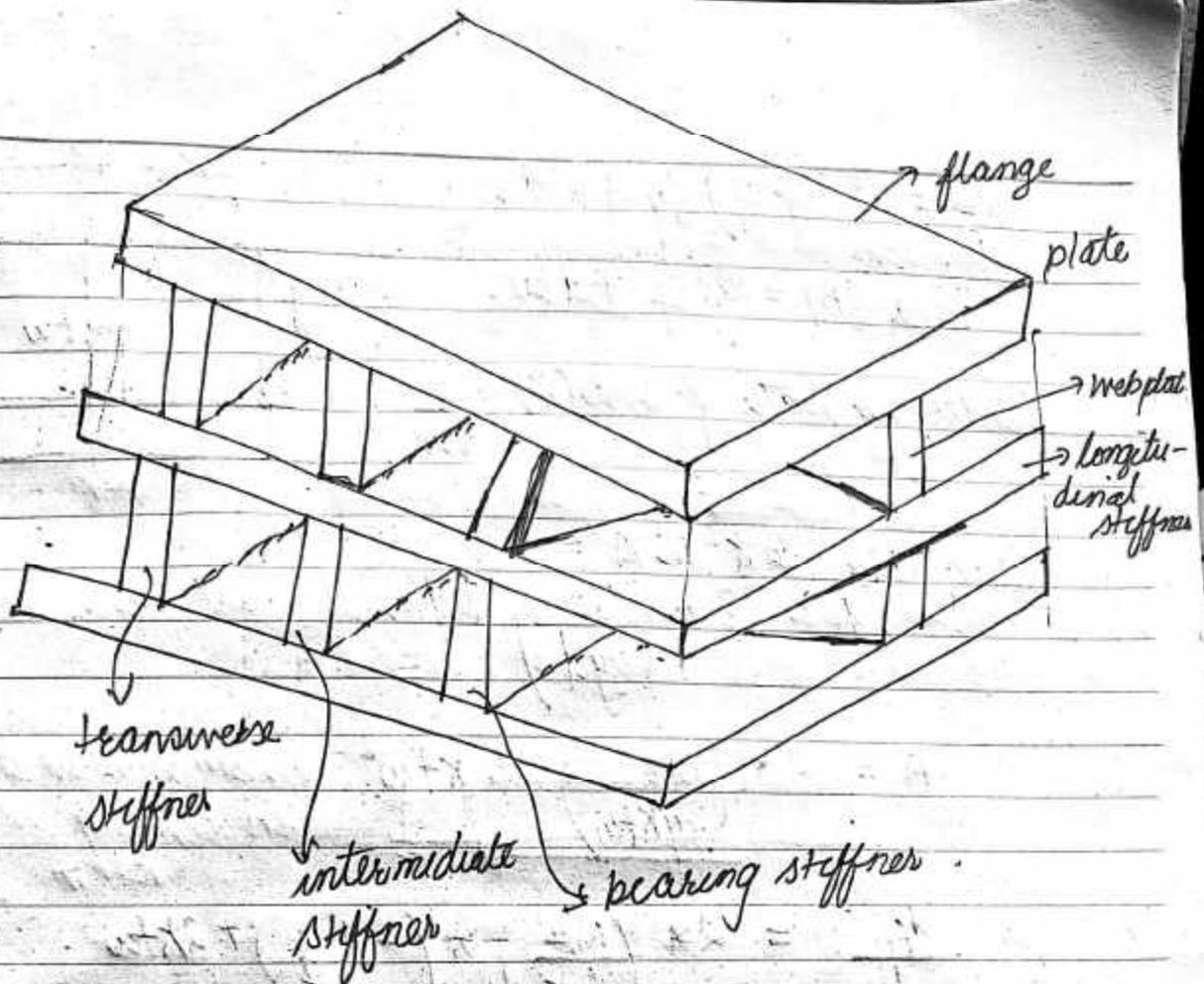
maximum thickness " " = 100mm

width of plank $\leq 8 \times$ thickness of plank

width of gusset plate combined should be less than main member thickness

Plate girders (when at high shear conditions)





Components of plate girder: (8.6)

- 1) flange plate
- 2) web-plate
- 3) splices (web & flange splice)
- 4) stiffener.

Economical depth of plate girder.

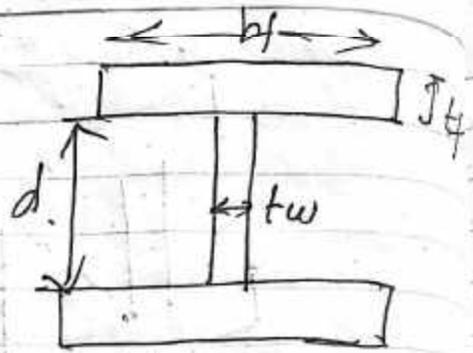
Depth taken between $\frac{1}{6}$ to $\frac{1}{15}$ of span but $\frac{1}{28}$ to $\frac{1}{12}$ of

span is preferred. Reducing area may increase depth causing difficulty in transportation.

$$M_z = [(bftf) f_y] * d.$$

$$\text{Area } (A) = 2bftf + dtw.$$

$$\text{Slenderness ratio of web } (k) = \frac{d}{tw}.$$



Using M_z & k in 'A'

$$A = 2 * \left(\frac{M_z}{f_y k} \right) + dtw.$$

$$A = 2 * \left(\frac{M_z}{f_y k tw} \right) + k tw^2.$$

$$\frac{dA}{dtw} = 2 * \left(\frac{M_z}{f_y k} \right) * \left(-\frac{1}{tw^2} \right) + 2k tw.$$

$$\text{for minima, } \frac{dA}{dtw} = 0$$

$$0 = -2 * \left(\frac{M_z}{f_y k} \right) \frac{1}{tw^2} + 2k tw$$

$$\left(\frac{2M_z}{f_y k} \right) = 2k tw^3.$$

$$\therefore tw = \left(\frac{M_z}{f_y k^2} \right)^{0.33}$$

$$A = 2 \left(\frac{Nz}{f_y k t_w} \right) + d t_w$$

$$A = 2 * \left(\frac{Nz}{f_y k \frac{d}{k}} \right) + d * \frac{d}{k}$$

N.w.r. to 'd'

$$\frac{dA}{dd} = - \frac{2 * Nz}{f_y d^2} + \frac{2d}{k}$$

for minima

$$\frac{2 Nz}{f_y d^2} = \frac{2d}{k}$$

$$d = \left(\frac{Nz k}{f_y} \right)^{0.33}$$

check

(x) Design a plate girder (web splice), column under eccentric loading (9.1, d. 9.3.2.2).

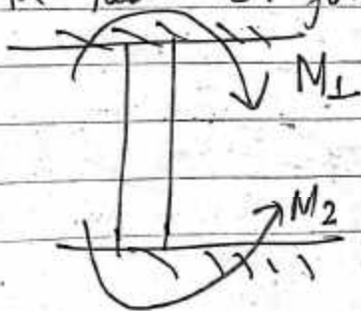
pg. 71.

$n_y = \frac{\text{x-direction load}}{\text{capacity}}$

$$\lambda_y = \sqrt{\frac{f_y}{f_{ec}}}$$

In n_y use n_y
In λ_y use m .

pg. no. 72 Table 18. for C_m & e_m .



$$M_1 \leq M_2$$

$$\psi = \frac{M_1}{M_2}$$

C_{mf} is smaller of C_{m1} & C_{m2} .

~~$M_2 = \psi$~~
Cl. 9.8.1.3.

In case of weld we use -

(*) Curtailment of plate

(~~$\neq V_{max}$~~)
when ~~moment~~ is max at sides but ~~min~~

When shear force is max at sides but min. at middle
then we curtail plate at middle.



as BM is max at middle
in simply supported
beam